

# Shock Electrochemistry in Porous Media

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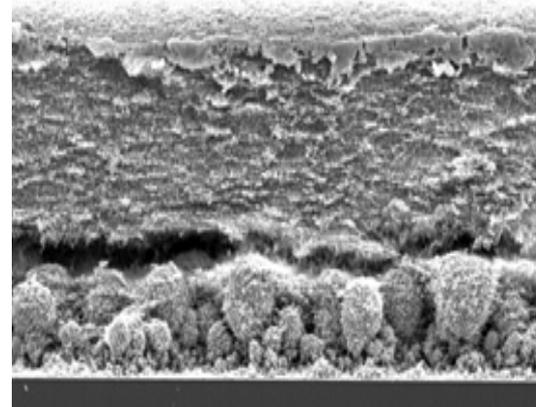
*GCEP Chair, Visiting Professor, Stanford (2015-16)*

## Students:

Sven Schlumpberger, Nancy Lu  
(Vicki Dydek)

## Postdocs:

Jihyung Han, Peng Bai  
(Ali Mani, Daosheng Deng, Matt Suss)



# Classical Models of Transport in Porous Media:

## *Linear Response*

Darcy's law  
Ohm's law  
Fick's law

Electro-osmosis    Diffusio-osmosis  
Diffusion current

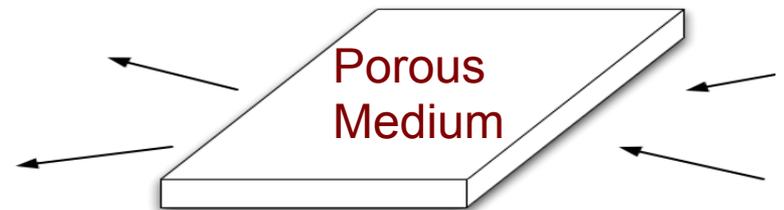
**Fluxes**

$$\begin{pmatrix} Q \\ I \\ F \end{pmatrix} = \begin{pmatrix} K_H & K_{EO} & K_{DO} \\ K_{EO} & K_E & K_{DC} \\ K_{DO} & K_{DC} & K_D \end{pmatrix} \begin{pmatrix} \Delta P \\ \Delta V \\ \Delta C \end{pmatrix} \quad \text{Forces}$$

Streaming current

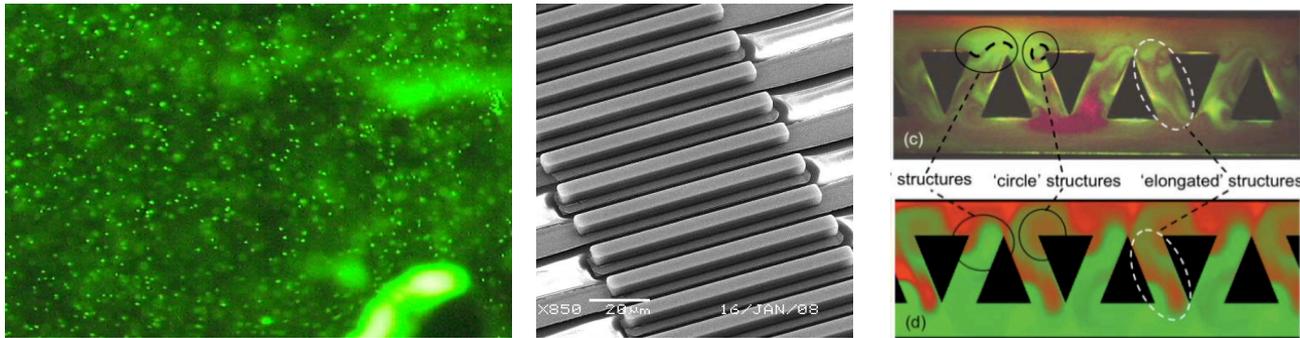
Osmotic flux

Electrodiffusion



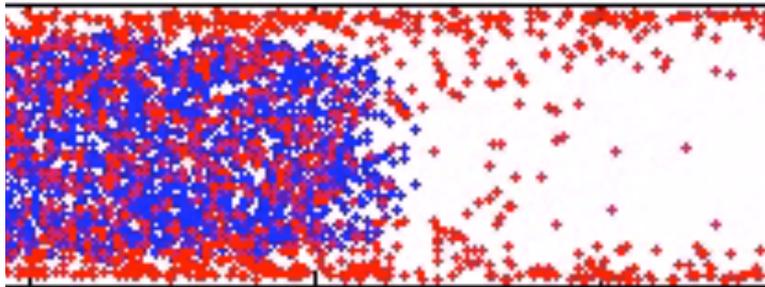
# *Nonlinear* Electrokinetic Phenomena, $K(F)$

## 1. Surface charge $q(V)$ , “induced charge electro-osmosis”

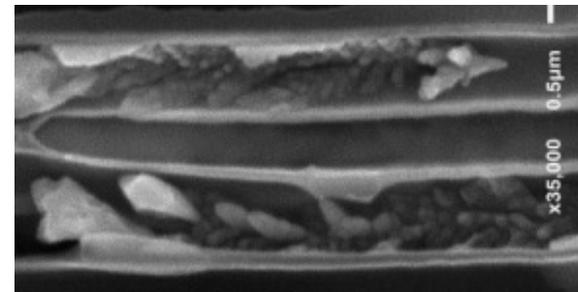


Review: Bazant & Squires, *Current Opinion Colloid Interface Science* (2010). Microfluidic applications.

## 2. Salt concentration $c(V)$ , “shock electrochemistry”

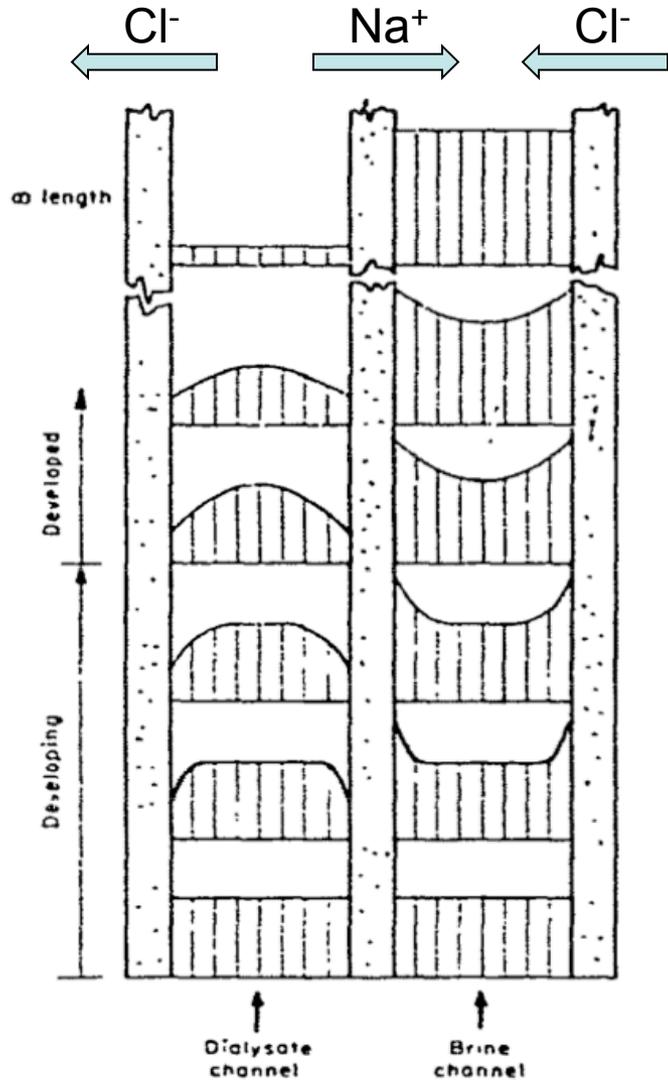


Deionization shock wave in a nanochannel  
Mani & Bazant, *Phys. Rev. E* (2011)

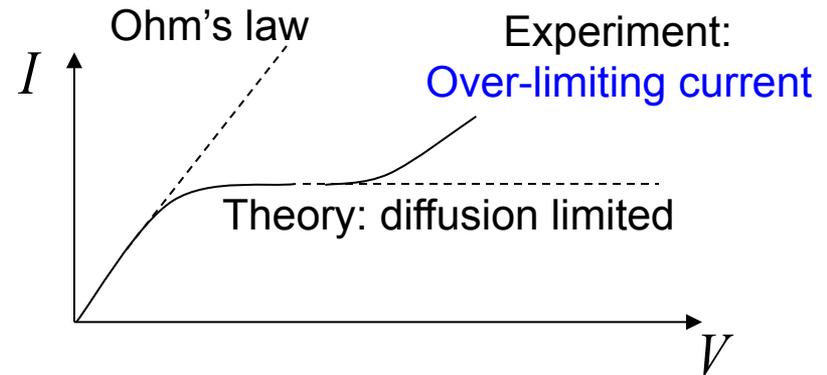
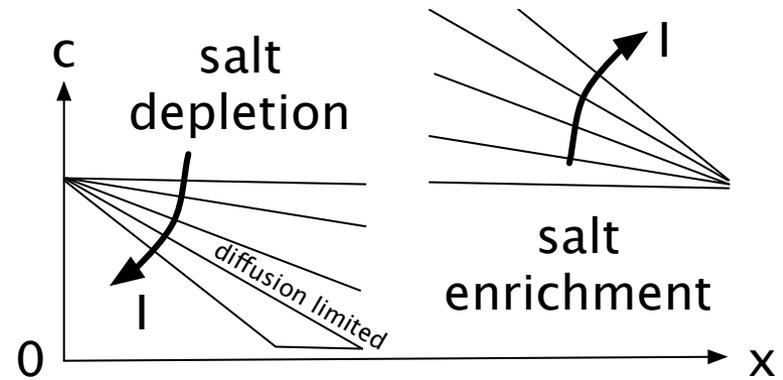
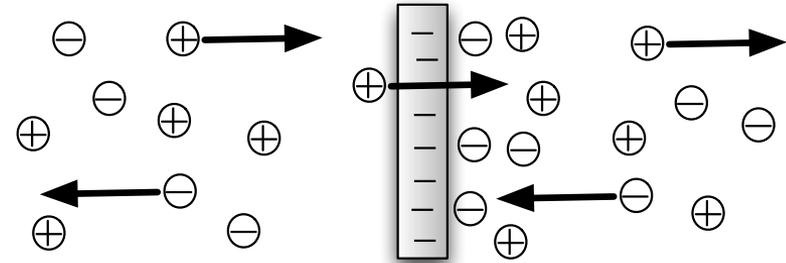


Shock electrodeposition of copper in AAO nanopores  
Han, Khoo, Bai & Bazant, *Sci. Rep.* (2014)

# Motivation: Electrodialysis



Sonin & Probstein (1968)



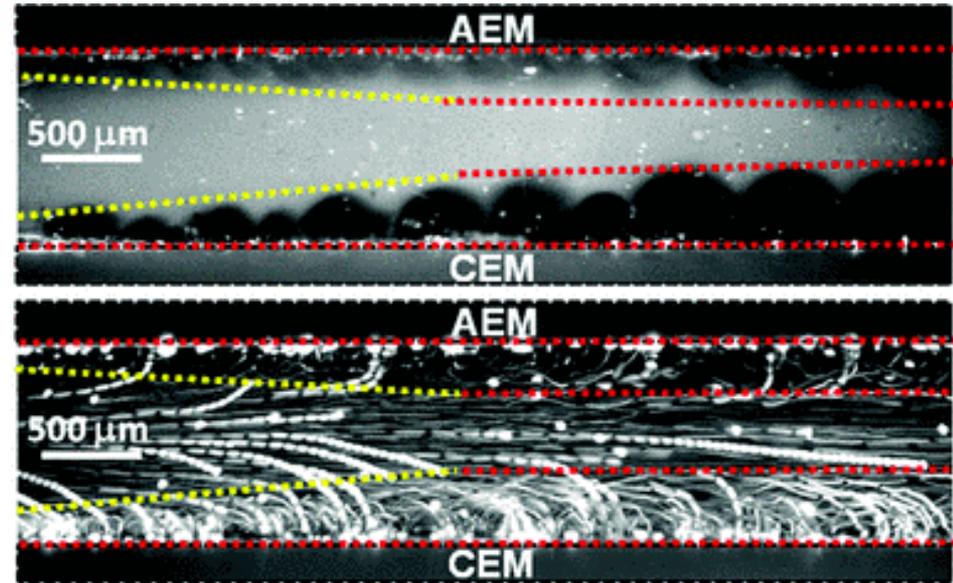
# Over-limiting Current in Bulk Electrolytes

## 1. Electro-osmotic Instability

Idea: I. Rubinstein et al. (1988)

Theory: I. Rubinstein, B. Zaltzman (2000)

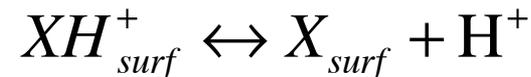
Experiment: S. Rubinstein et al. (2008)  
G. Yossifon, H.-C. Chang (2008)



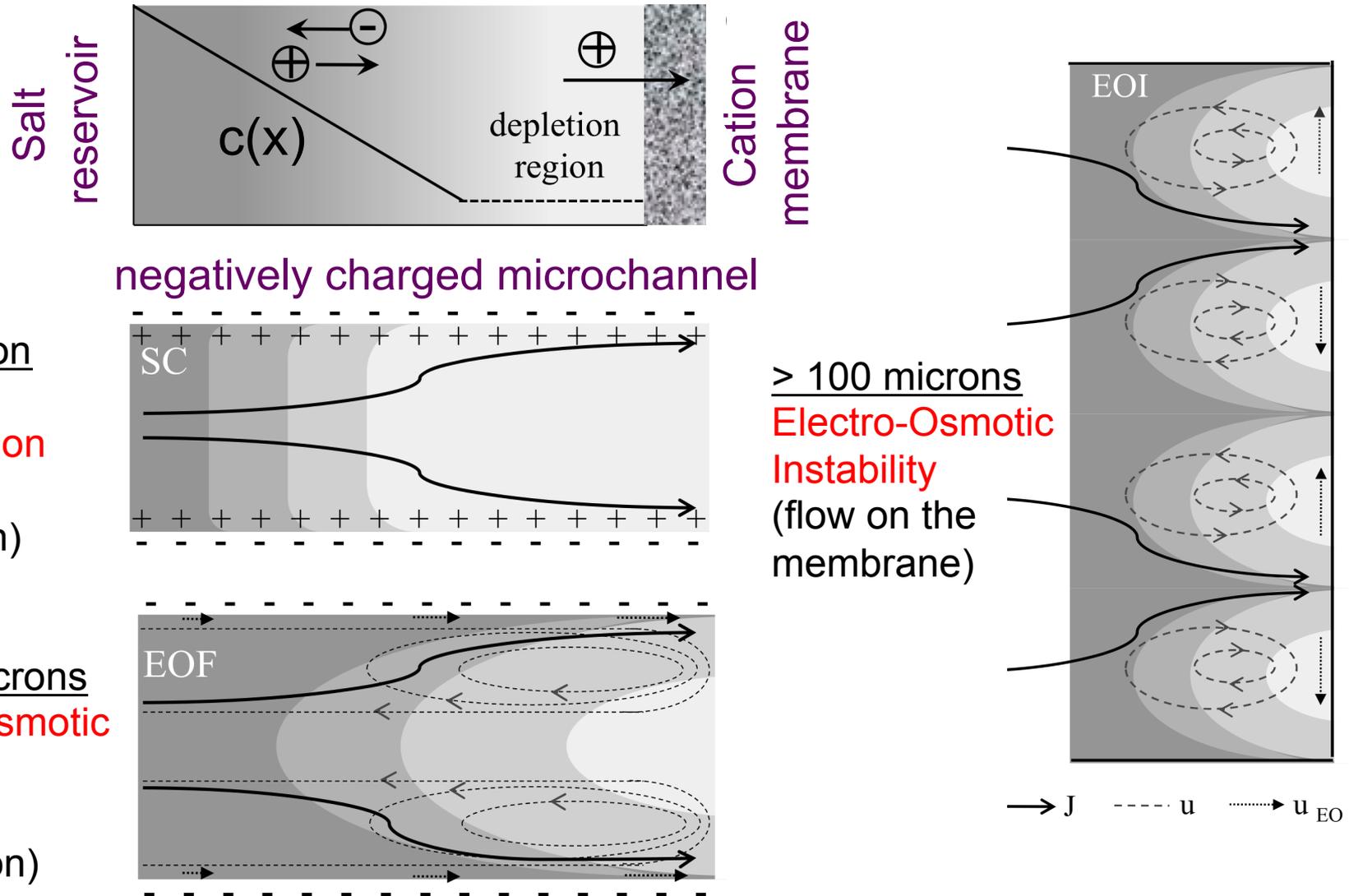
Kwak, Pham, Lim, Han, PRL (2013)

## 2. Current-Induced Membrane Discharge

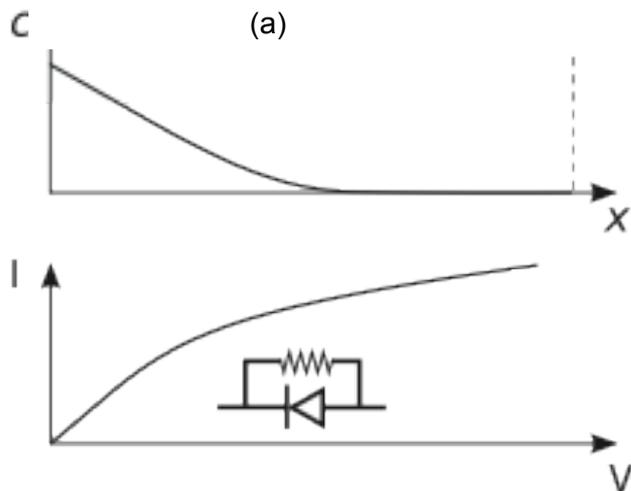
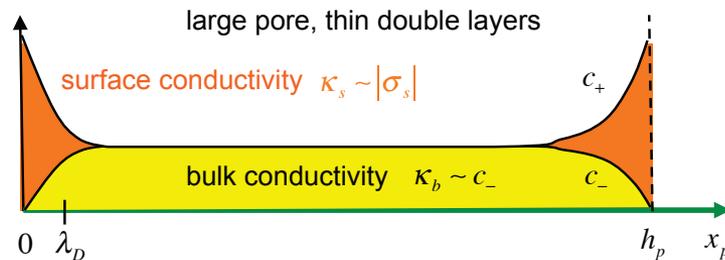
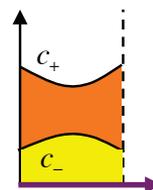
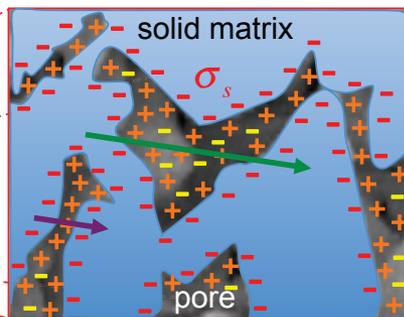
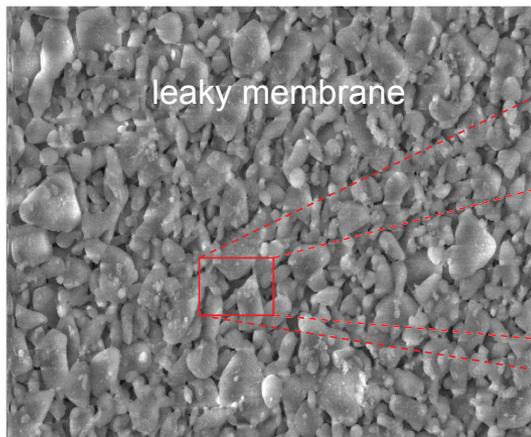
M. Andersen, H. Bruus, A. Mani, M. Soestbergen, PM Biesheuvel, MZB, Phys. Rev. Lett. (2012)



# Over-limiting Current in a Microchannel

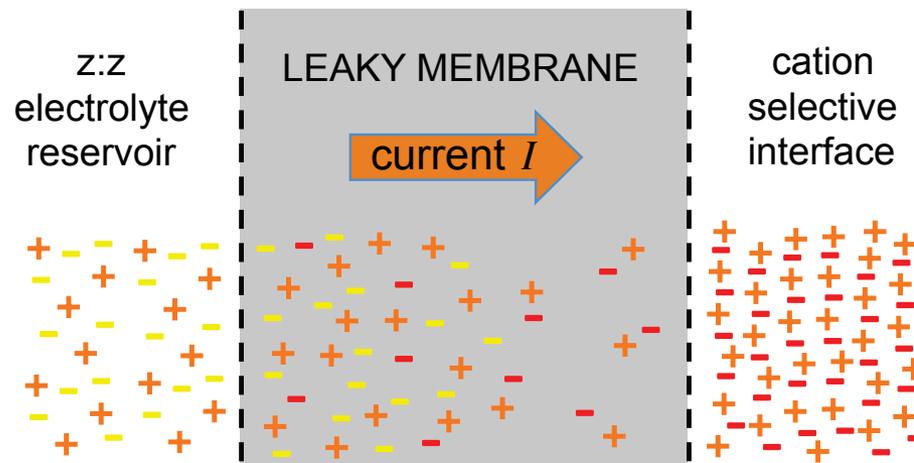


# Over-limiting Current in Porous Media



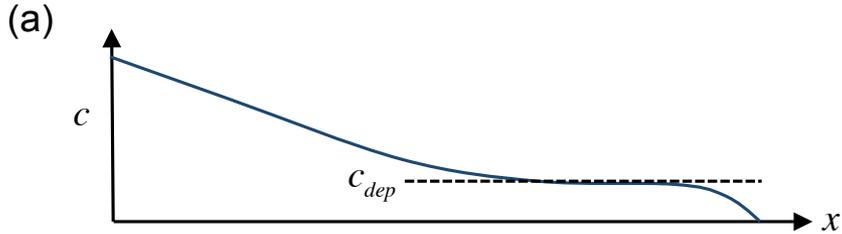
(b)

(c)

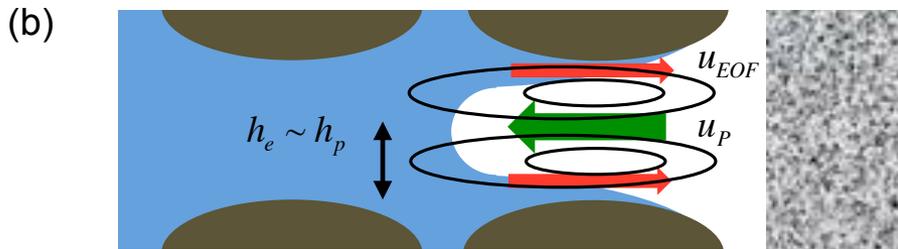


$$I = I_{\text{lim}} \left( 1 - e^{-\tilde{V}} \right) - \sigma_{OLC} \tilde{V}$$

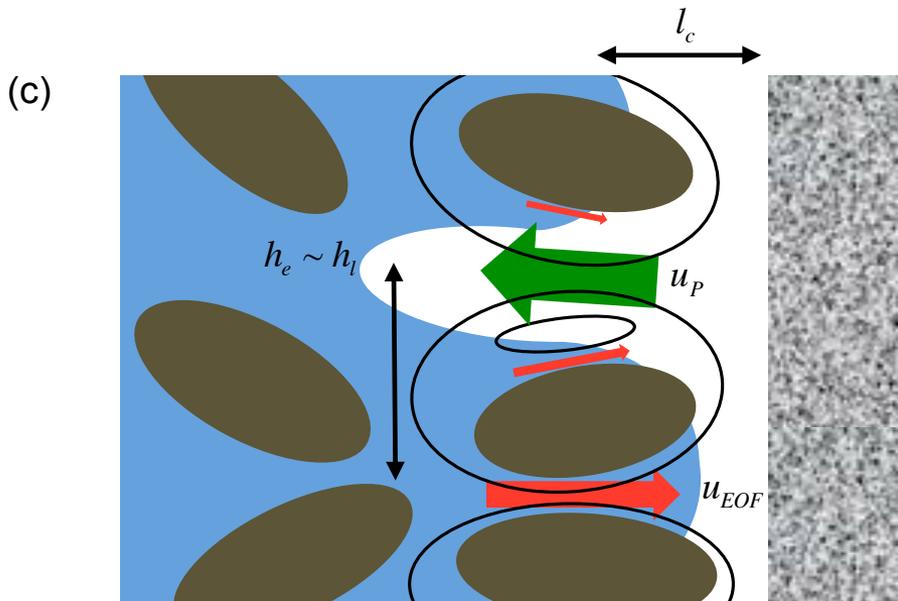
# Mechanisms for Over-limiting Conductance



## 1. Surface conduction



$$\sigma_{SC} \approx \frac{zeDq_s}{k_B T L h_p}$$

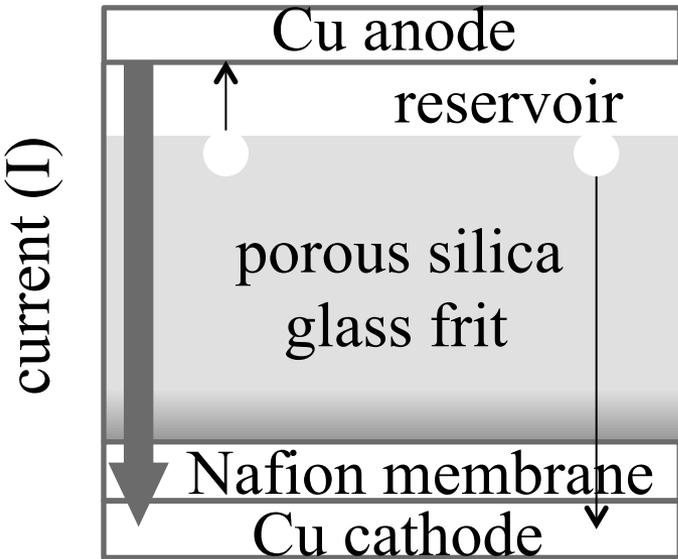


## 2. Surface convection (electro-osmotic flow)

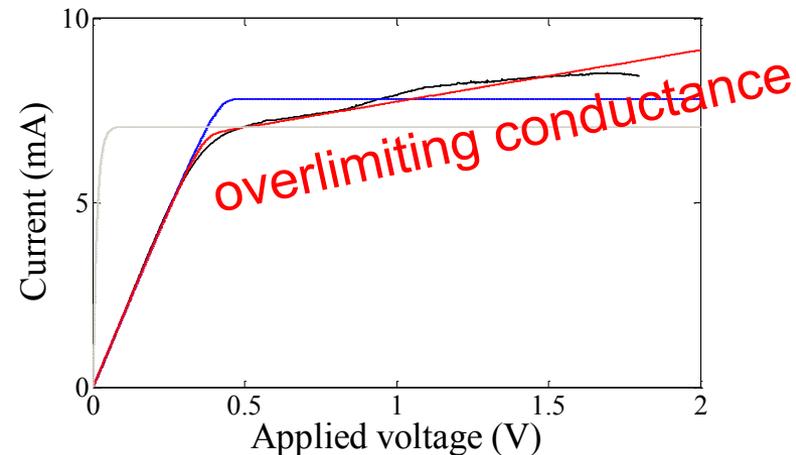
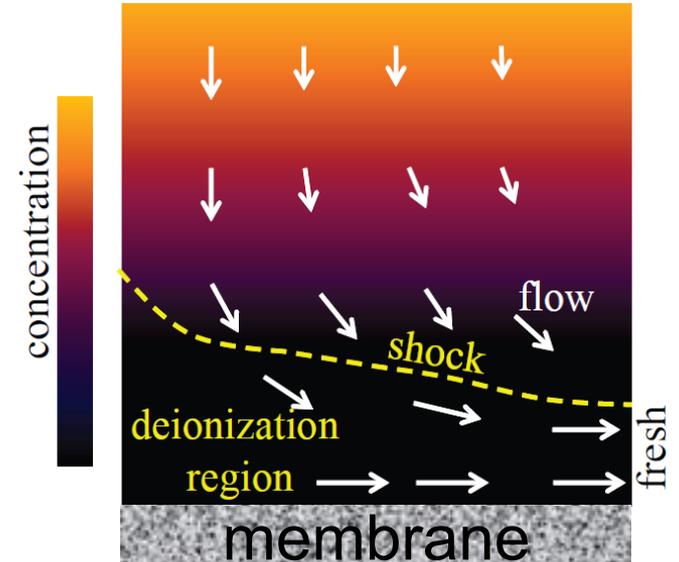
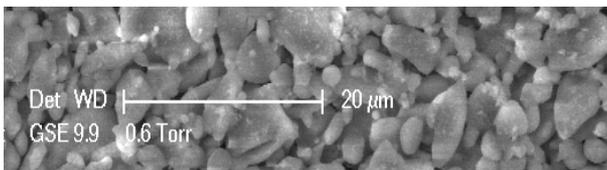
$$\sigma_{EOF} \approx \frac{(ze)^{6/5} (2h_e)^{4/5} \epsilon^{1/5} D^{3/5} q_s^{2/5} c_0^{4/5}}{L^{9/5} (\eta k_B T)^{2/5}}$$

# First Experimental Evidence

Deng, Han, Dydek, Schlumpberger, Mani, MZB, *Langmuir* (2013)

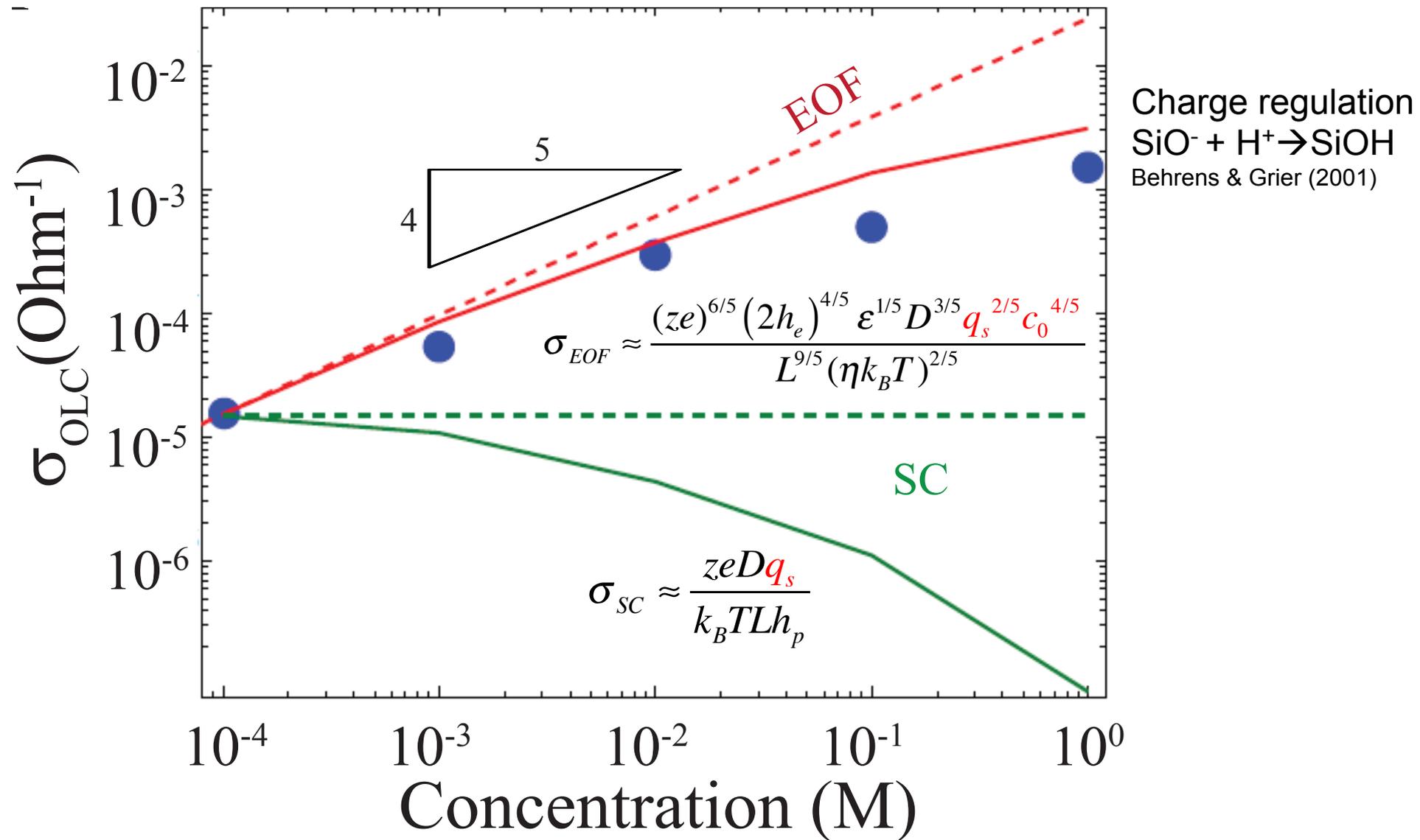


Validate with known chemistry:  
 $\text{Cu}|\text{CuSO}_4|\text{Cu}$   
 $\text{SiOH} \rightarrow \text{SiO}^- + \text{H}^+$

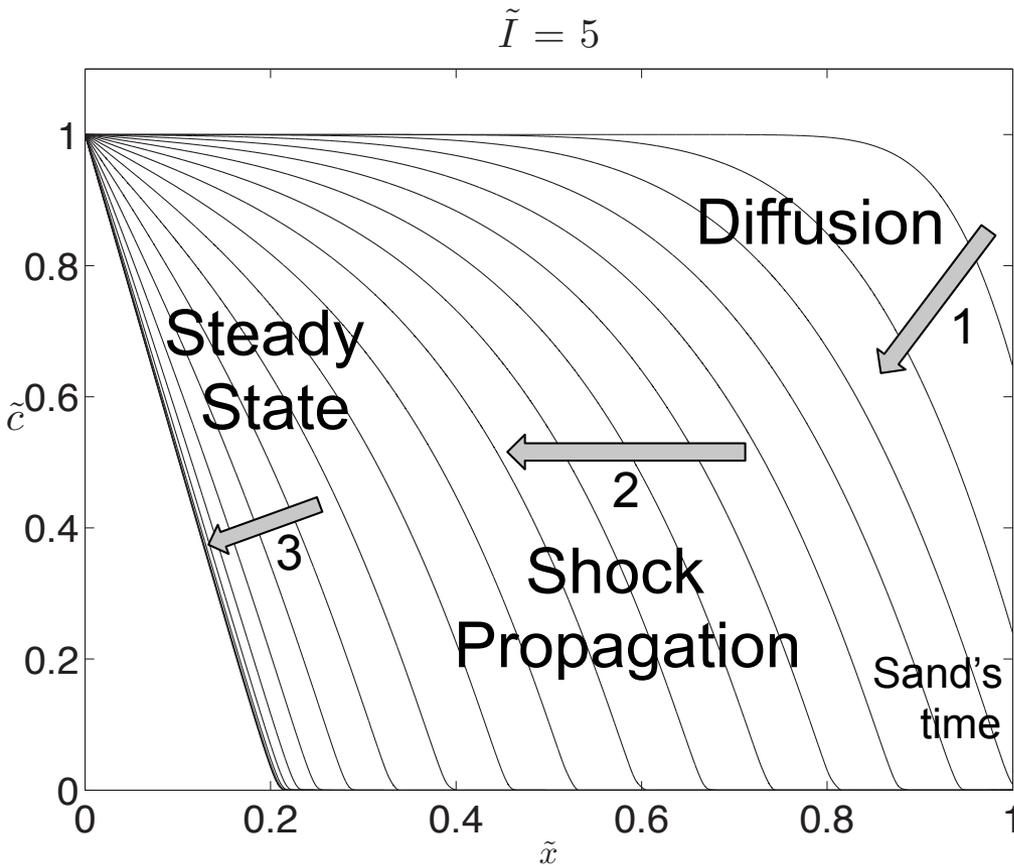


$$I = I_{\text{lim}} \left( 1 - e^{-\tilde{V}} \right) - \sigma_{\text{OLC}} \tilde{V}$$

# Over-limiting Current by Electro-osmotic Flow

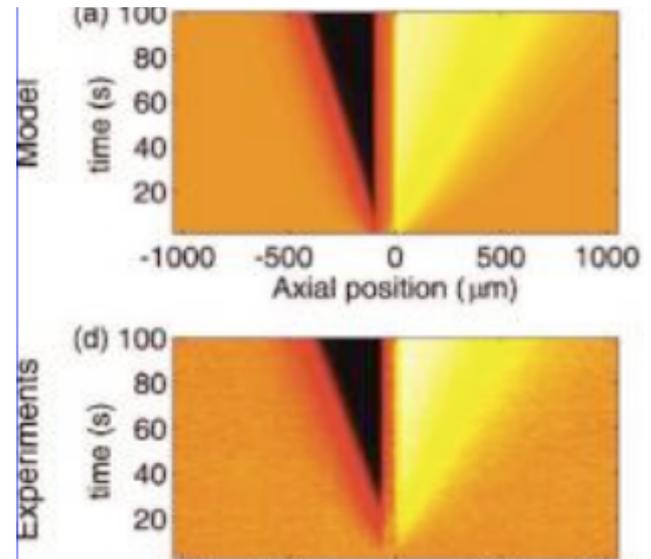


# Transients at Constant Over-limiting Current: Deionization Shock Waves



Theory for porous media, steady over-limiting current in a finite system  
A. Mani & MZB, Phys Rev E (2011); E. V. Dydek & MZB AIChE J (2013)

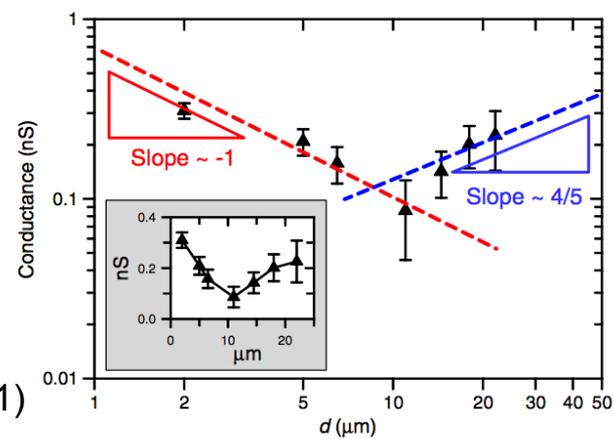
Discovery in Microfluidics:  
A. Mani, T. Zangle, J. Santiago,  
*Langmuir* (2009)



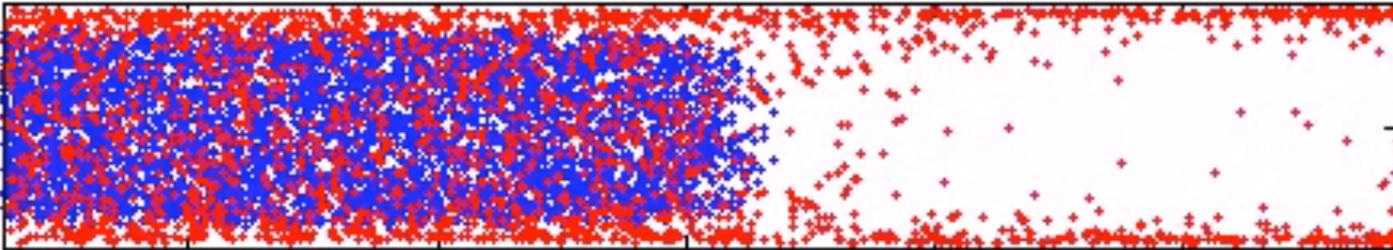
micro | nano | micro  
channel junction

# Two Shock Mechanisms

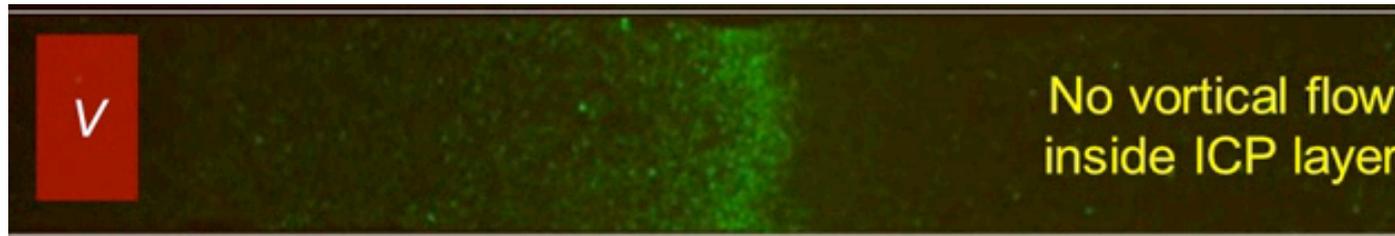
S. Nam, I. Ho, J. Heo, MZB, S. Kim, PRL (2015).



THEORY: **SURFACE CONDUCTION** ( $d=2\text{nm}$ ) Mani & MZB (2011)



EXPERIMENT: **SURFACE CONDUCTION** ( $d=2\mu\text{m}$ )

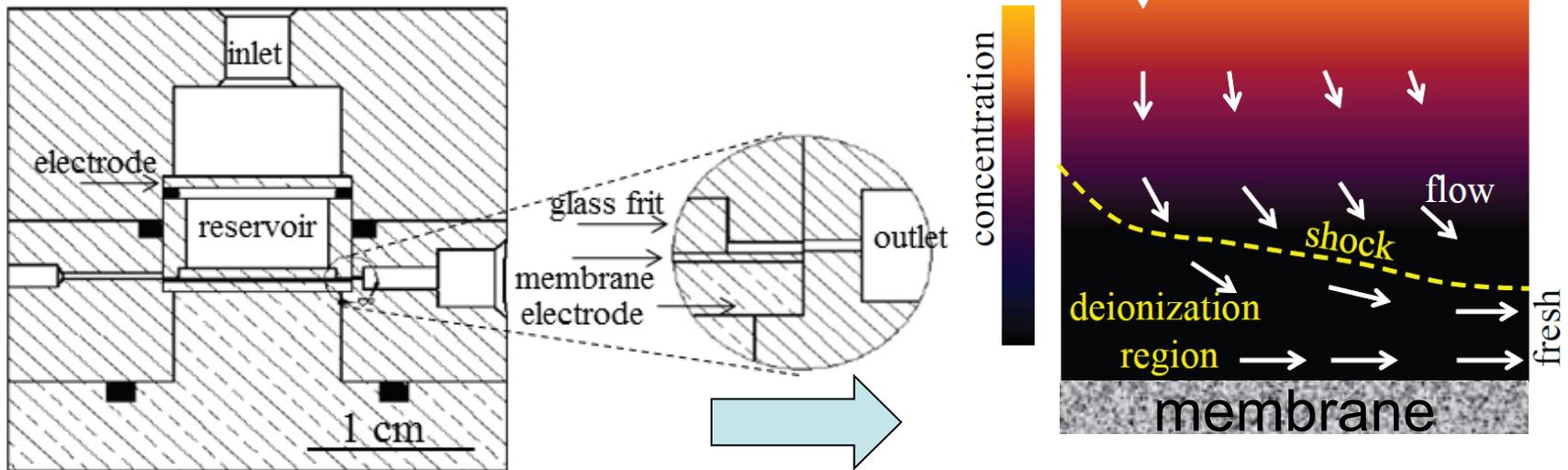


EXPERIMENT: **ELECTRO-OSMOTIC FLOW** ( $d=6.5\mu\text{m}$ )



# Deionization Shocks in Porous Media: Experimental Proof and Application to Water Purification

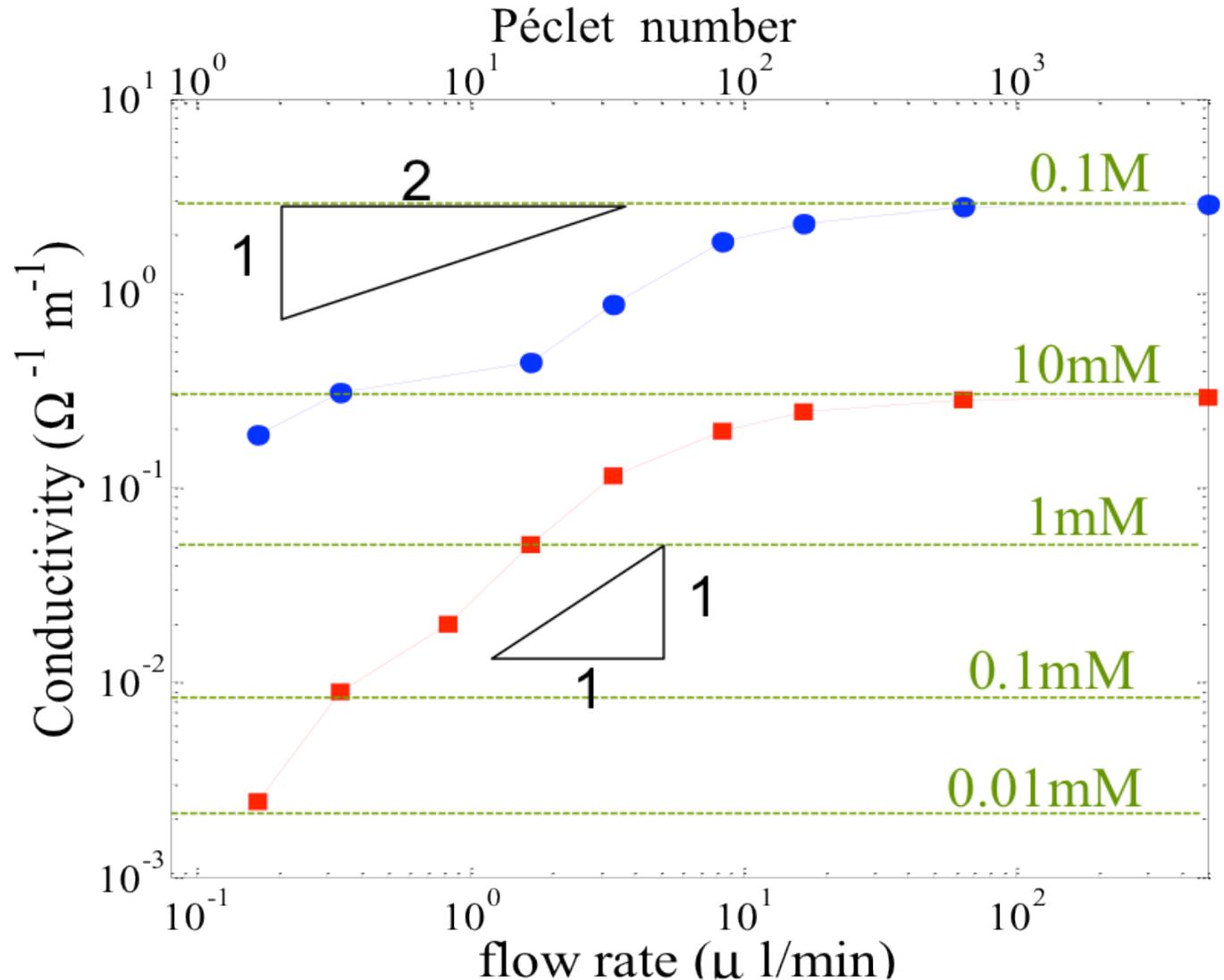
Deng, Han, Dydek, Schlumpberger, Mani, MZB, *Langmuir* (2013)



# Shock Electro-deionization of $\text{CuSO}_4$

Step 1:  
Desalination  
0.1 M in  
5 mM out

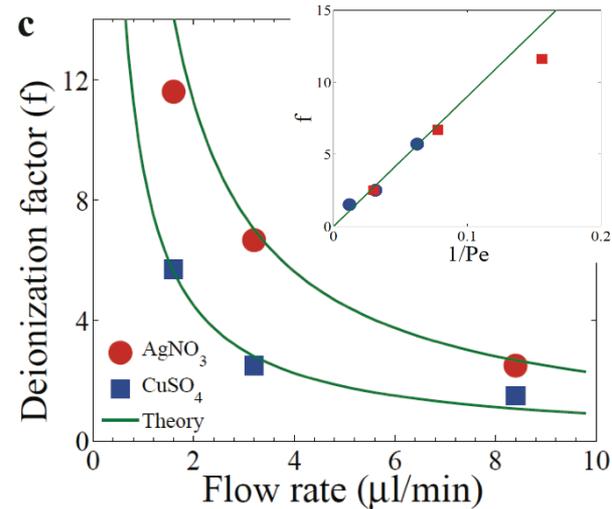
Step 2:  
Deionization  
10 mM in  
10  $\mu\text{M}$  out



# Multifunctionality of Shock ED

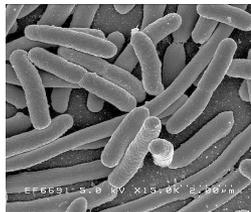
## Separations

Ionic: Toxic multivalent ions  
Molecular: Fluorescein dye  
Colloidal: nanoparticles

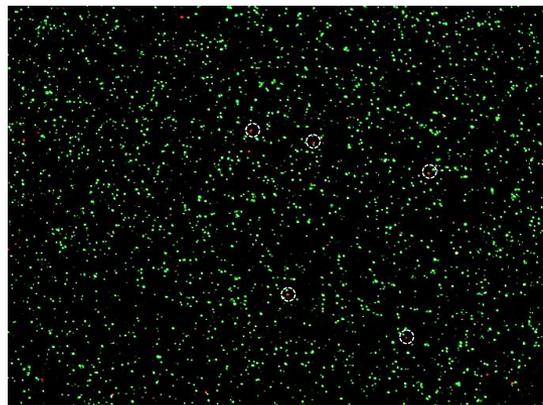


## Disinfection

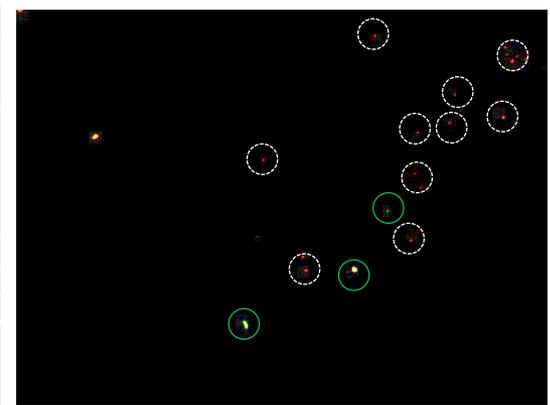
E Coli



Extraction rate: 0.2ul/min;  
Applied voltage: 1.5V.



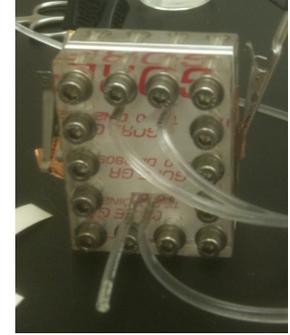
Inlet (10X)



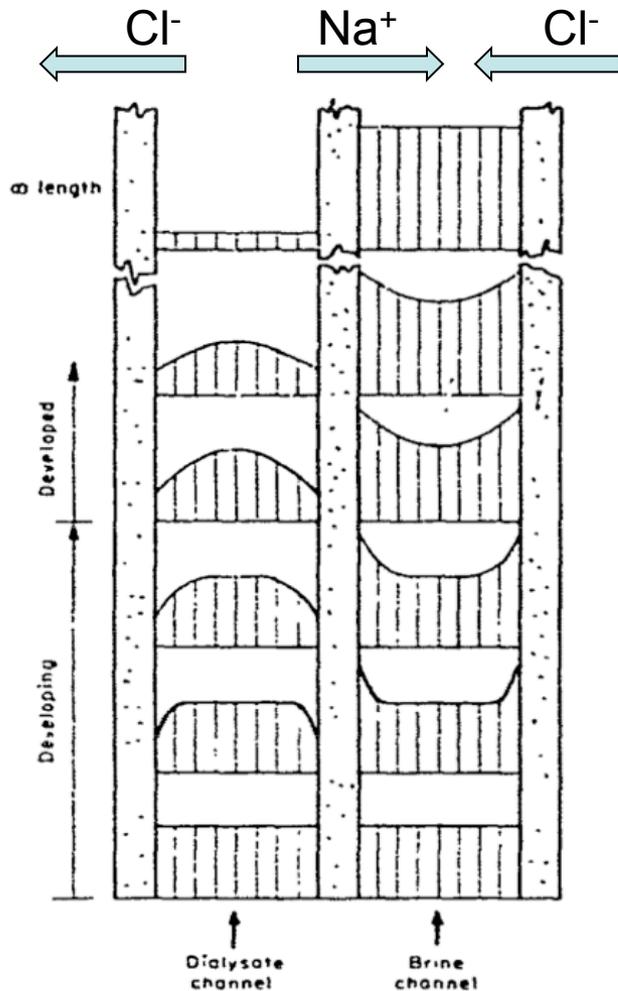
Outlet (4X)

Green: live cells  
Red : dead cells

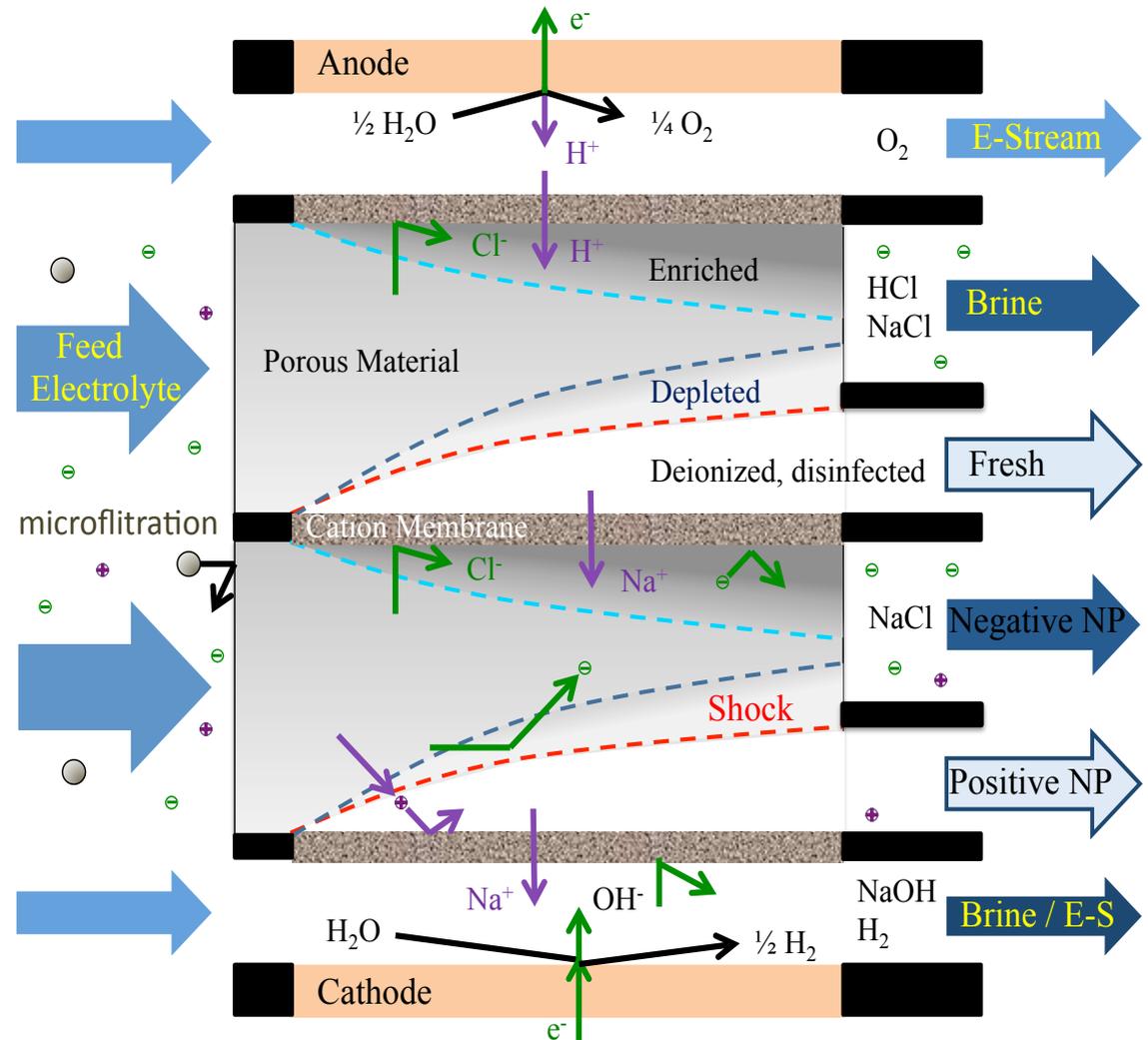
# New Science → Engineering



## Electrodialysis



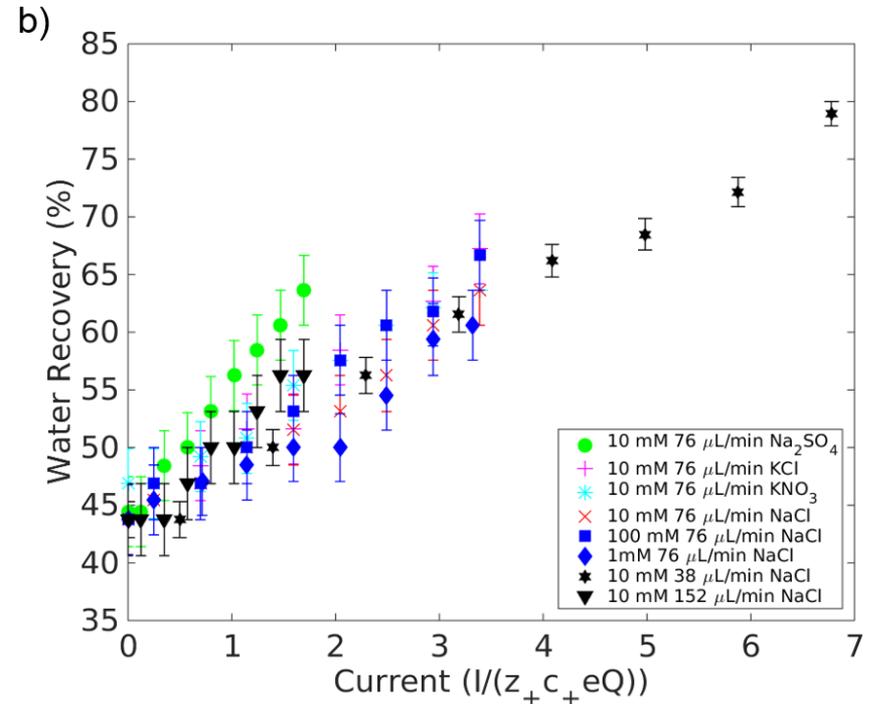
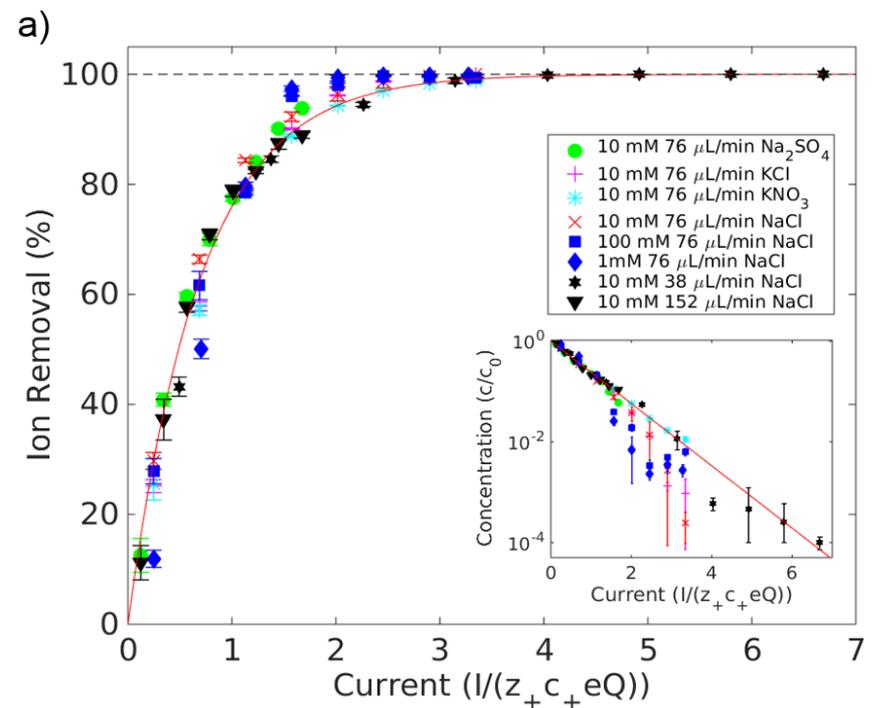
## Shock Electrodialysis



# First Scalable Shock ED System

S. Schlumberger, N. Lu, M. Suss, MZB,  
submitted (2015)

- Up to 99.9% salt removal
- Any electrolyte (NaCl)
- Unexpected result:  
Enhanced water recovery from electro-osmotic flow

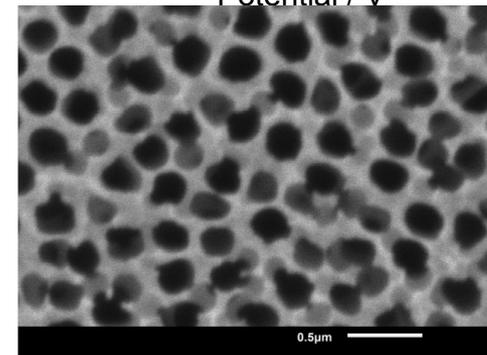
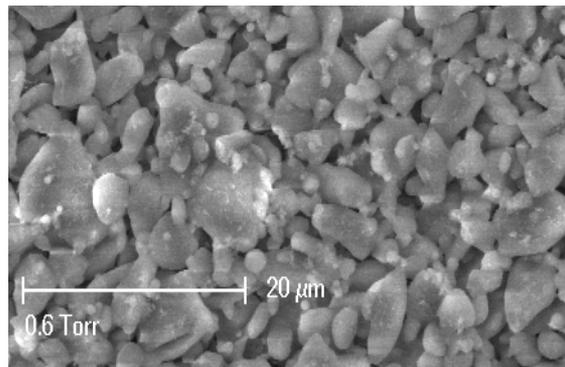
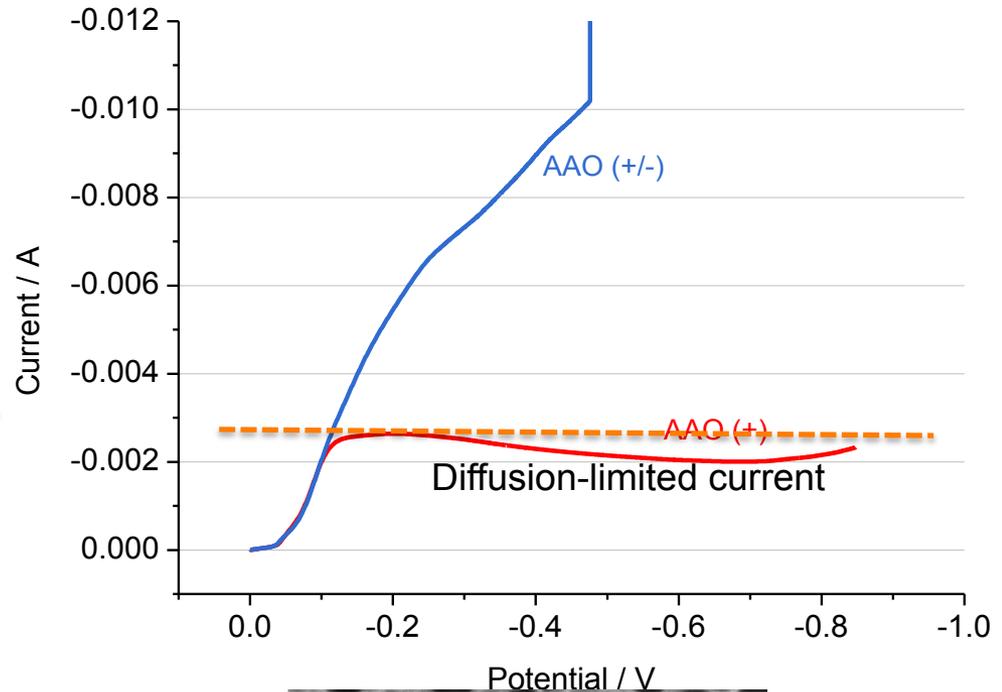
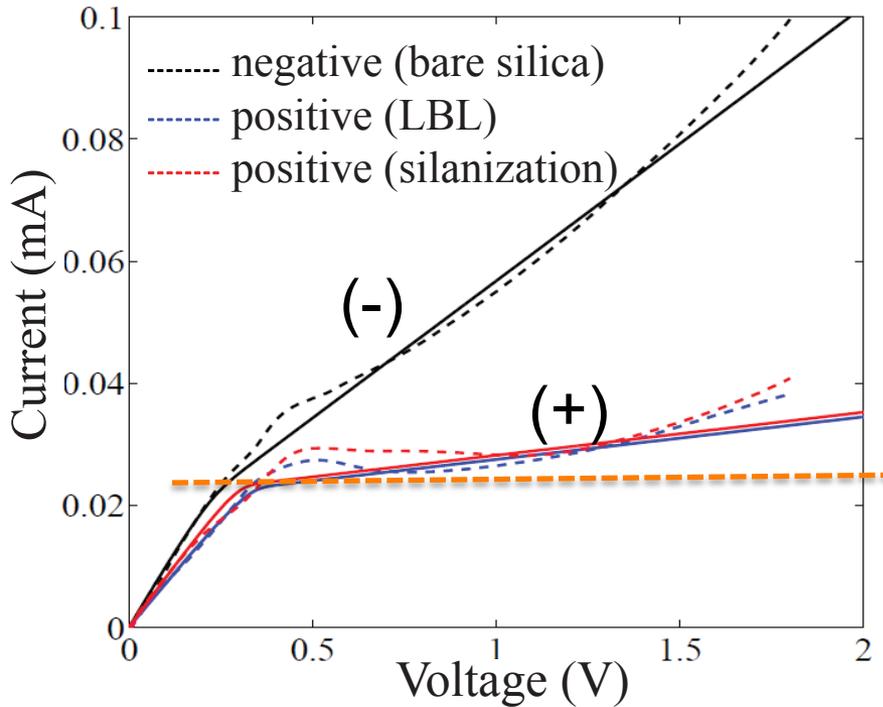




# Two Mechanisms for Over-limiting Current

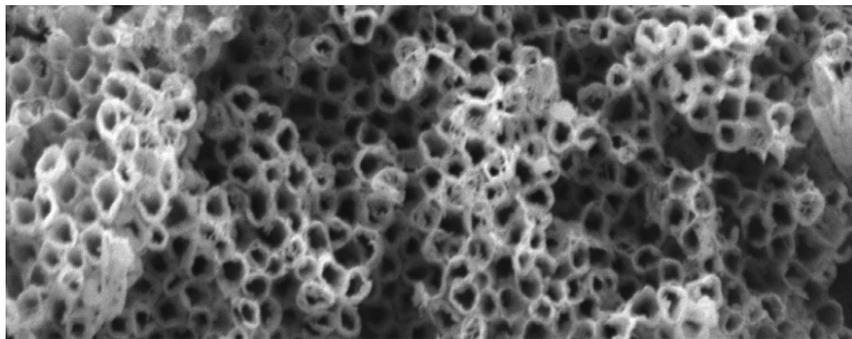
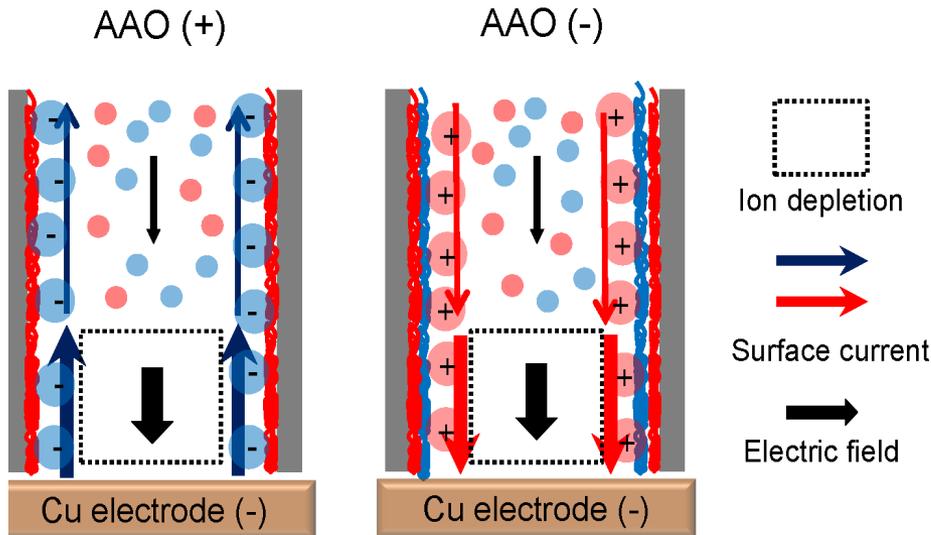
Large, random pores: Electro-osmotic flow

Small, ordered pores: Surface conduction

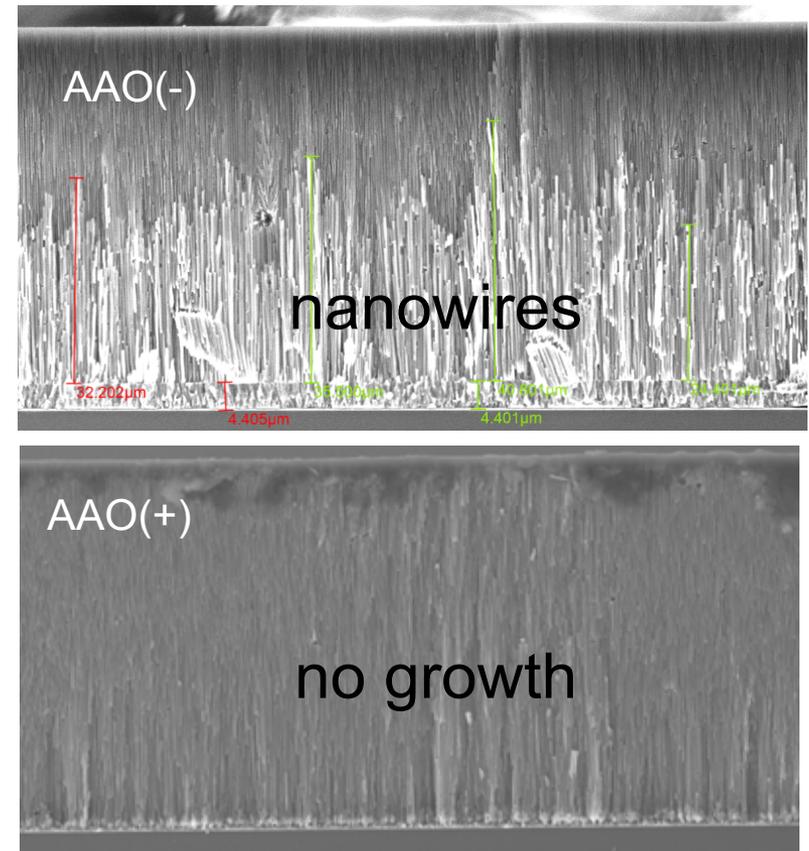


# Shock Electrodeposition in Nanochannels

Ji-Hyung Han, Edwin Khoo, Peng Bai, MZB, *Scientific Reports* (2014)



Proof of surface conduction: Nanotubes

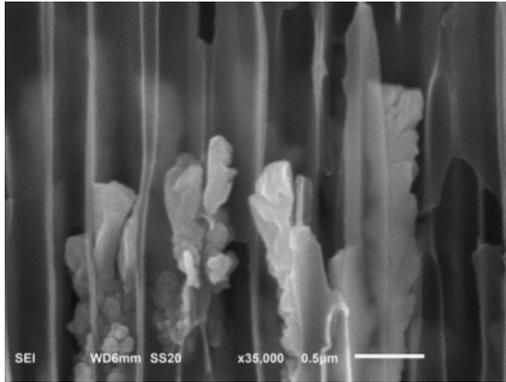


“passively save” high-rate battery separators

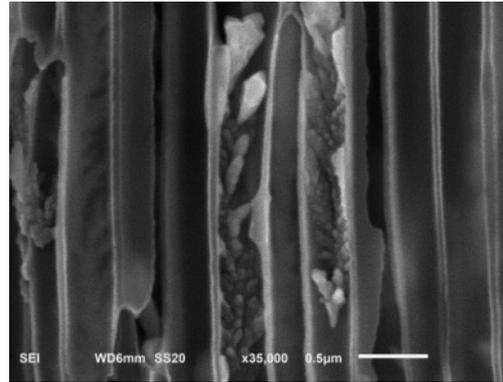
# Morphology Control by Surface Conduction

AAO(-)

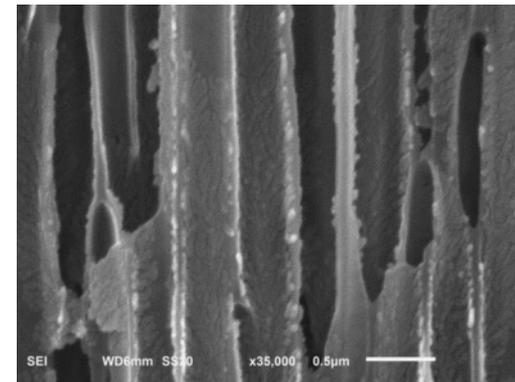
Nanowires



Pore surface dendrites



Nanotubes

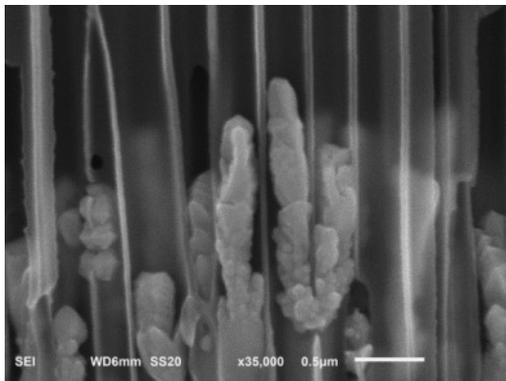


-1.0 V

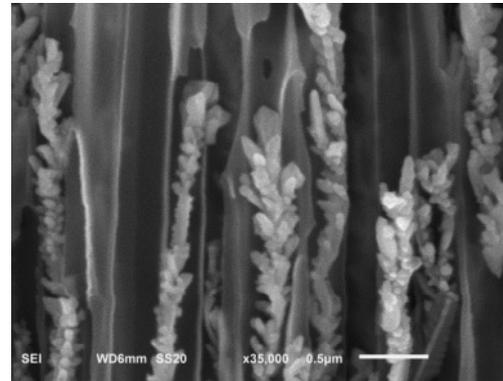
-1.3 V

-1.5 V

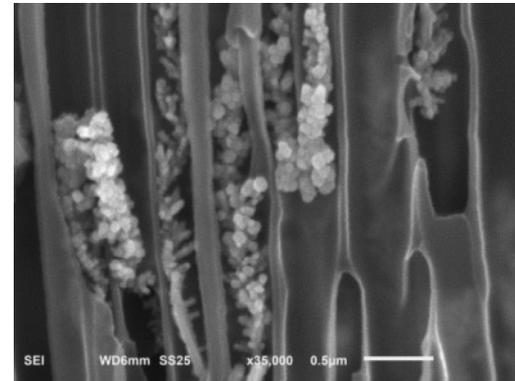
AAO(+)



Nanowires



Pore center dendrites

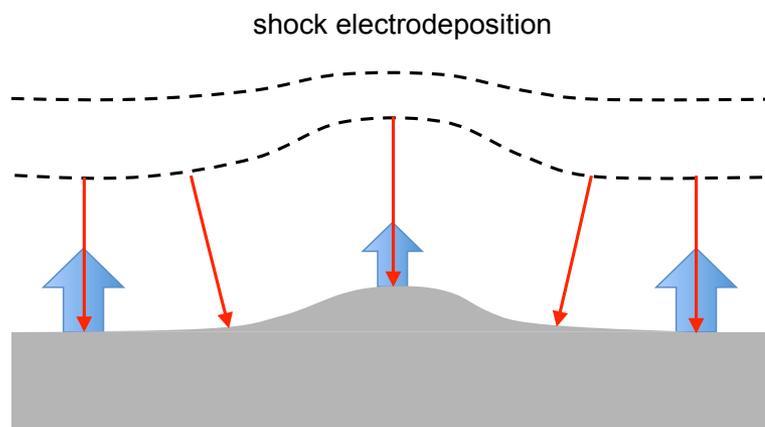
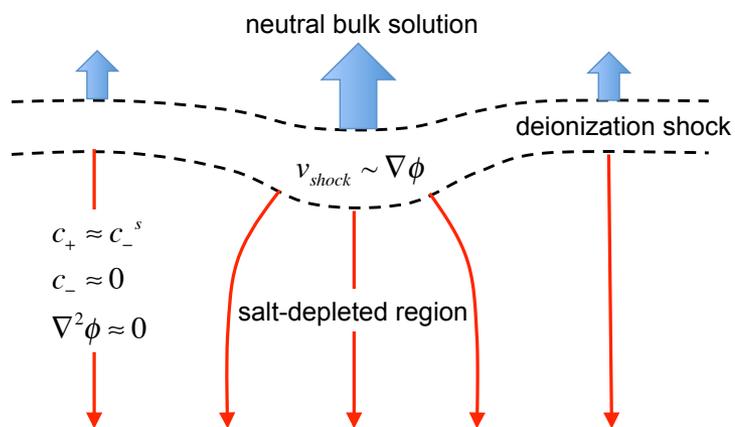
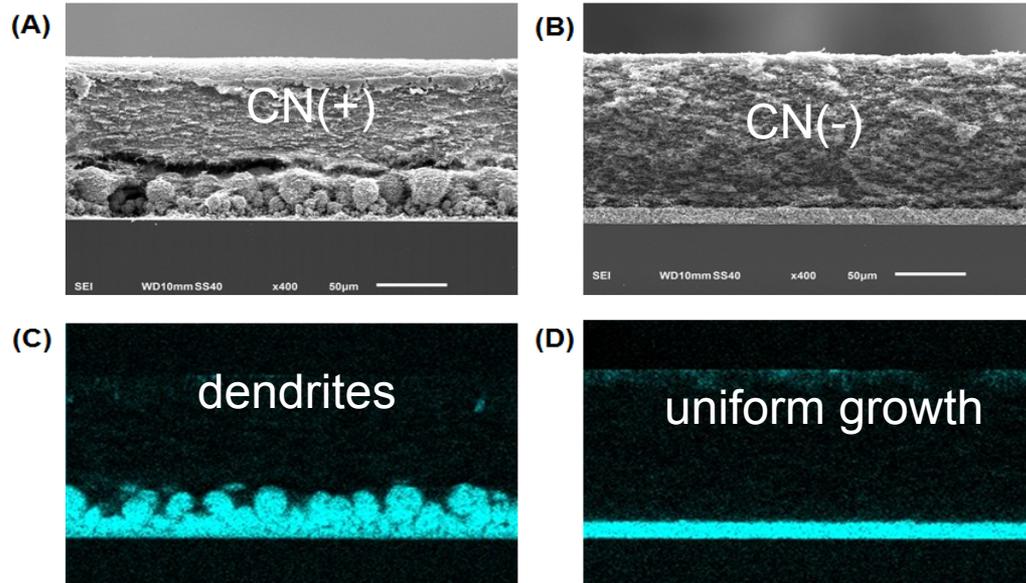
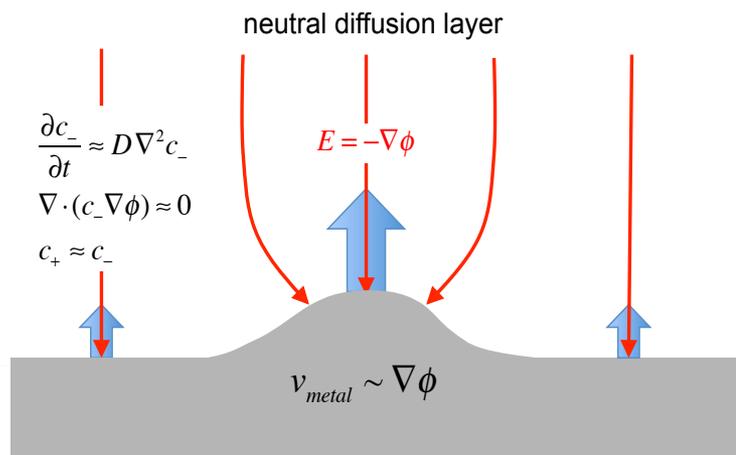


Pore center dendrites

# Dendrite Suppression by Shocks

Ji-Hyung Han & MZB, in preparation

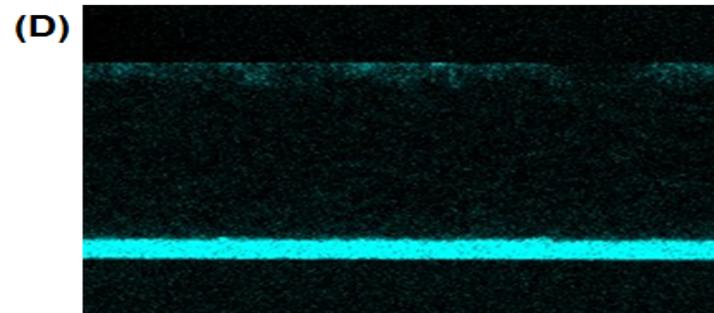
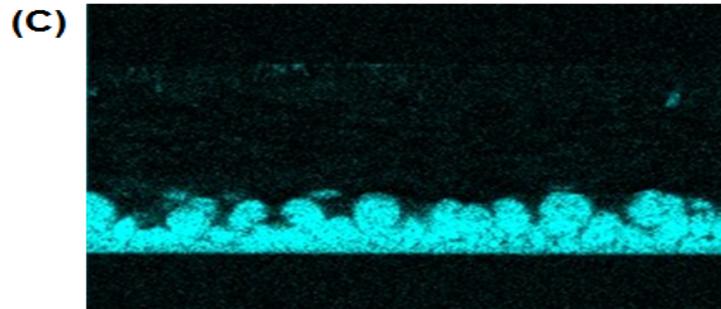
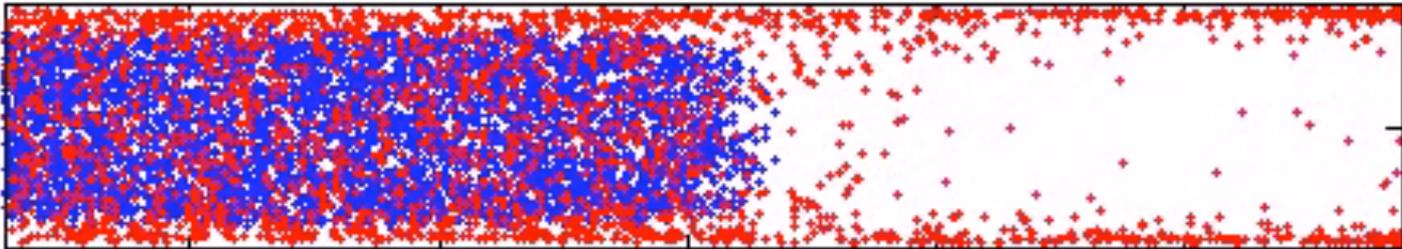
Polyelectrolyte coated cellulose nitride membranes



**Application: Metal Batteries**  
 May explain expts of L. Archer (2013-14)

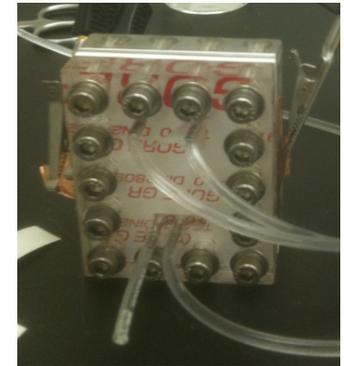
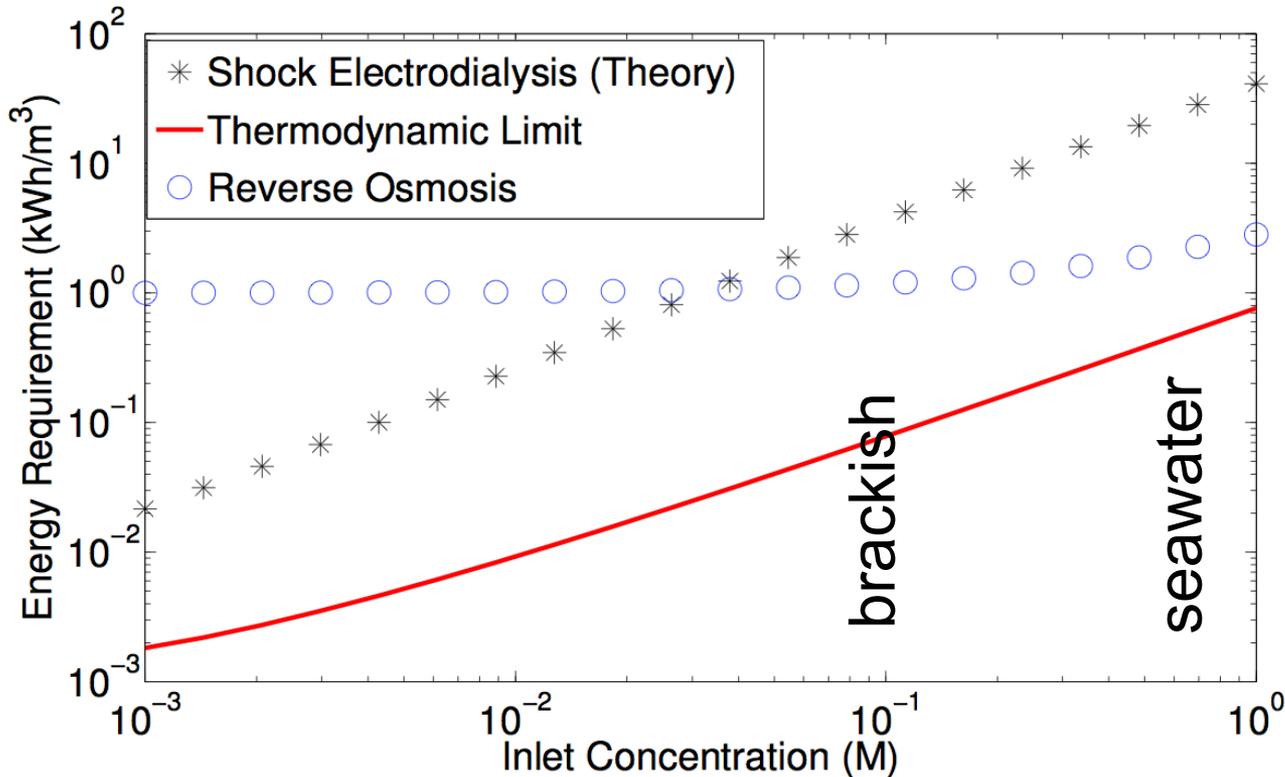
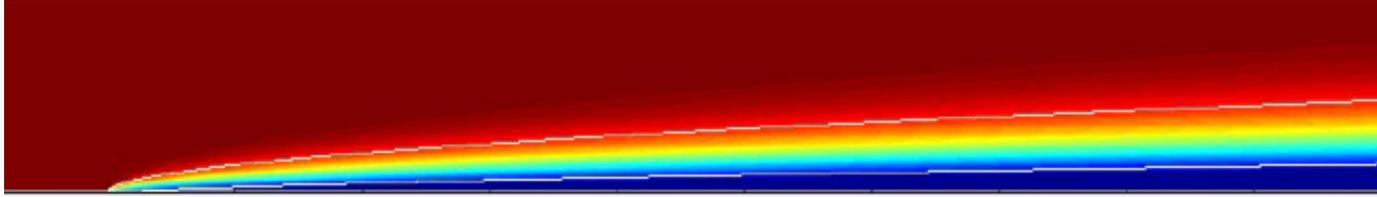
# Conclusion: Shock Electrochemistry

- ~~Electroneutrality~~—Double layers are important.
- Exceed diffusion-limited current in porous media
- Applications: separations, batteries, nanotechnology



**BACKUP SLIDES**

# Toward Cross-flow Scalable Shock ED

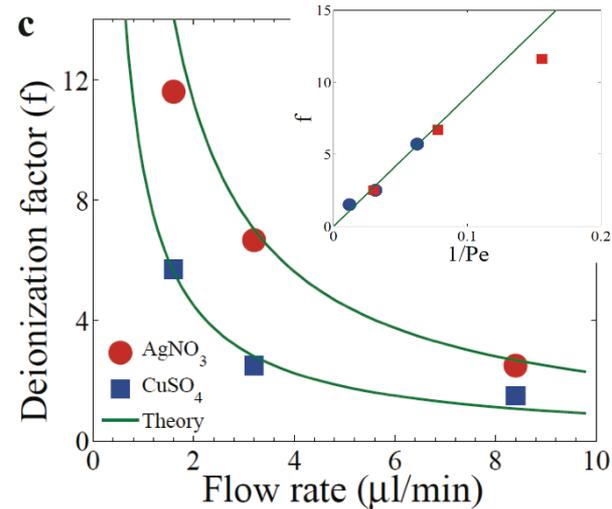


Energy cost to reduce salt by 80%

# Multifunctionality of Shock ED

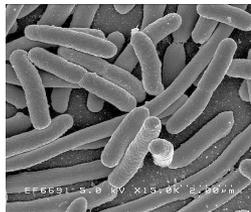
## Separations

Ionic: Toxic multivalent ions  
Molecular: Fluorescein dye  
Colloidal: nanoparticles

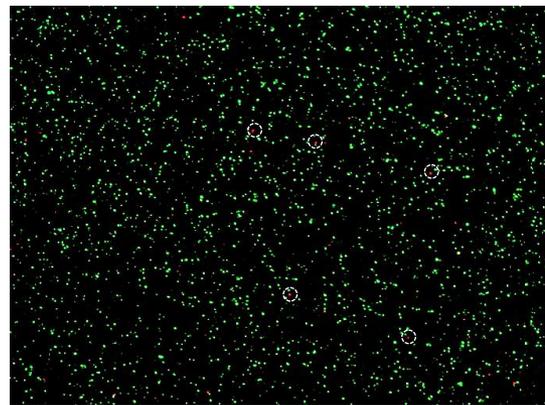


## Disinfection

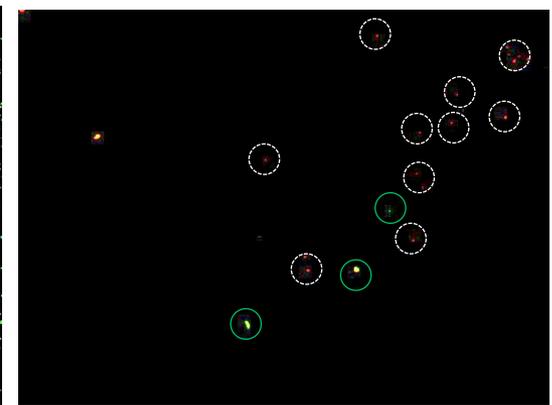
E Coli



Extraction rate: 0.2ul/min;  
Applied voltage: 1.5V.



Inlet (10X)



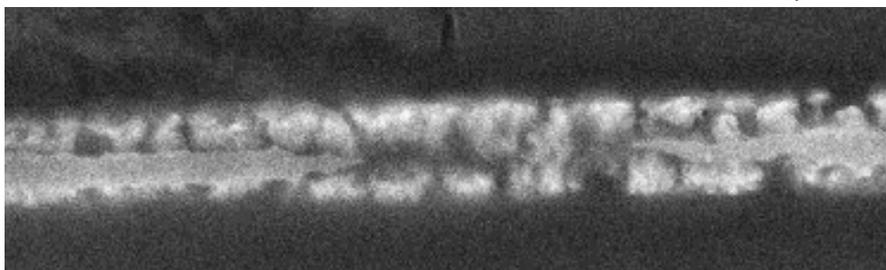
Outlet (4X)

Green: live cells  
Red : dead cells

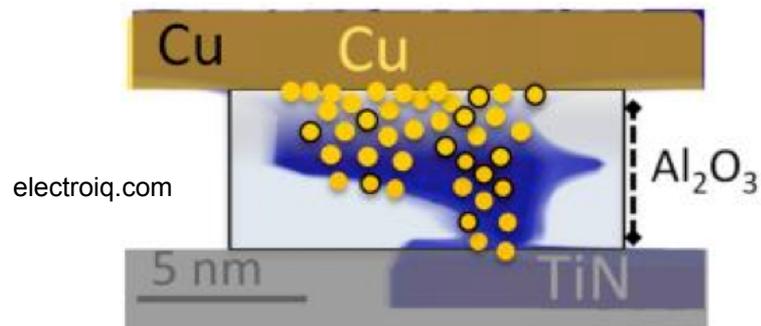
# Applications

## Integrated circuits (IBM)

wikipedia



10-100nm Cu interconnects – suppress dendrites

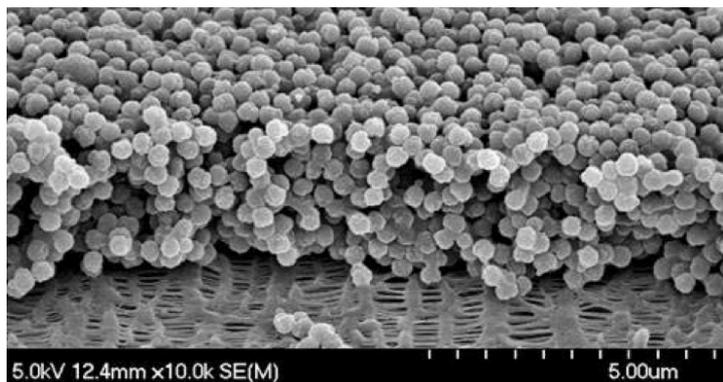


electroiq.com

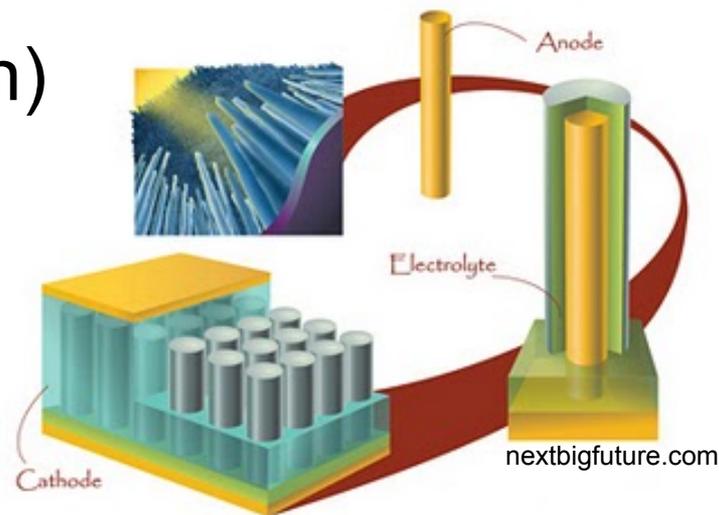
CB-RAM – control dendrites

## Battery separators (Saint Gobain)

Kaneda, ECS abstracts 2012



Alumina powders – suppress dendrites

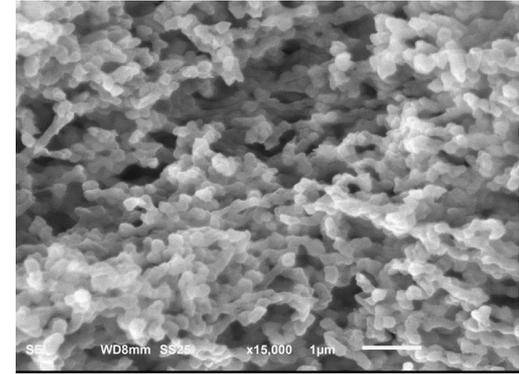
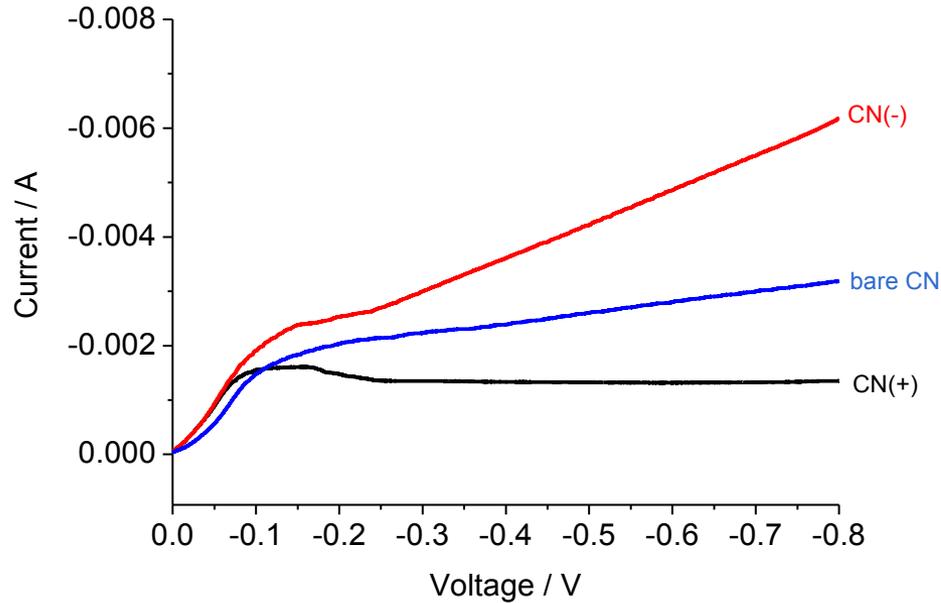


3D Battery fabrication – control dendrites

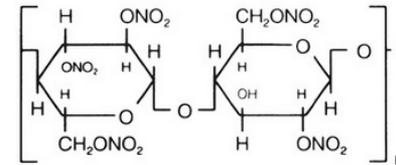
# Shock Electrodeposition in Random Nanopores

Ji-Hyung Han

10 mM CuSO<sub>4</sub>\_1mV/s



Cellulose nitrate (CN) membrane



Intrinsic surface charge is negative

CN(-) Very uniform growth  
CN(+) No metal penetration

Next: Li-ion battery separators

