## 9.520 in 2015 Statistical Learning Theory and Applications

#### **Class Times:**

Monday and Wednesday 1pm-2:30pm

Units: 3-0-9 H,G

#### Location:

46-5193

Instructors: Carlo Ciliberto, Georgios Evangelopoulos, Maximilian Nickel, Ben Deen, Hongyi Zhang, Steve Voinea, Owen Lewis, T. Poggio, J. Posssoo

T. Poggio, L. Rosasco

Web site: http://www.mit.edu/~9.520/

**Office Hours:** Friday 2-3 pm in 46-5156, CBCL lounge (by appointment)

Email Contact : 9.520@mit.edu



#### Class

#### http://www.mit.edu/~9.520/

Class 3 (Wed, Sept 16): Mathcamps

• Functional analysis (~45mins)

### Linear Algebra

Basic notion and definitions: matrix and vectors norms, positive, symmetric, invertible matrices, linear systems, condition number.

#### & Multivariate Calculus:

Extremal problems, differential, gradient.

#### **Functional Analysis:**

Linear and Euclidean spaces scalar product, orthogonality orthonormal bases, norms and semi-norms, Cauchy sequence and complete spaces Hilbert spaces, function spaces and linear functional, Riesz representation theorem, convex functions, functional calculus.

• Probability (~45mins)

#### Probability Theory:

Random Variables (and related concepts), Law of Large Numbers, Probabilistic Convergence, Concentration Inequalities.

## 9.520: Statistical Learning Theory and Applications, Fall 2015

- Course focuses on regularization techniques, that provide a theoretical foundation to high- dimensional supervised learning.
- Support Vector Machines, manifold learning, sparsity, batch and online supervised learning, feature selection, structured prediction and multitask learning.
- Optimization theory critical for machine learning (first order methods, proximal/splitting techniques).
- In the final part focus on deep theory: deep learning networks, theory of invariance, extension of convolutional layers, learning invariance, connection of DCLNs with hierarchical splines, possibility of theory.

The goal of this class is to provide the theoretical knowledge and the basic intuitions needed to use and develop effective machine learning solutions to a variety of problems.

#### **Class**

#### http://www.mit.edu/~9.520/

Rules of the game:

- problem sets (2)
- final project: you have to give us title + abstract before November 25th
- participation
- Grading is based on Psets (27.5%+27.5%) + Final Project (32.5%) + Participation (12.5%)

Slides on the Web site (most classes on blackboard) Staff mailing list is 9.520@mit.edu Student list will be 9.520students@mit.edu <u>Please fill form!</u>

send email to us if you want to be added to mailing list

Friday 2-3 pm in 46-5156, CBCL lounge (by appointment) Problem Set 1: 05 Oct (Class 8) Problem Set 2: 09 Nov (Class 18) Final Project Decision: 25 Nov (Class 22)

## **Final Project**

The final project can be

- a Wikipedia entry or
- problems for chapters of the textbook of the class or
- contributions to GURLs (GURLS: a Toolbox for Regularized Least Squares Learning) or
- a research project.

For the Wikipedia article we suggest to post 1-2 pages (short) using Wikipedia standard format (of course).

For the research project (either Application or Theory) you should use the template on the Web site.

## Project: posting/editing article on Wikipedia (past examples below)

• Kernel methods for vector output : http://en.wikipedia.org/wiki/ Kernel\_methods\_for\_vector\_output

- Principal component regression : http://en.wikipedia.org/wiki/Principal\_component\_regression
- Reproducing kernel Hilbert space : http://en.wikipedia.org/wiki/ Reproducing\_kernel\_Hilbert\_space
- Proximal gradient methods for learning :
  http://op.wilkipedie.org/wilki/Drowingel.gradient.metho
- http://en.wikipedia.org/wiki/Proximal\_gradient\_methods\_for\_learning
- Regularization by spectral filtering : https://en.wikipedia.org/wiki/ Regularization\_by\_spectral\_filtering
- Online

learning and stochastic gradient descent : http://en.wikipedia.org/wiki/Online\_machine\_learning

- Kernel embedding of distributions : http://en.wikipedia.org/wiki/ Kernel\_embedding\_of\_distributions
- Vapnik–Chervonenkis theory : https://en.wikipedia.org/wiki/VC\_theory
- Deep learning : http://en.wikipedia.org/wiki/Deep\_learning
- Early stopping and regularization : http://en.wikipedia.org/wiki/Early\_stopping
- Statistical learning theory : http://en.wikipedia.org/wiki/Statistical\_learning\_theory
- Representer theorem : http://en.wikipedia.org/wiki/Representer\_theorem
- Regularization perspectives on support vector machines :

http://en.wikipedia.org/wiki/Regularization\_perspectives\_on\_support\_vector\_machines

• Semisupervised

learning : http://en.wikipedia.org/wiki/Semi\_supervised\_learning

- Devenion interpretation of regularization :

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- Regularization perspectives on support vector machines :

http://en.wikipedia.org/wiki/Regularization\_perspectives\_on\_support\_vector\_machines

Semisupervised

learning : http://en.wikipedia.org/wiki/Semi\_supervised\_learning

• Bayesian interpretation of regularization :

http://en.wikipedia.org/wiki/Bayesian\_interpretation\_of\_regularization

- Regularized least squares (RLS) : http://en.wikipedia.org/wiki/User:Bdeen/sandbox
- Occam Learning (PAC Learning) : https://en.wikipedia.org/wiki/Occam\_learning
- Multiple Kernel Learning: https://en.wikipedia.org/wiki/Multiple\_kernel\_learning
- Loss Function for Classification : https://en.wikipedia.org/wiki/Loss\_functions\_for\_classification
- Online Machine Learning : https://en.wikipedia.org/wiki/Online\_machine\_learning
- Sparse PCA : https://en.wikipedia.org/wiki/Sparse\_PCA
- Distribution Learning Theory : https://en.wikipedia.org/wiki/Distribution\_learning\_theory
- Sample Complexity : https://en.wikipedia.org/wiki/Sample\_complexity
- Hyper Basis Function Network : https://en.wikipedia.org/wiki/Hyper\_basis\_function\_network
- Diffusion Map : https://en.wikipedia.org/wiki/Diffusion\_map
- Matrix Regularization: https://en.wikipedia.org/wiki/Matrix\_regularization
- Mtheory

(Learning Framework) : https://en.wikipedia.org/wiki/MTheory\_( learning\_framework)

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- Feature Learning : https://en.wikipedia.org/wiki/Feature\_learning Done but not submitted in (public) Wikipedia
- Lasso Regression : https://en.wikipedia.org/wiki/User:Rezamohammadighazi/sandbox
- Unsupervised Learning: Dim. Red. : https://en.wikipedia.org/wiki/User:Iloverobotics/sandbox
- Regularized Least Squares : https://en.wikipedia.org/wiki/User:Yakirrr
- Error Tolerance (PAC Learning): https://en.wikipedia.org/wiki/User:Alex\_e\_e\_alex/sandbox

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- Desnity Estimation : https://en.wikipedia.org/wiki/User:Linjing1119/sandbox
- Matrix Completion : https://en.wikipedia.org/wiki/User:Milanambiar/sandbox
- Multiple Instance Learning : we have Wiki markup

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• Uniform Stability and Generalization in Learning Theory :

https://en.wikipedia.org/wiki/Draft:Uniform\_Stability\_and\_Generalization\_in\_learning\_theory

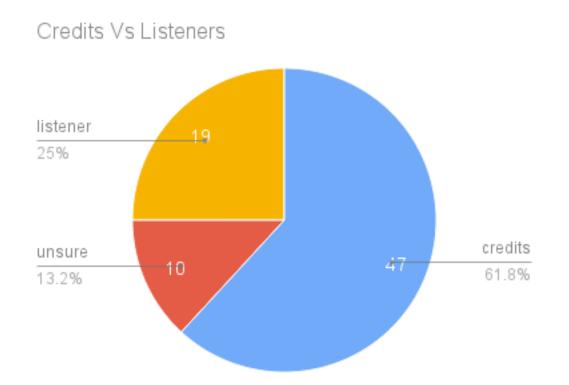
- Generalization Error: https://en.wikipedia.org/wiki/User:Agkonings/sandbox
- Tensor Completion : https://en.wikipedia.org/wiki/User:Aali9520/Tensor\_Completion
- Structured Sparsity Regularization : https://en.wikipedia.org/wiki/User:A.n.campero/sandbox
- Proximal Operator for Matrix Function : https://en.wikipedia.org/wiki/User:Lovebeloved/sandbox
- Sparse Dictionary Learning : we have pdf
- PAC Learning : https://en.wikipedia.org/wiki/User:Scott.linderman/sandbox
- Convolutional Neural Networks : https://en.wikipedia.org/wiki/User:Wfwhitney/sandbox
- Frames/Basis Functions: https://en.wikipedia.org/wiki/Frame\_(linear\_algebra)

#### **Class**

#### http://www.mit.edu/~9.520/

- The pace is fast on purpose...
- Big picture will be provided today and repeated at the end of the course...
- Be ready for a lot of material: this is MIT.
- If you need a refreshment in Fourier analysis you should not be in this class.
- We do not compare the approach in this class to others -- such as Bayesian one -- because we do not like to complain too much about others.

## 9.520 in 2015



## Summary of today's overview

- Motivations for this course: a golden age for new AI (and the key role of Machine Learning)
- Statistical Learning Theory
- Success stories from past research in Machine Learning: examples of engineering applications
- In this machine learning class: computer science and neuroscience, developing a theory for deep learning.

## Summary of today's overview

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- Success stories from past research in Machine Learning: examples of engineering applications
- A new phase in machine learning: computer science and neuroscience, learning and the brain, CBMM:

## The problem of intelligence: how it arises in the brain and how to replicate it in machines

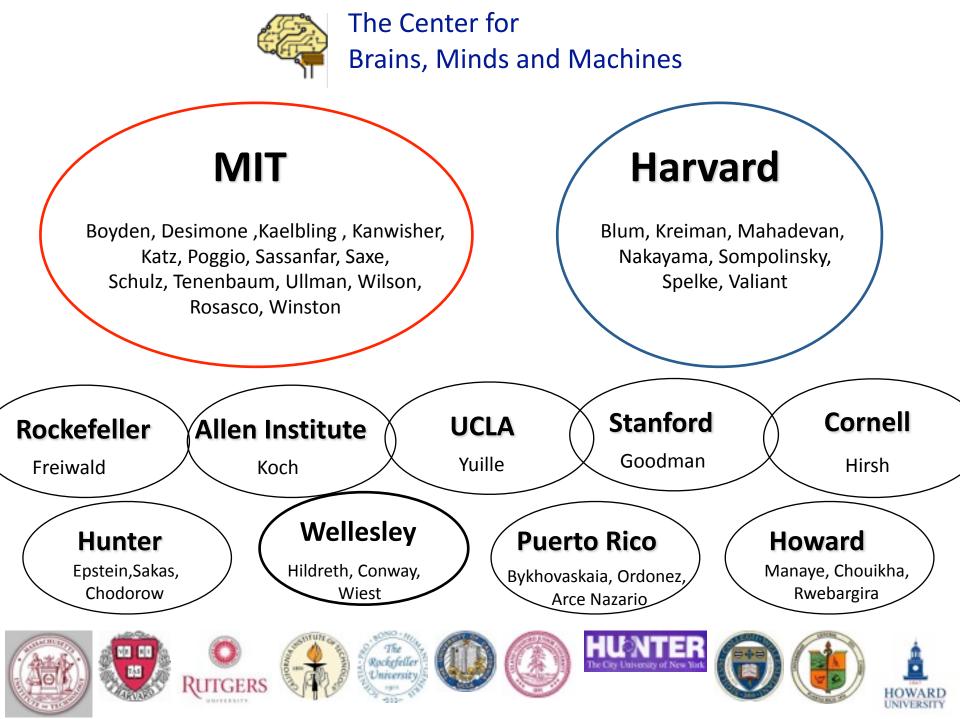
The problem of intelligence is one of the great problems in science, probably the greatest.

Research on intelligence:

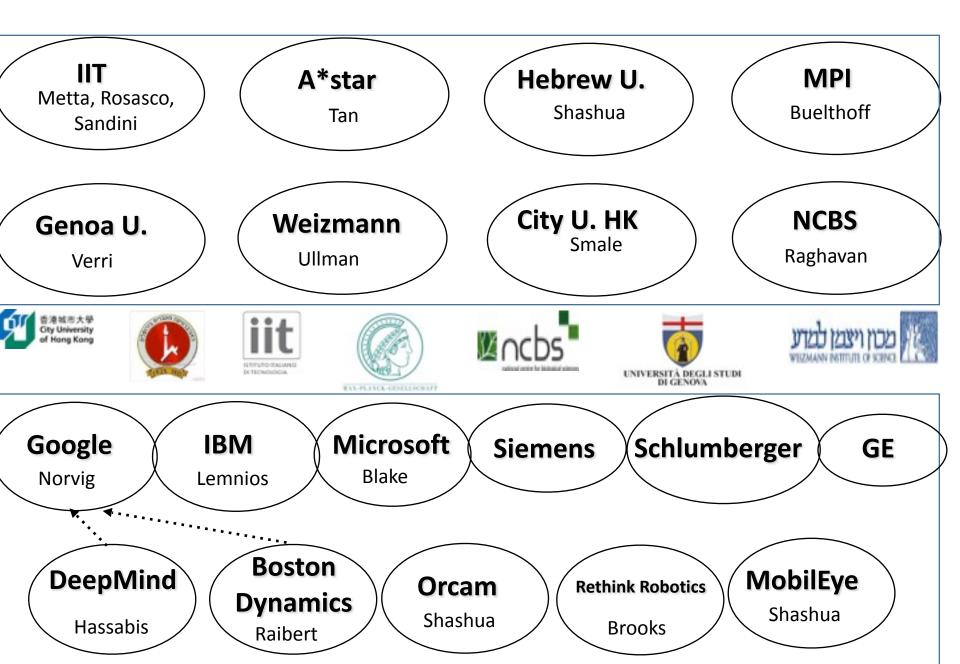
- a great intellectual mission: understand the brain, reproduce it in machines
- will help develop intelligent machines

These advances will be critical to of our society's

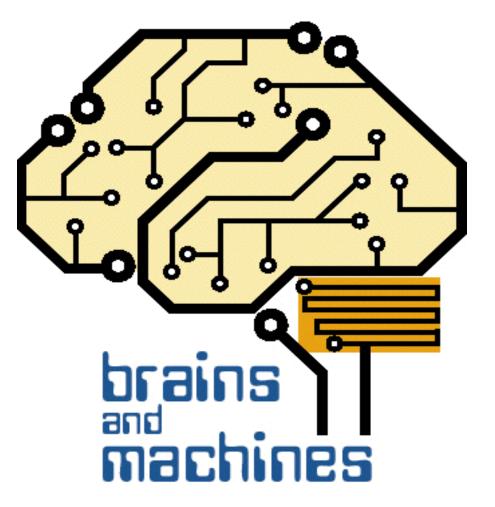
- future prosperity
- education, health, security



### Industrial partners



At the core of the problem of Intelligence is the problem of Learning



Learning is the gateway to understanding the brain and to making intelligent machines.

Problem of learning:

- a focus for
  - o math
  - o computer algorithms
  - neuroscience

## Theory of Learning

- Learning is now the lingua franca of Computer Science
- Learning is at the center of recent successes in AI over the last 15 years
- Now and the next 10 year will be a golden age for technology based on learning: Google, Siri, Mobileye, Deep Mind etc.
- The next 50 years will be a golden age for the science and engineering of intelligence. Theories of learning and their tools will be a key part of this.

#### Class

#### http://www.mit.edu/~9.520/

- The pace is fast on purpose, otherwise we get too bored.
- Big picture will be provided today and repeated at the end of the course. Listen carefully.
- Be ready for a lot of material: this is MIT.
- If you think that the course is disorganized, it means you have not really understood it.a
- I am passionate about ML and I will show it today. If you think Lorenzo is not, complain to him, not to me!
- Notation is kept inconsistent throughout the course on purpose to train you to read and understand different papers with different notations.
- If you need a refreshment in Fourier analysis you should not be in this class.
- We do not compare the approach in this class to others -- such as Bayesian one -- because we do not like to complain too much about others.

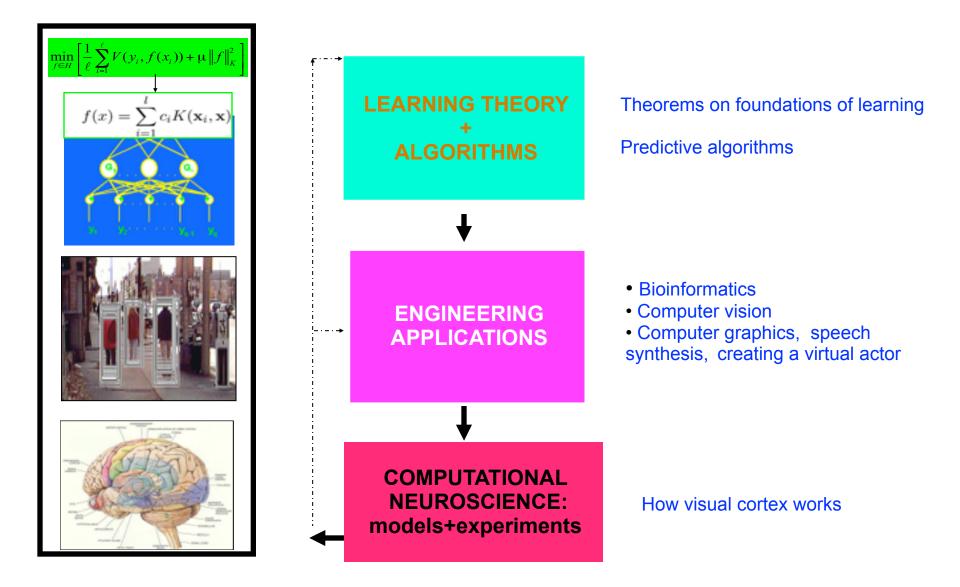
## Class <u>http://www.mit.edu/~9.520/</u>: big picture

- Classes 2-9 are the core: foundations + regularization
- Classes 10-20 are state-of-the-art topics for research in and applications of — ML
- Classes 21-26 are mostly new, about multilayer networks (DCLNs)

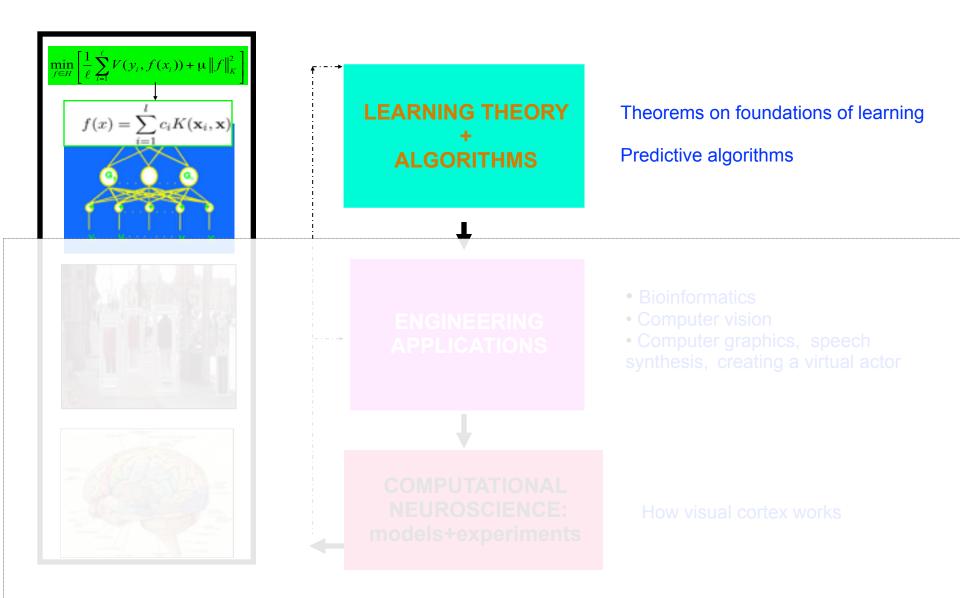
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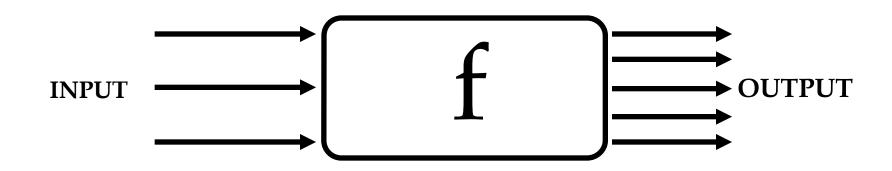
## Learning: Math, Engineering, Neuroscience



## **Statistical Learning Theory**



Statistical Learning Theory: supervised learning



Given a set of I examples (data)

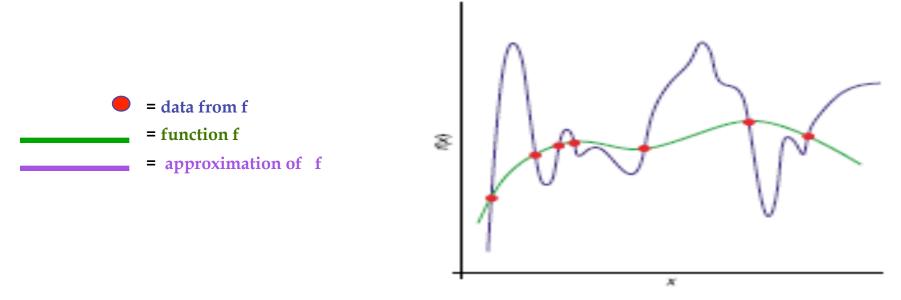
$$\{(x_1, y_1), (x_2, y_2), \dots, (x_{\ell}, y_{\ell})\}$$

Question: find function f such that

$$f(x) = \hat{y}$$

is a good predictor of y for a future input x (fitting the data is not enough!)

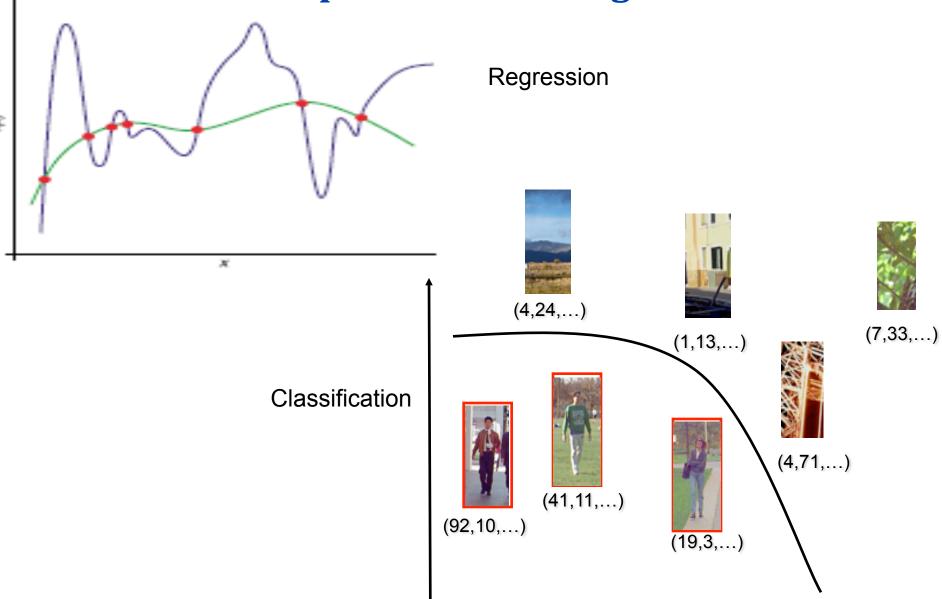
# Statistical Learning Theory: prediction, not curve fitting



#### Generalization:

estimating value of function where there are no data (good generalization means predicting the function well; important is for empirical or validation error to be a good proxy of the prediction error)

## Statistical Learning Theory: supervised learning



## Statistical Learning Theory: part of mainstream math not just statistics (Valiant, Vapnik, Smale, Devore...)

BULLETIN (New Series) OF THE AMERICAN MATHEMATICAL SOCIETY Volume 39, Number 1, Pages 1–49 S 0273-0979(01)00923-5 Article electronically published on October 5, 2001

#### ON THE MATHEMATICAL FOUNDATIONS OF LEARNING



FELIPE CUCKER AND STEVE SMALE

The problem of learning is arguably at the very core of the problem of intelligence, both bi

T. Poggio and C.R. Shelton

#### INTRODUCTION

(1) A main theme of this report is the relationship of approximation to learning and the primary role of sampling (inductive inference). We try to emphasize relations of the theory of learning to the mainstream of mathematics. In particular, there are large roles for probability theory, for algorithms such as *least squares*, and for tools and ideas from linear algebra and linear analysis. An advantage of doing this is that communication is facilitated and the power of core mathematics is more easily brought to bear.

# Statistical Learning Theory: supervised learning

There is an unknown **probability distribution** on the product space  $Z = X \times Y$ , written  $\mu(z) = \mu(x, y)$ . We assume that X is a compact domain in Euclidean space and Y a bounded subset of  $\mathbb{R}$ . The **training set**  $S = \{(\mathbf{x}_1, y_1), ..., (\mathbf{x}_n, y_n)\} = \{z_1, ..., z_n\}$ 

consists of *n* samples drawn i.i.d. from  $\mu$ .

- $\mathcal{H}$  is the **hypothesis space**, a space of functions  $f : X \to Y$ .
- A **learning algorithm** is a map  $L : Z^n \to \mathcal{H}$  that looks at S and selects from  $\mathcal{H}$  a function  $f_S : \mathbf{x} \to y$  such that  $f_S(\mathbf{x}) \approx y$  in a predictive way.

## Statistical Learning Theory: the learning problem should be well-posed



- A problem is well-posed if its solution
- exists, unique and

J. S. Hadamard, 1865-1963

is stable, eg depends continuously on the data (here examples)

Statistical Learning Theory: theorems extending foundations of learning theory

Conditions for <u>generalization</u> in learning theory

have deep, almost philosophical, implications:

they can be regarded as equivalent conditions that guarantee a theory to be predictive (that is scientific)

- theory must be chosen from a small set
- theory should not change much with new data...most of the time

A classical algorithm in Statistical Learning Theory: Kernel Machines eg Regularization in RKHS

$$\min_{f \in H} \left[ \frac{1}{n} \sum_{i=1}^{n} V(f(x_i) - y_i) + \lambda \| \|f\|_{K}^{2} \right]$$

implies

$$f(\mathbf{x}) = \sum_{i=1}^{n} \alpha_{i} K(\mathbf{x}, \mathbf{x}_{i})$$

Equation includes splines, Radial Basis Functions and SVMs (depending on choice of K and V).

For a review, see Poggio and Smale, 2003; see also Schoelkopf and Smola, 2002; Bousquet, O., S. Boucheron and G. Lugosi; Cucker and Smale; Zhou and Smale...

Statistical Learning Theory: classical algorithms: Regularization  $\min_{f \in H} \left[ \frac{1}{n} \sum_{i=1}^{n} V(f(x_i) - y_i) + \lambda \| \|f\|_{K}^{2} \right]$ 

has a Bayesian interpretation:

data term is a model of the noise and the stabilizer is a prior on the hypothesis space of functions f. That is, Bayes rule  $\mathcal{P}[D_{c}|f] = \mathcal{P}[f]$ 

$$\mathcal{P}[f|D_{\ell}] = \frac{\mathcal{P}[D_{\ell}|f] \ \mathcal{P}[f]}{P(D_{\ell})}$$

leads to

$$\mathcal{P}[f|D_{\ell}] = \frac{1}{Z_D Z_L Z_r} e^{-\left(\frac{1}{2\sigma^2} \sum_{i=1}^{\ell} (y_i - f(\mathbf{x}_i))^2 + \|f\|_K^2\right)}$$

## Statistical Learning Theory: classical algorithms: Regularization

Classical learning algorithms: Kernel Machines (eg Regularization in RKHS)

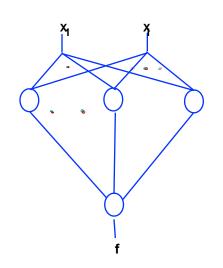
$$\min_{f \in H} \left[ \frac{1}{n} \sum_{i=1}^{n} V(f(x_i) - y_i) + \lambda \| \|f\|_{K}^{2} \right]$$

implies

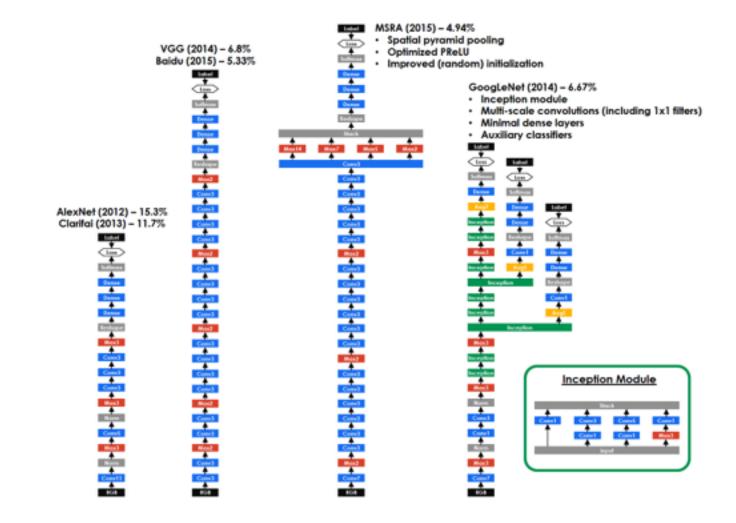
$$f(\mathbf{x}) = \sum_{i=1}^{n} \alpha_{i} K(\mathbf{x}, \mathbf{x}_{i})$$

Remark (for later use):

Classical kernel machines correspond to shallow networks



## A present challenge: a theory for Deep Learning



## Statistical Learning Theory: note

Two connected and overlapping strands in learning theory:

Bayes, hierarchical models, graphical models...

□ Statistical learning theory, regularization

## Summary of today's overview

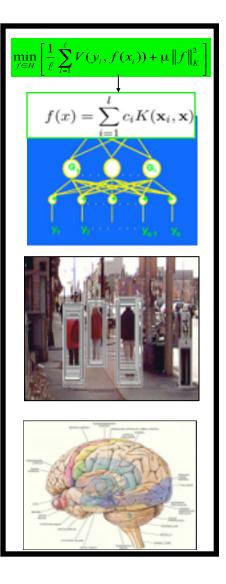
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## Supervised learning

Since the introduction of supervised learning techniques 20 years ago, AI has made significant (and not well known) advances in a few domains:

- Vision
- Graphics and morphing
- Natural Language/Knowledge retrieval (Watson and Jeopardy)
- Speech recognition (Nuance, Microsoft, Google)
- Games (Go, chess, Atari games...)
- Semiautonomous driving

#### Learning



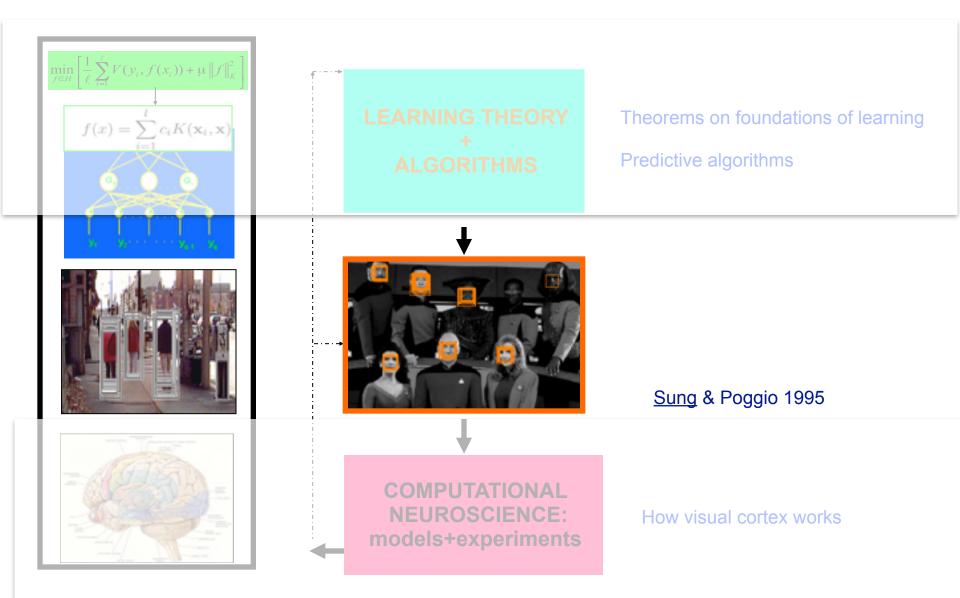




COMPUTATIONAL NEUROSCIENCE: models+experiments Theorems on foundations of learning Predictive algorithms

<u>Sung</u> & Poggio 1995, also Kanade& Baluja....

How visual cortex works



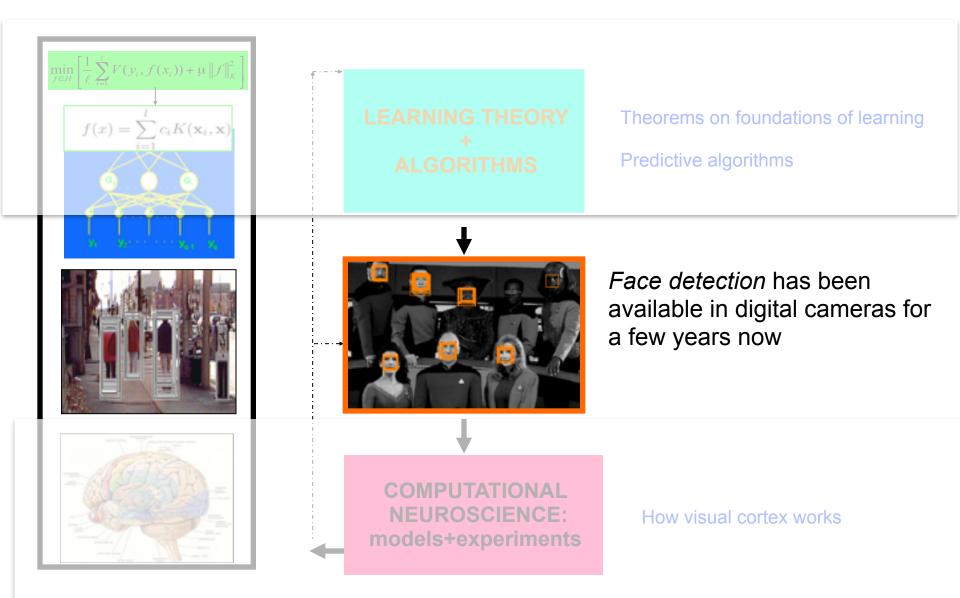


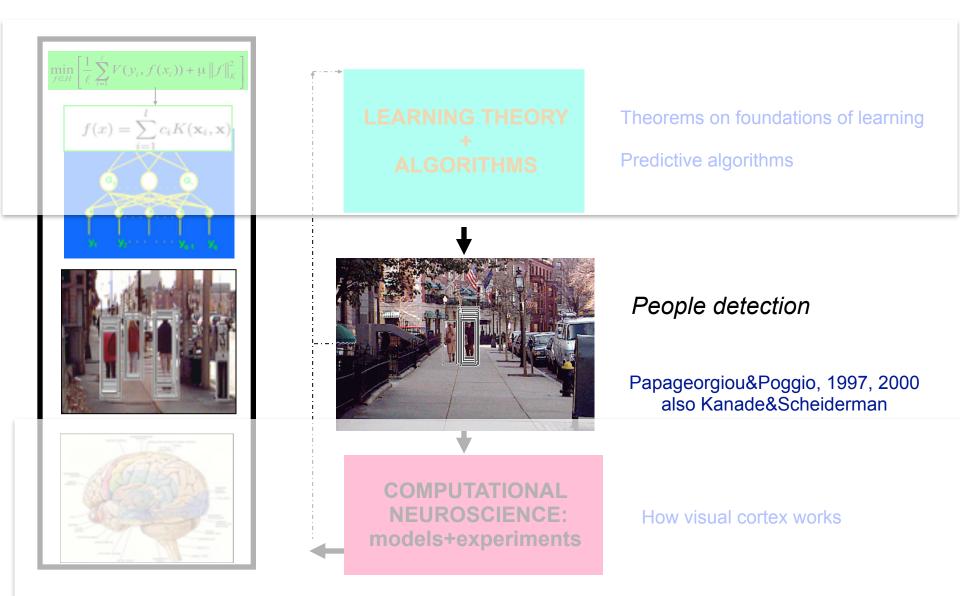


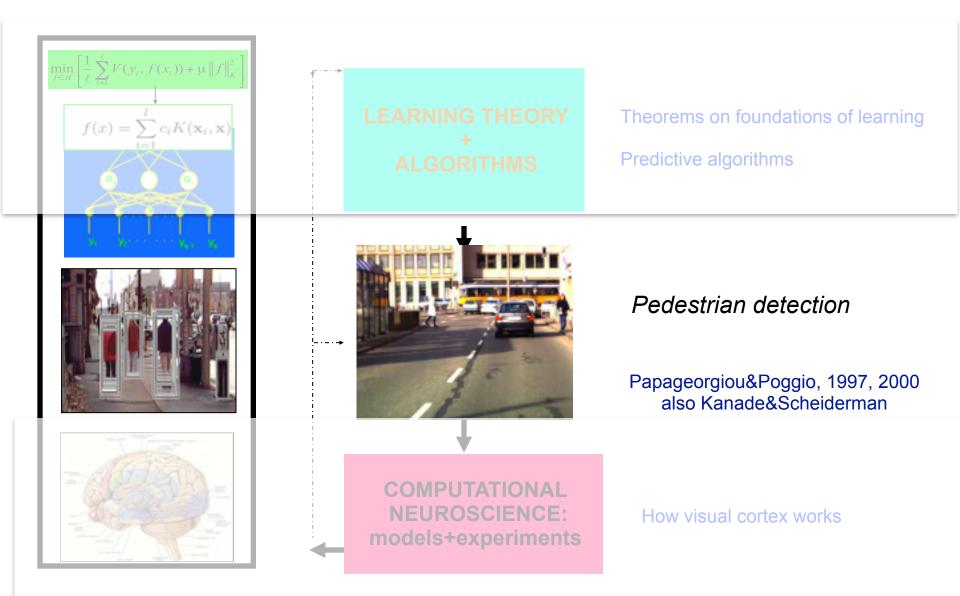
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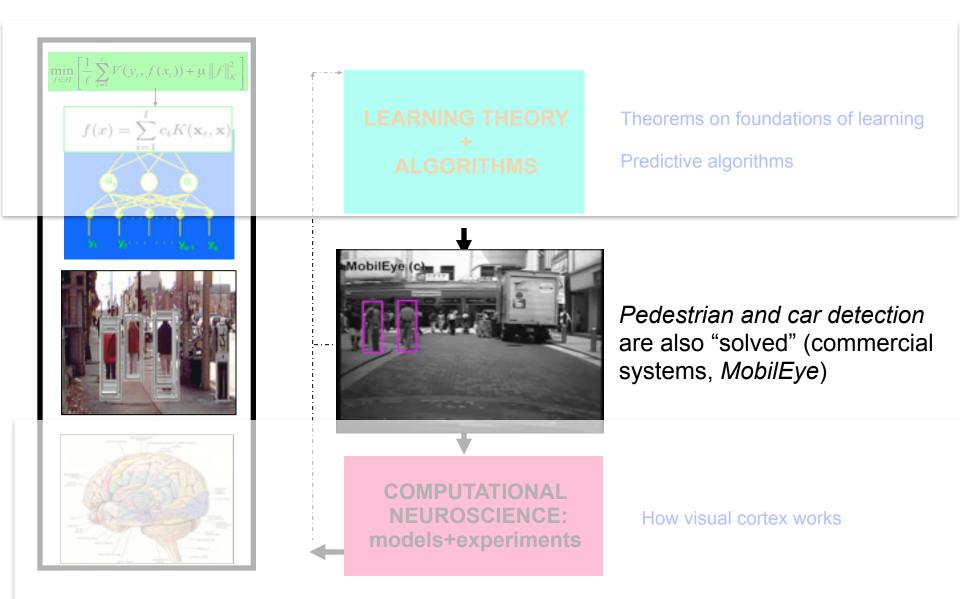
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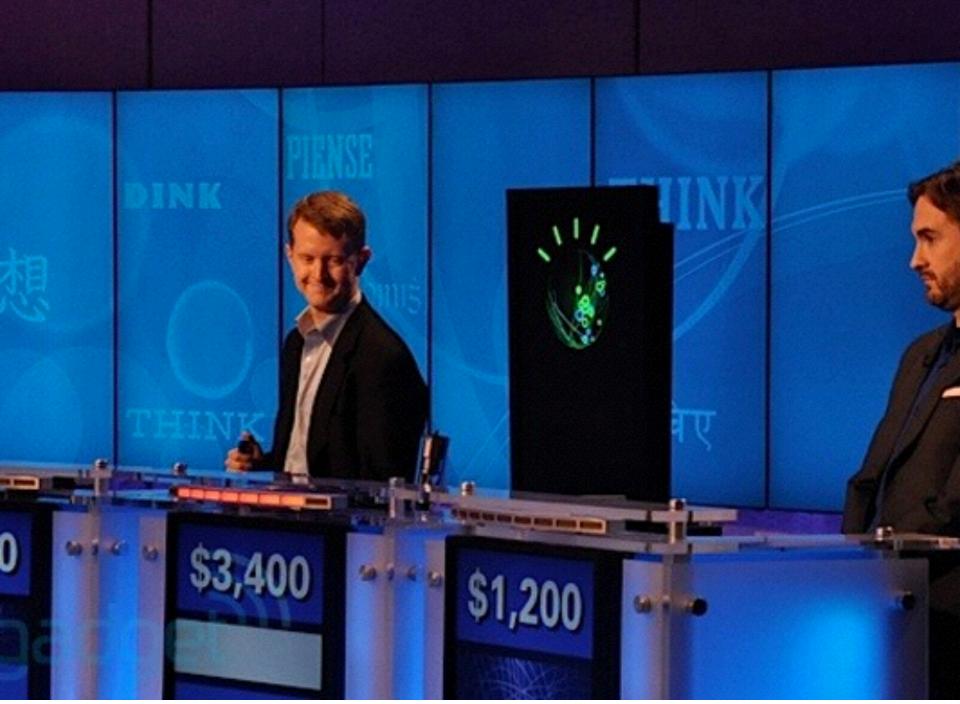




Recent progress in Al and machine learning

# Why now: recent progress in Al



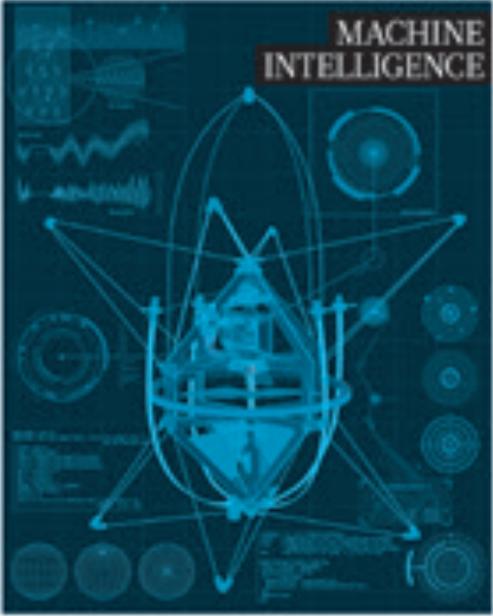




## Why now: very recent progress in Al



# natureINSIGHT





Pedestrian accidents occur every day in our increasingly intensive traffic environment.





Center for Brains, Minds & Machines

# Why now: very recent progress in Al







#### CBMM Summer School Schedule

August 13<sup>th</sup> through September 2<sup>nd</sup> Organized by the Center for Brains, Minds, and Machines At the Marine Biology Lab at Woods Hole

|                   |    | Morning 9-12                           | Afternoon 1:30-5:30                   | Evening 8-9             |           |
|-------------------|----|--|---------------------------------------|-------------------------|-----------|
| Th                | 13 |  | Reception - 5PM - Swope               |                         |           |
| F                 | 14 | Introduction                           | Student introductions                 | Project introductions   | Social    |
| Sa                | 15 | Line ar algebra, probability           | Neuroscience, programming             | Project discussion      |           |
| Su                | 16 | iCub, Google Glass                     |                                       | Dinner - 6:30 - Swope   |           |
| м                 | 17 | Computational neuroscience/            | Biological and computer vision        | Larry Abbott            | Reception |
|                   |    | Propagation of sensory representations | Jim DiCarlo                           |                         |           |
|                   |    | in cortex-like deep architectures      |                                       |                         |           |
|                   |    | Gabriel Kæiman/Haim Sompolinsky        |                                       |                         |           |
| Tu                | 18 | Cognitive Neuroscience                 | Computer vision, deep learning        | Tom Mitchell            | Reception |
|                   |    | and Face Recognition                   | Andrei Barbu                          |                         |           |
|                   |    | Winrich Freiwald, Nancy Kanwisher      |                                       |                         |           |
| w                 | 19 | Machine learning                       | Machine learning                      | Demis Hassabis          | Reception |
|                   |    | Lorenzo Rosasco                        | Lorenzo Rosasco                       |                         |           |
| Th*               | 20 | Surya Ganguli                          | Robotics Afternoon                    |                         |           |
| F                 | 21 | Computational cogsci                   | Church                                |                         |           |
|                   |    | Josh Tenenbaum, Tomer Uliman           | Tomer Uliman                          |                         |           |
| Sa                | 22 |  |                                       |                         |           |
| Su                | 23 | Martha's Vineyard trip                 |                                       |                         |           |
| М                 | 24 | Memory                                 | AI / Vision                           | Eero Simoncelli         | Reception |
|                   |    | Matt Wilson, Aude Oliva                | Shimon Uliman                         |                         |           |
| Tu                | 25 | Development I                          | Psychophysics and mTurk               | Dorin Comaniciu         | Reception |
|                   |    | Liz Spelke, Alia Martin                | Leyla Isik, Tomer Uliman              |                         |           |
| W*                | 26 | Social perception                      | Neural data analysis                  |                         |           |
|                   |    | Rebecca Saxe, Ken Naksyama             | Ethan Meyers                          |                         |           |
| Th                | 27 | Development II                         | Invariance, inverse problems          | Jessica Sommerville     | Reception |
|                   |    | Laura Schulz, Tomer Uliman             | Tomaso Poggio, Mahadevan              |                         | -         |
| F*                | 28 | AI / Language                          | AI / Vision                           |                         |           |
|                   |    | Patrick Winston, Boris Katz            | Andrei Barbu                          |                         |           |
| Sa                | 29 | Audition and speech                    | Audition/vision panel                 |                         |           |
|                   |    | Josh McDermott, Hynek Hermansky        | J. McDermott, H. Hermansky, D. Yamins |                         |           |
| Su*               | 30 |  |                                       | Dinner - 6:30 - Swope   |           |
| м                 | 31 |  |                                       | Amnon Shashua           | Reception |
| Tu                | 1  |  |                                       |                         |           |
| w                 | 2  | Student presentations                  |                                       | Closing reception - 7PM |           |
|                   |    |  |                                       |                         |           |
| talk social panel |    |  |                                       |                         |           |

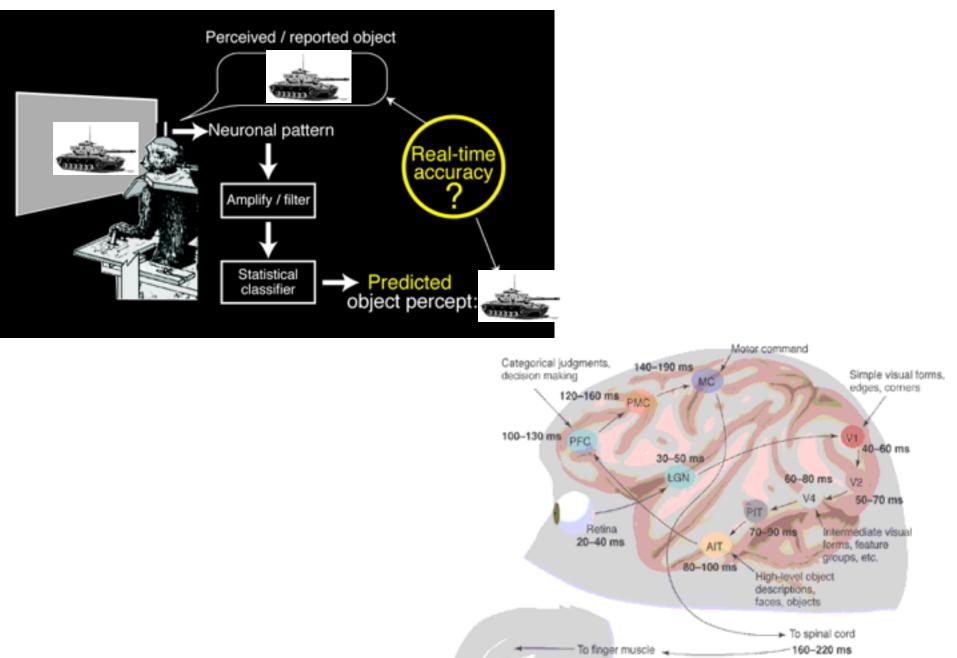
project tutorial

\*Starred days will feature a journal club.

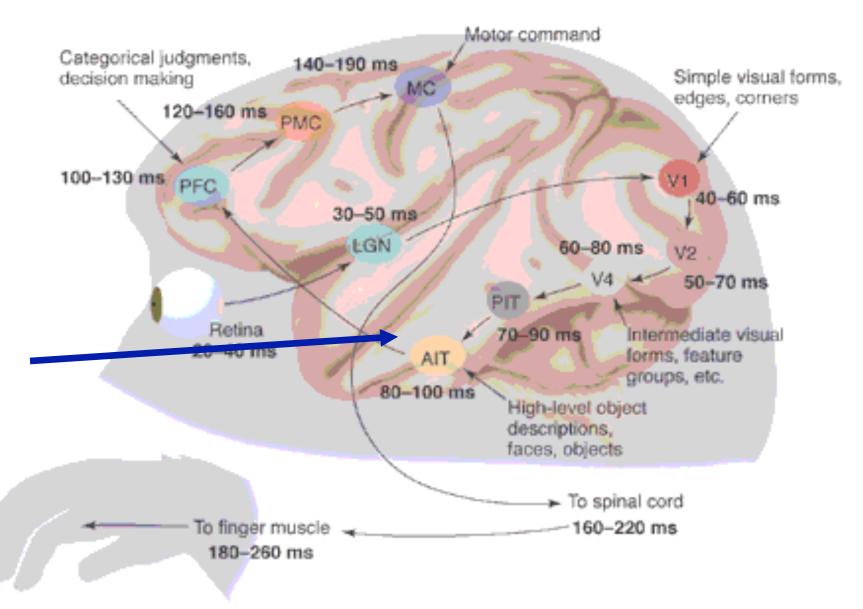
Talks (red) are in Lillie Audiorium. Tutorials and Projects (orange, green) are in Loeb 306. Some other examples of past ML applications from my lab

- Computer Vision
- Face detection
- Pedestrian detection
- Scene understanding
- Video categorization
- Video compression
- Pose estimation
- Graphics
- Speech recognition
- Speech synthesis
- Decoding the Neural Code
- **Bioinformatics**
- Text Classification
- Artificial Markets
- Stock option pricing

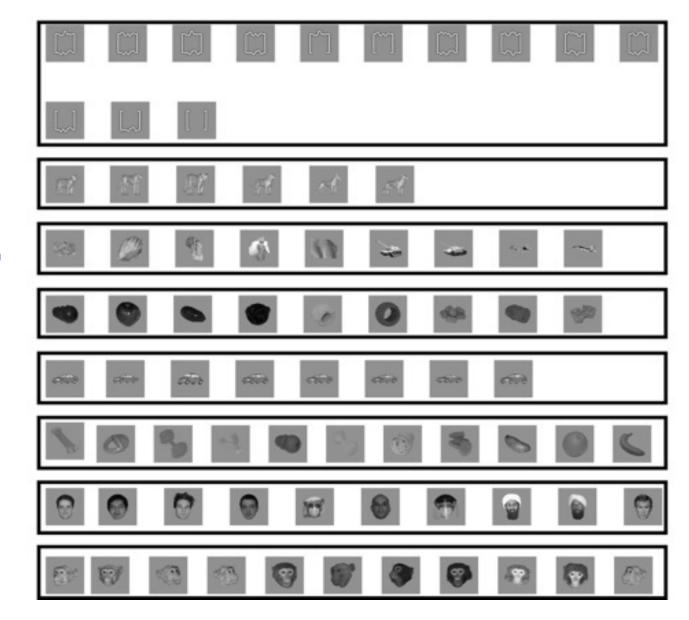
#### Decoding the neural code: Matrix-like read-out from the brain



# The end station of the ventral stream in visual cortex is IT



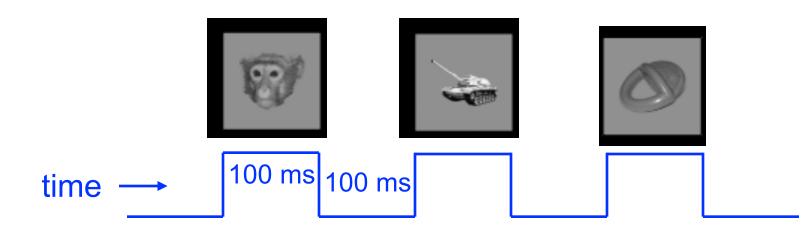
Reading-out the neural code in AIT



77 objects,8 classes

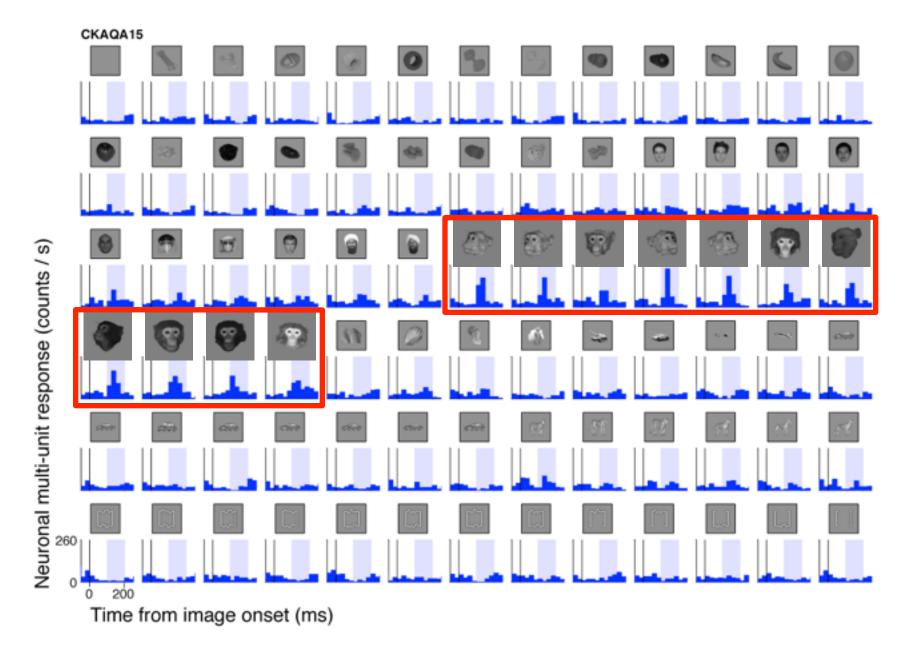
Chou Hung, Gabriel Kreiman, James DiCarlo, Tomaso Poggio, Science, Nov 4, 2005

Recording at each recording site during passive viewing

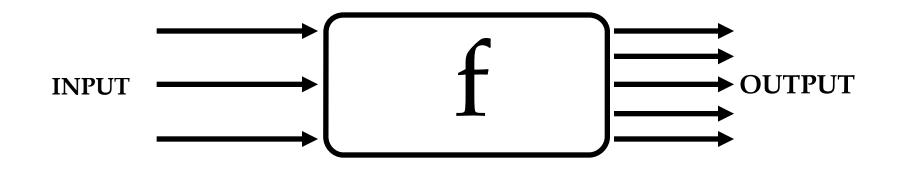


- 77 visual objects
- 10 presentation repetitions per object
- presentation order randomized and counter-balanced

#### **Example of one AIT cell**



#### Learning: read-out from the brain

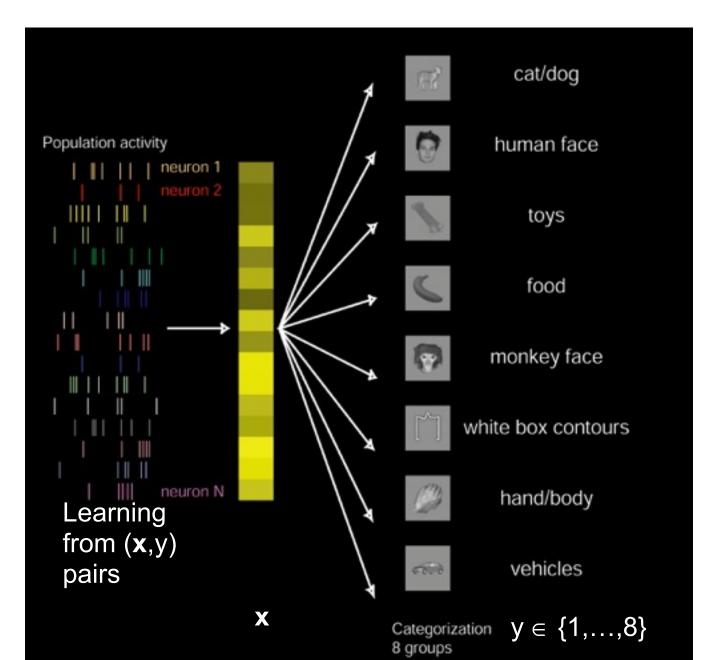


From a set of data (vectors of activity of n neurons (x) and object label (y)  $\{(x_1, y_1), (x_2, y_2), \dots, (x_{\ell}, y_{\ell})\}$ 

Find (by training) a classifier eg a function f such that  $f(x) = \hat{y}$ 

is a good predictor of object labely for a future neuronal activity x

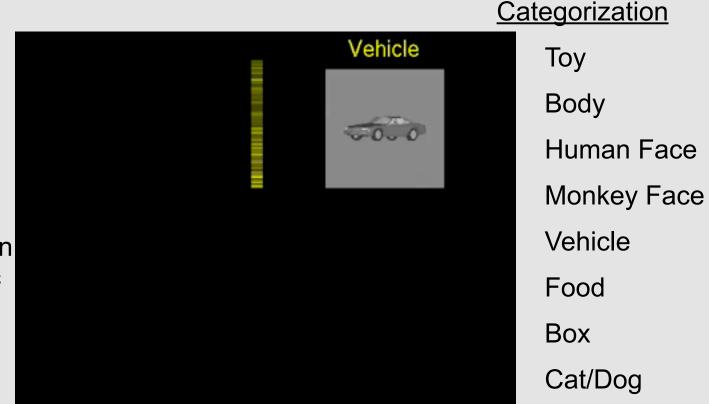
#### **Decoding the neural code ... using a classifier**



We can decode the brain's code and read-out from neuronal populations: reliable object categorization (>90% correct) using ~200 <u>arbitrary</u> AIT "neurons"

Video speed: 1 frame/sec

Actual presentation rate: 5 objects/sec

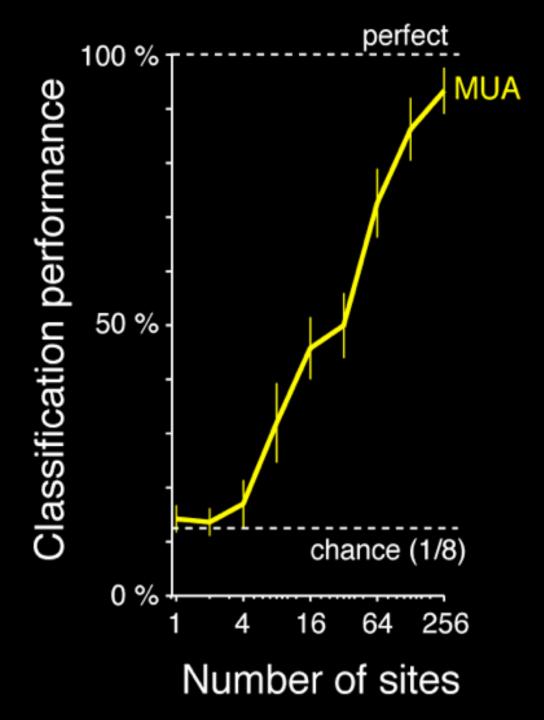


Hung, Kreiman, Poggio, DiCarlo. Science 2005

We can decode the brain's code and read-out from neuronal populations:

reliable object categorization using ~100 arbitrary AIT sites

- [100-300 ms] interval
- 50 ms bin size



#### Learning: image analysis



#### $\Rightarrow$ Bear (0° view)



#### $\Rightarrow$ Bear (45° view)

Learning: image synthesis

#### **UNCONVENTIONAL GRAPHICS**

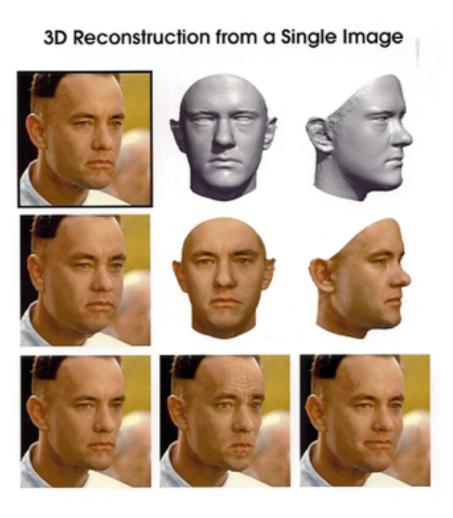


$$\Theta$$
 = 0° view  $\Rightarrow$ 



$$\Theta$$
 = 45° view  $\Rightarrow$ 

#### Learning: image synthesis



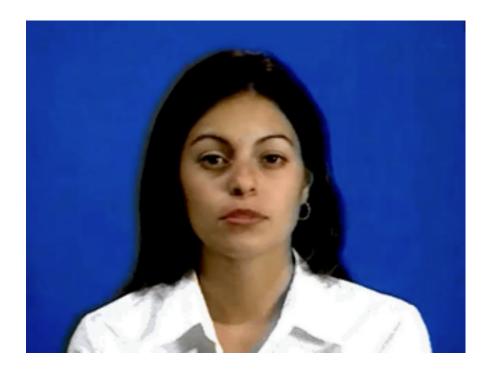
Blanz and Vetter, MPI SigGraph '99

#### Learning: image synthesis



Blanz and Vetter, MPI SigGraph '99

#### Mary101



A- more in a moment

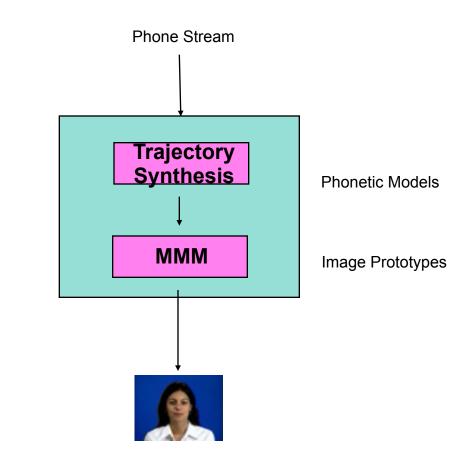
Tony Ezzat, Geiger, Poggio, SigGraph 2002

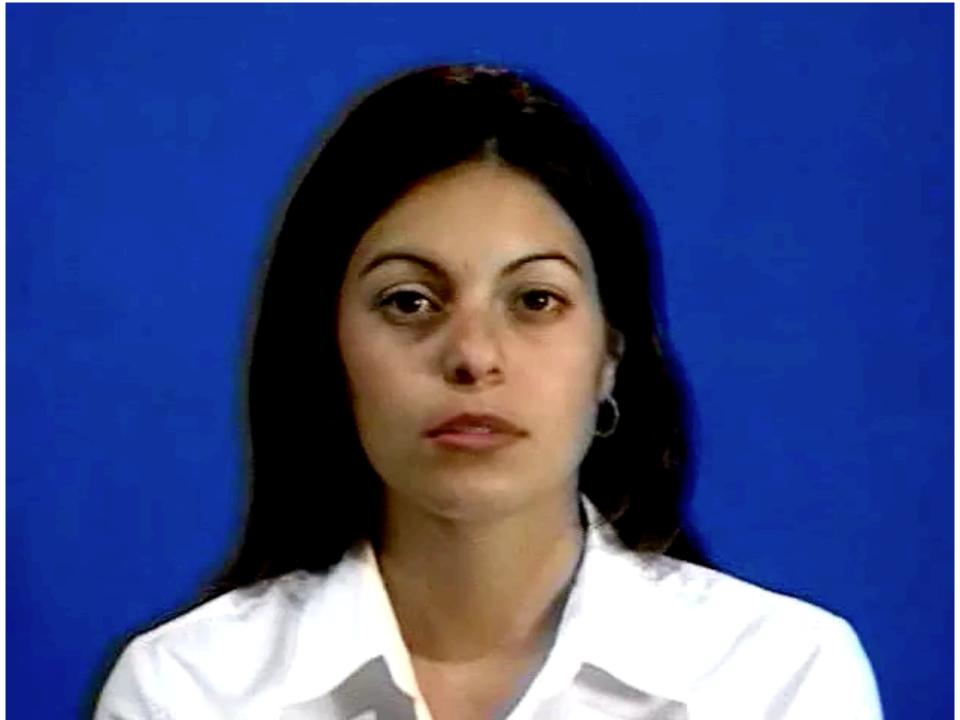
#### 1. Learning

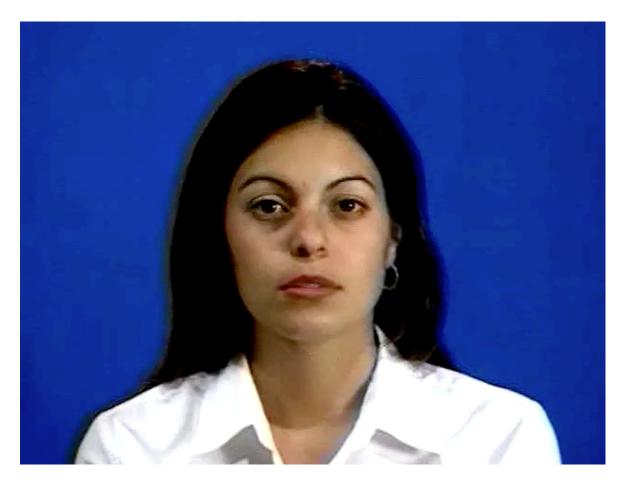
System learns from 4 mins of video face appearance (Morphable Model) and speech dynamics of the person

#### 2. Run Time

For any speech input the system provides as output a synthetic video stream







B-Dido



C-Hikaru



D-Denglijun



E-Marylin



F-Katie Couric



G-Katie



H-Rehema



I-Rehemax

### A Turing test: what is real and what is synthetic?



L-real-synth

### A Turing test: what is real and what is synthetic?

| Experiment        | # subjects | % correct | t     | p<  |
|-------------------|------------|-----------|-------|-----|
| Single pres.      | 22         | 54.3%     | 1.243 | 0.3 |
| Fast single pres. | 21         | 52.1%     | 0.619 | 0.5 |
| Double pres.      | 22         | 46.6%     | -0.75 | 0.5 |

Table 1: Levels of correct identification of real and synthetic sequences. t represents the value from a standard t-test with significance level of p<.

## Summary of today's overview

- Motivations for this course: a golden age for new AI and the key role of Machine Learning
- Statistical Learning Theory
- Success stories from past research in Machine Learning: examples of engineering applications
- Our machine learning class: science of intelligence, learning and the brain, CBMM.

## What is this?

## What is Hueihan doing?

## What does Hueihan think about Joel's thoughts about her?

## Intelligence and Turing<sup>++</sup> Questions

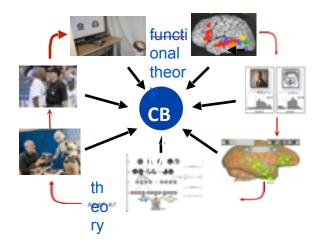
• Intelligence —> <u>Human</u> Intelligence

• (Human) Intelligence: one word, many problems

• A CBMM mission: define and "answer" these *Turing*<sup>++</sup> *Questions* 

## **Turing**<sup>++</sup> **Questions**



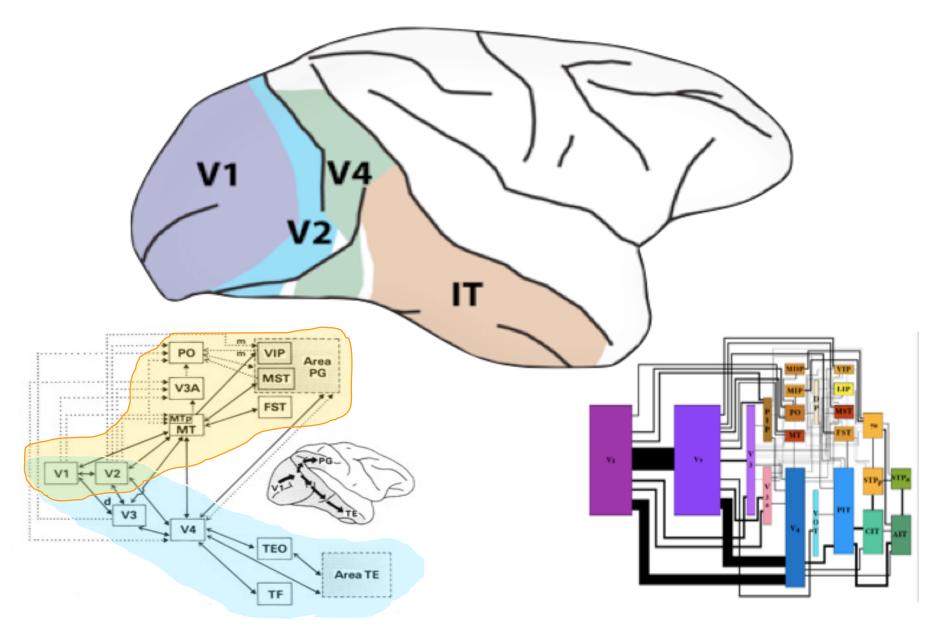


The challenge is to develop computational models that answer questions about images and videos such as *what is there / who is there / what is the person doing* and eventually more difficult questions such as *who is doing what to whom?* 

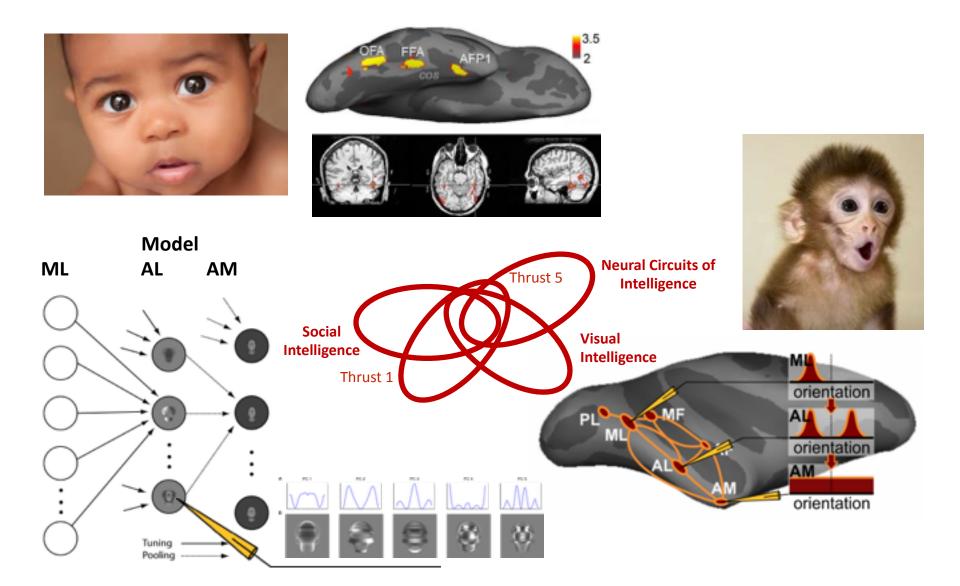
• what happens next?

at the computational, psychophysical and neural levels.

**Object recognition** 

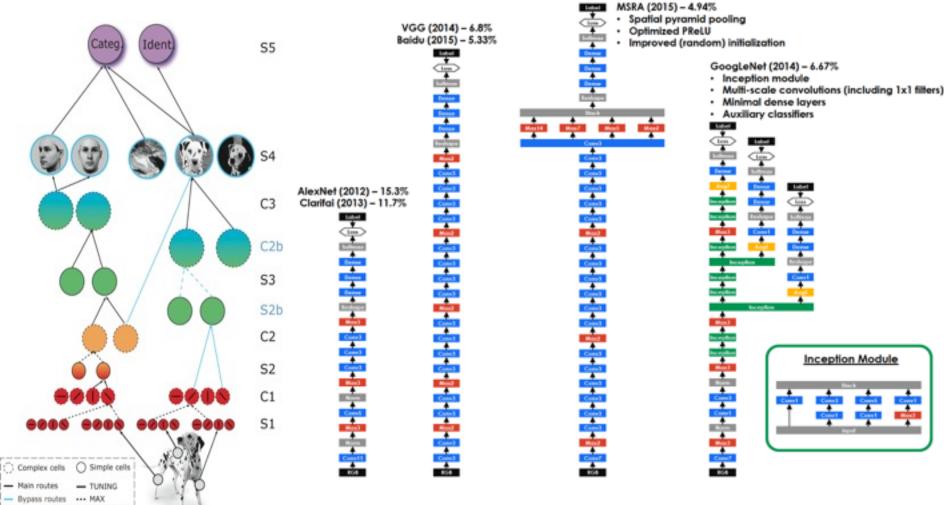


#### The who question: face recognition from experiments to theory (Workshop, Sept 4-5, 2015)



## Extended i-theory

#### Learning of invariant&selective Representations

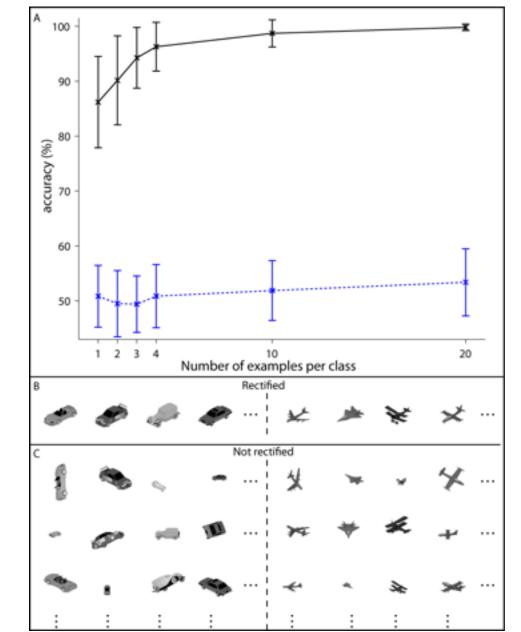


i-theory: invariant representations lead to lower sample complexity

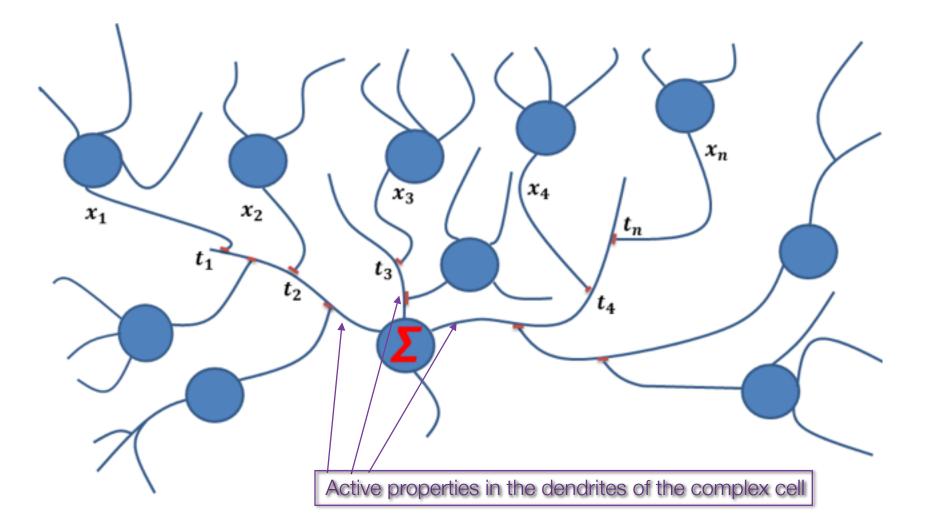
for a supervised classifier

**Theorem** (translation case) Consider a space of images of dimensions  $d \times d$ pixels which may appear in any position within a window of size  $rd \times rd$  pixels. The usual image representation yields a sample complexity (of a linear classifier) o f order  $m = O(r^2 d^2)$ ; the oracle representation (invariant) yields (because of much smaller covering numbers) a sample complexity of order

$$m_{oracle} = O(d^2) = \frac{m_{image}}{r^2}$$



## Dendrites of a complex cells as simple cells...



I am now more in favor of deep learning as models of parts of the brain

WHY?

The background: DCLNs (Deep Convolutional Learning Networks) are doing very well

# Is the lack of a theory a problem for DCLNs?

In Poggio and Smale (2003) we wrote "A comparison with real brains offers another, and probably related, challenge to learning theory. The ``learning algorithms'' we have described in this paper correspond to one-layer architectures. Are hierarchical architectures with more layers justifiable in terms of learning theory? Twelve years later, a most interesting theoretical question that still remains open, both for machine learning and neuroscience, is indeed why hierarchies.

## What if DCLNs are the secret of the brain?

## Is supervised training with millions of labeled examples biologically plausible?

## Implicitly Labeled Examples (ILEs): interesting research here!

Deep Convolutional Learning Networks like HMAX can be trained effectively with large numbers of labeled examples. This may be biologically plausible if we can show that ILEs could be be used to the same effect. What needs to be done is to train, with a plausible number of ILEs, biologically plausible multilayer architectures. For instance, for visual cortex take into account known parameters, such as receptive field sizes, related range of pooling and especially eccentricity dependence of RF. Through a new theory for DCLNs to the next frontier in machine learning

## <u>The first phase</u> (and successes) of ML: supervised learning: $n \rightarrow \infty$

 $n \rightarrow 1$ 



<u>The next phase</u> of ML: unsupervised and *implicitely supervised* learning of invariant representations for learning: