

In-Medium Form-Factors and the Coulomb Sum Rule

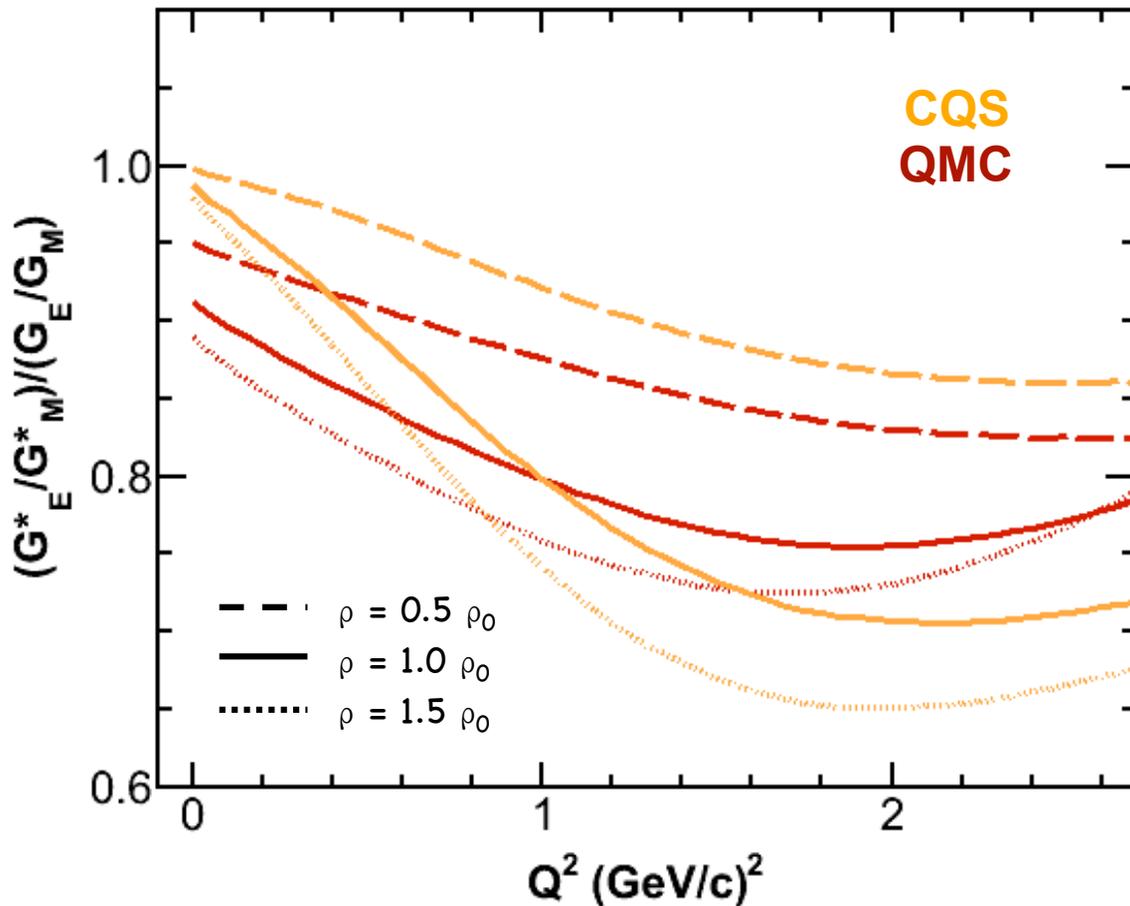
- Models
- Experiments on nuclei that are sensitive to form factors
 - $(e,e'N)$ - quasi-elastic proton knockout
 - (e,e') - quasi-elastic inclusive cross section

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Quantitative challenges in EMC and SRC Research and Data-Mining,
MIT, December 2-5, 2016

Models Predict Form-Factor Medium Modifications



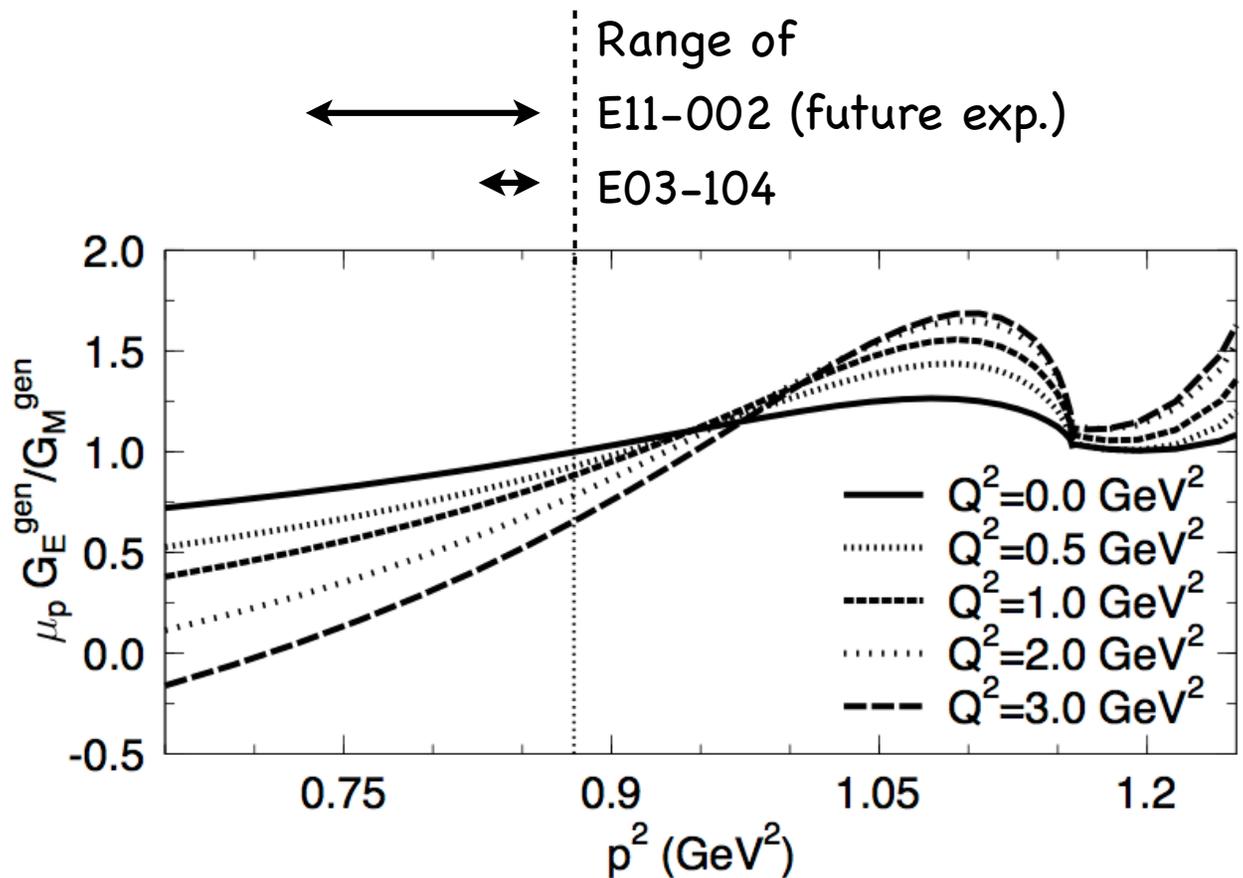
CQS: J.R. Smith and G.A. Miller, Phys. Rev. C **70**, 065205 (2004)

QMC: D.H. Lu et al., Phys. Lett. B **417**, 217 (1998)

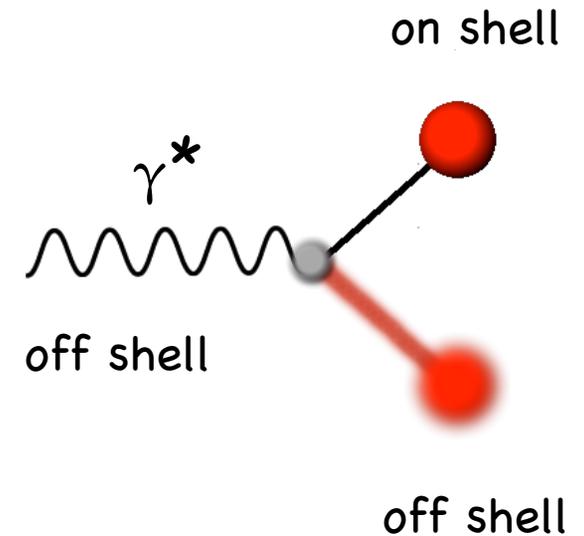
NJL: I.C. Cloet, W. Bentz, and A.W. Thomas

- Changes in the internal structure of bound nucleons result also in **bound nucleon form factors**.
- Chiral Quark Soliton (CQS), Quark Meson Coupling (QMC), Skyrme, Nambu-Jona-Lasinio (NJL), GPD Models.
- Observable effects predicted. Model predictions:
 - are density and Q^2 dependent,
 - show similar behavior,
 - consistent with experimental data (within large uncertainties).

Form Factors in the Dressed γNN Vertex



photon-nucleon vertex

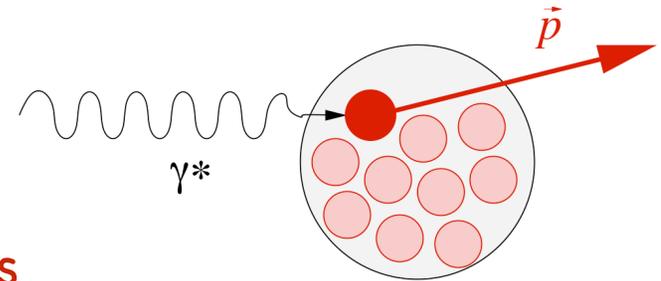


- **Dressed K-Matrix model (DKM):** dressing the bare vertex with an infinite number of meson loops (π , ρ , σ mesons)

Polarization-Transfer Technique

$$\frac{G_{Ep}}{G_{Mp}} = -\frac{P'_x}{P'_z} \frac{E_i + E_f}{2m} \tan \frac{\theta_e}{2}$$

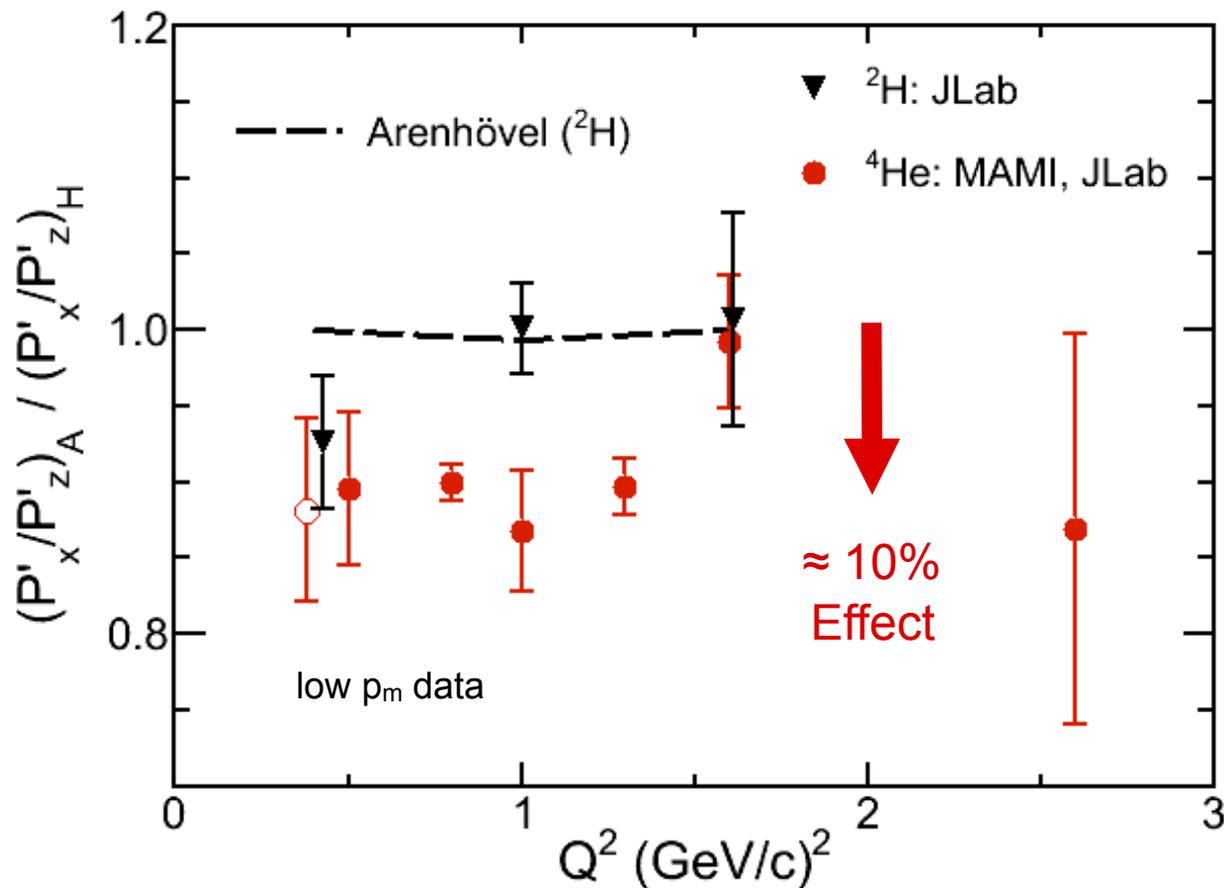
- Free nucleon
- Bound nucleon data need evaluation within model
Reaction-mechanism effects predicted to be small and minimal for
 - Quasi-elastic scattering
 - High Q^2 , small missing momenta
- Compare quasi-elastic and free-proton scattering to study possible medium effects



$$R = \left(\frac{P'_x}{P'_z} \right)_A / \left(\frac{P'_x}{P'_z} \right)_H$$

$${}^A X(\vec{e}, e' \vec{p}) {}^{A-1} X$$

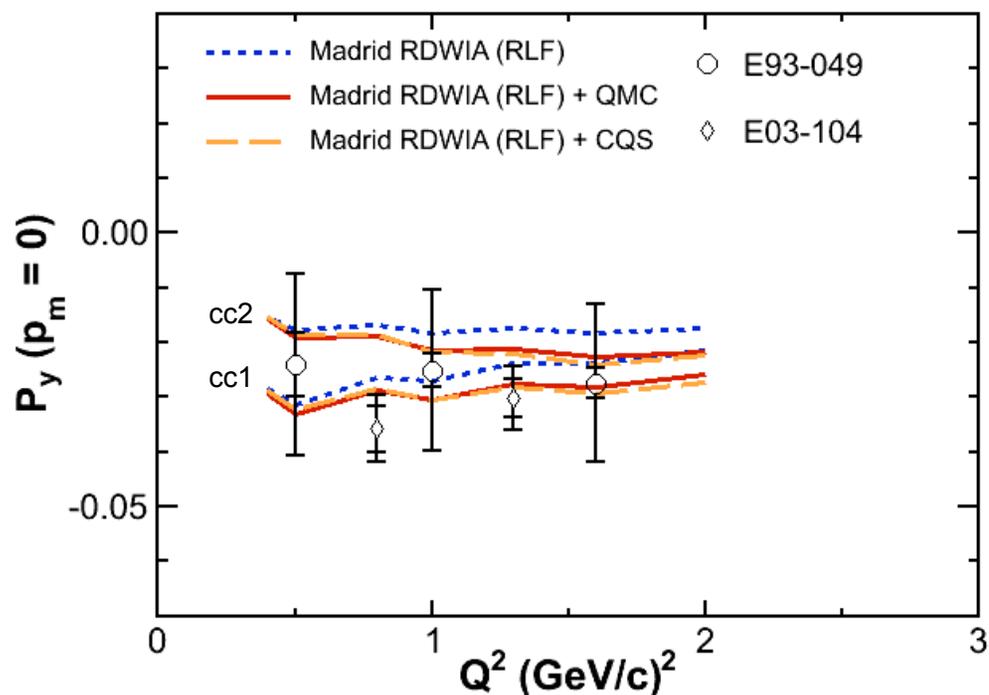
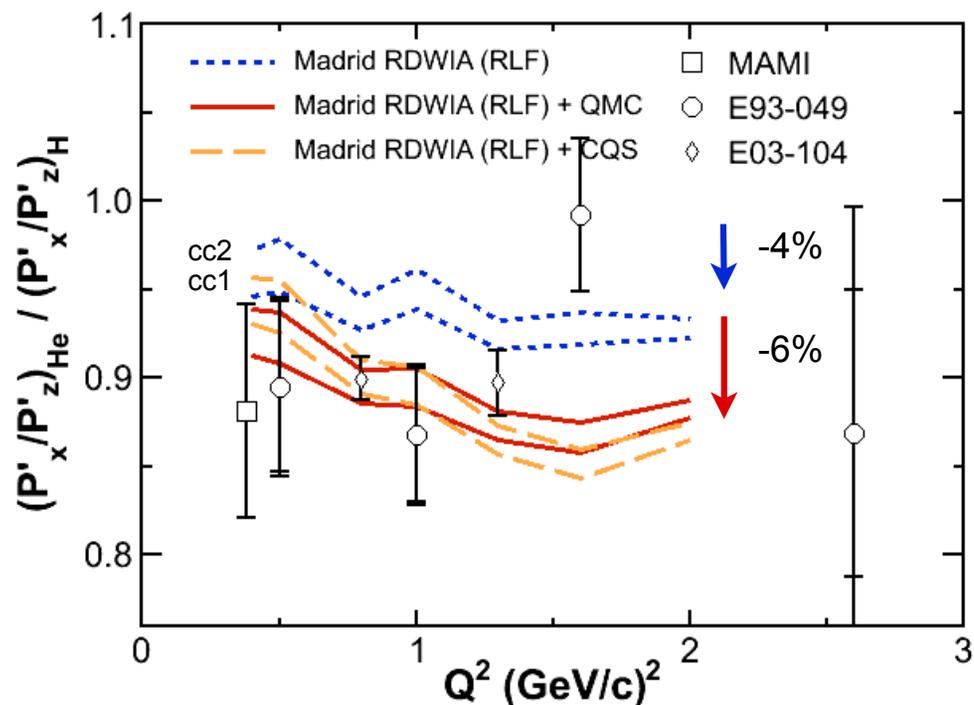
Strong Medium Effects Observed in ^4He Polarization-Transfer Double Ratios



- ^2H and ^1H polarization-transfer data are similar
- ^4He data are significantly different than ^2H , ^1H data

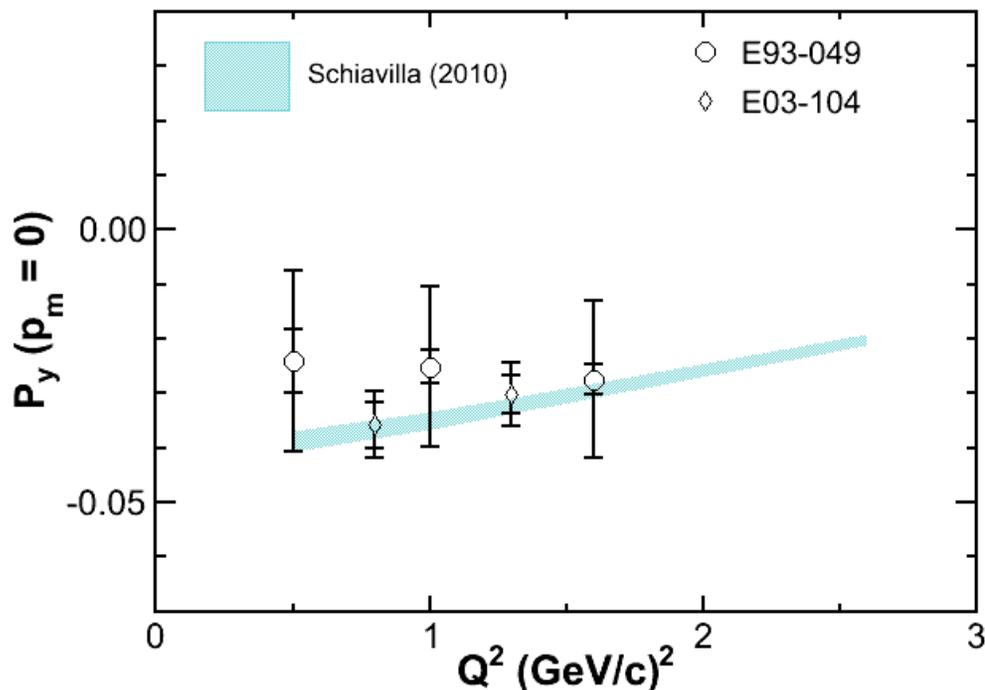
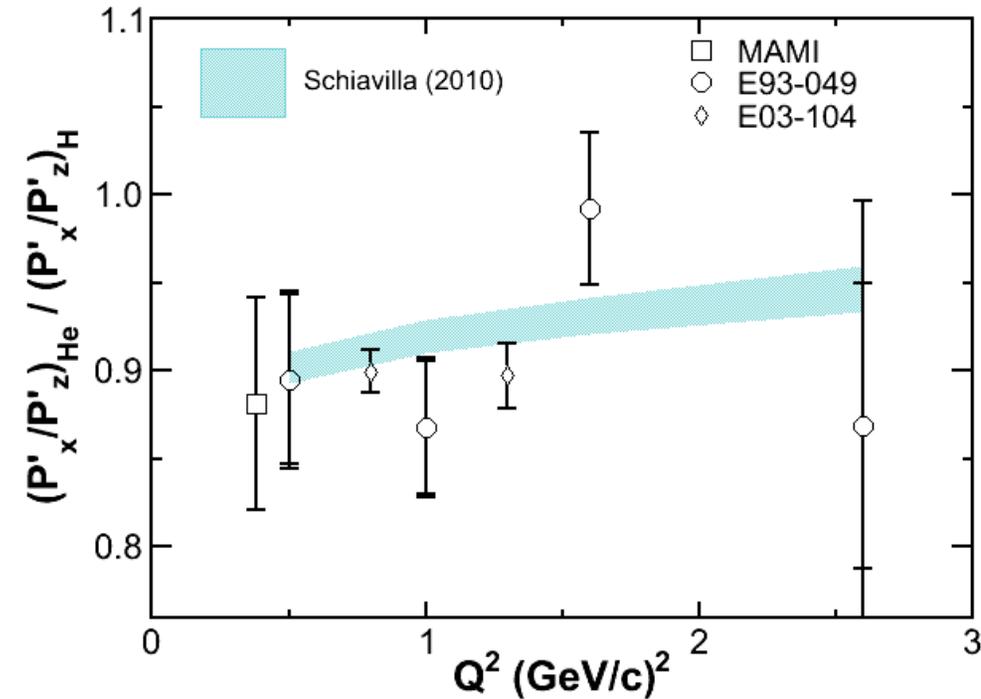
^2H : B. Hu et al., PRC **73**, 064004 (2006). ^4He : S. Dieterich et al., PLB **500**, **47** (2001); S. S., et al., PRL **91**, 052301 (2003); M. Paolone, et al., PRL **105**, 0722001 (2010); S. Malace et al., PRL **106**, 052501 (2011)

Madrid RDWIA



- Relativistic calculation in distorted-wave impulse approximation (**RDWIA**) overestimates R
- Both, the **QMC** and **CQS** models give reduction in R by about 6% and are in very good agreement with data
- Induced polarization, P_y , is almost exclusively sensitive to FSI
- **RLF optical potential** along with cc1 current operator results in excellent description of P_y within the Madrid model

Schiavilla (2010)

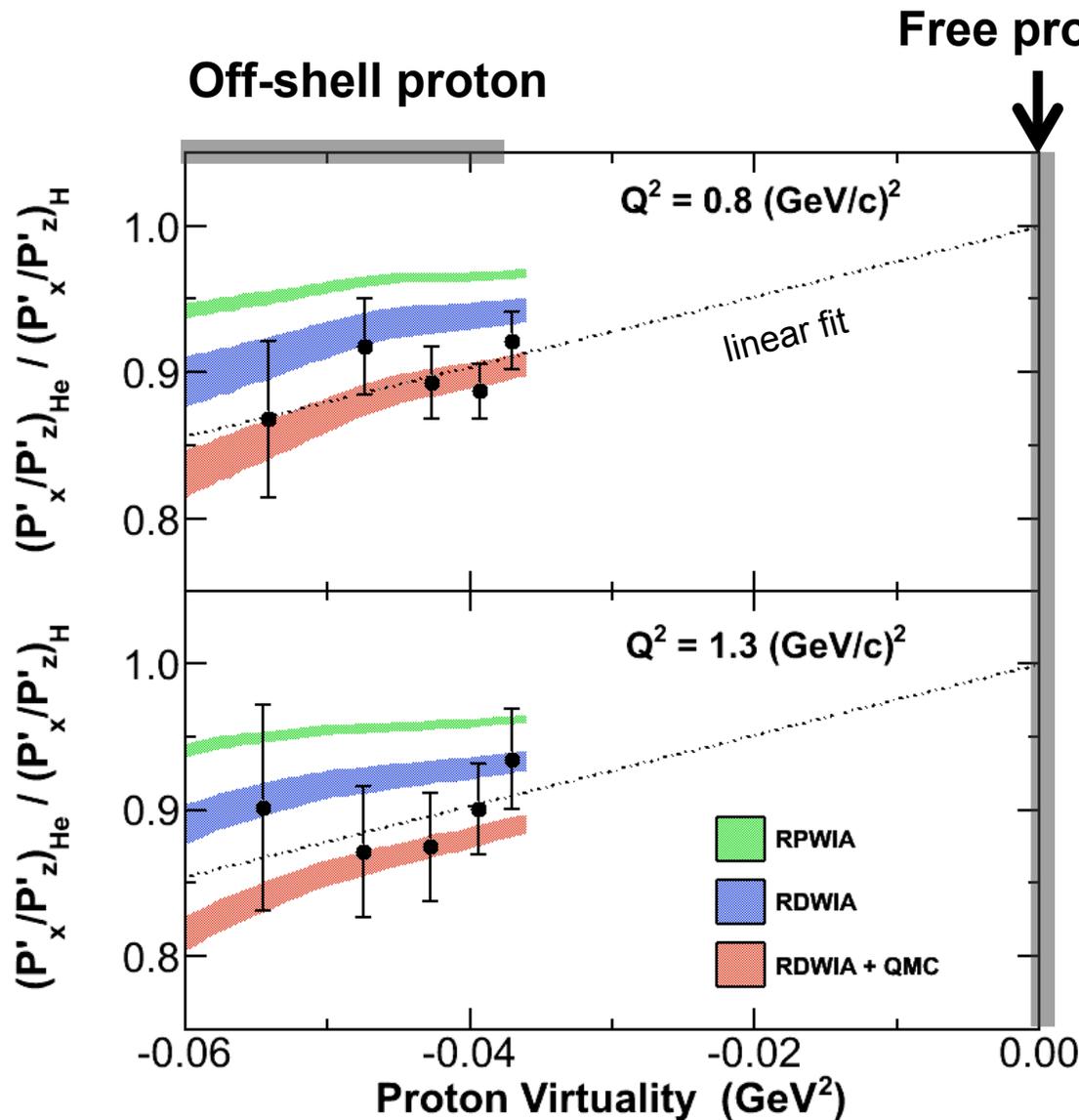


- Variational wave functions for the bound three- and four-nucleon systems + nonrelativistic MEC
- Optical potentials include additional charge-exchange terms which are not all well constrained.
- The charge-exchange independent spin-orbit component of the optical potential was reduced to describe the P_y data (2010).
- Very good agreement with the data after fitting FSI parameters to the induced polarization of E03-104.

R. Schiavilla, O. Benhar, A. Kievsky, L.E. Marcucci, and M. Viviani, *Phys. Rev. Lett.* **94**, 072303 (2005)

Within the **Madrid model** P_y seems unaffected by charge exchange to a large degree.

Medium Effect Increases with Proton Virtuality



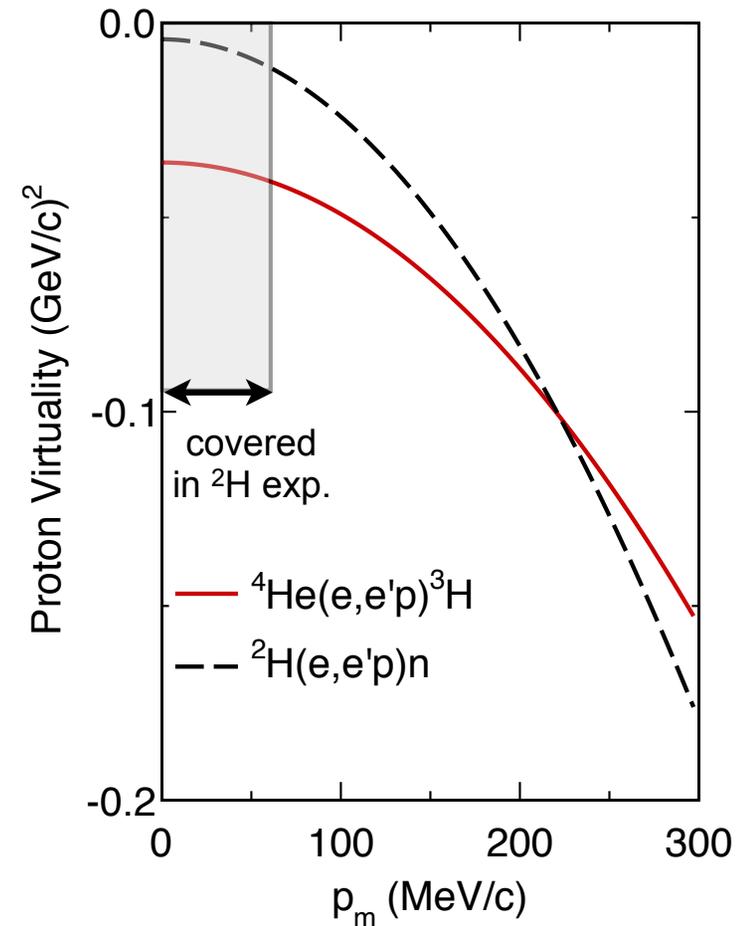
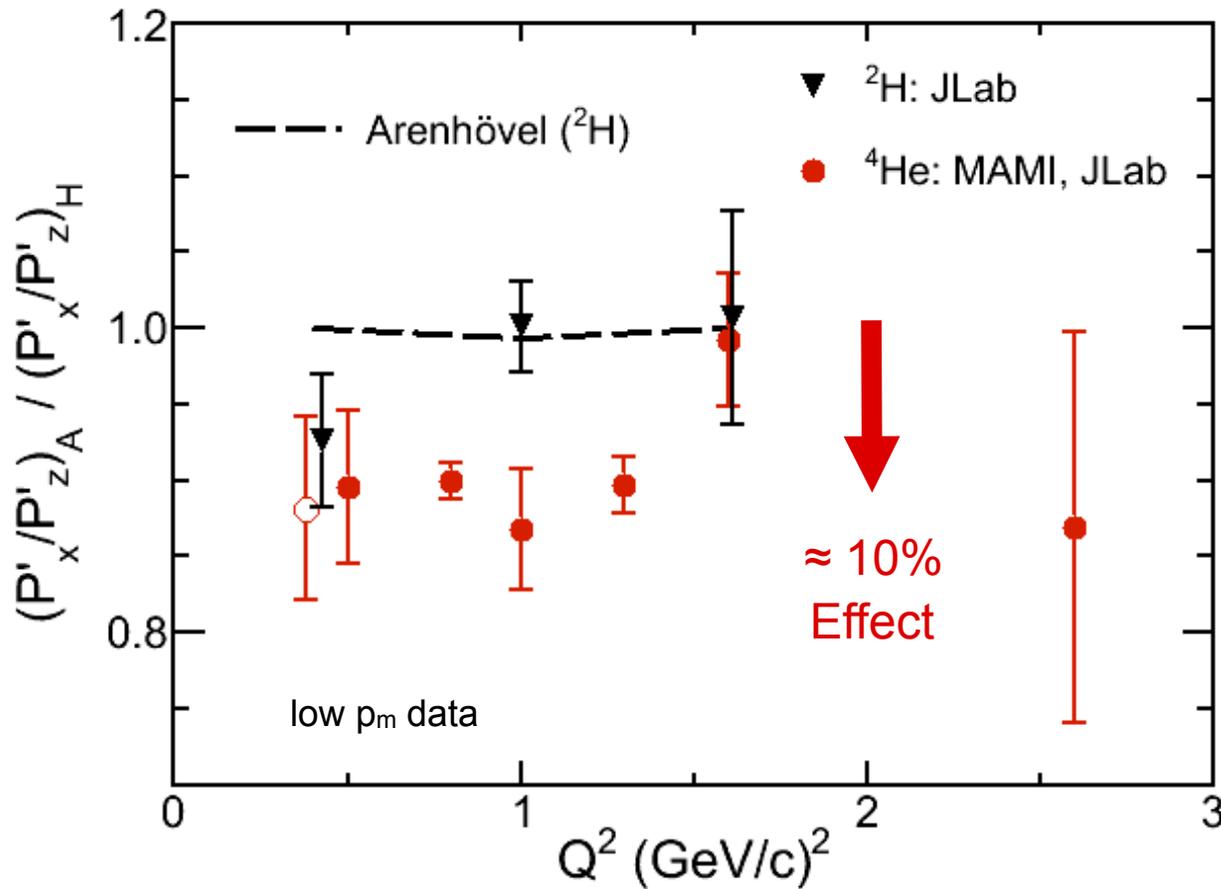
- $^4\text{He}(e,e'p)^3\text{H}$ polarization-transfer double-ratio data and calculations show **dependence on proton virtuality**

$$v = p^2 - m_p^2$$

with the trend of $R \approx 1$ for $p^2 = m_p^2$; as it should be.

- **Increase of medium effects with proton virtuality;** 4% to 10% over the range covered.

What Generates the Large Medium Effect?



- The nuclear **density** or
- the larger proton **virtuality** probed in the ^4He experiments?

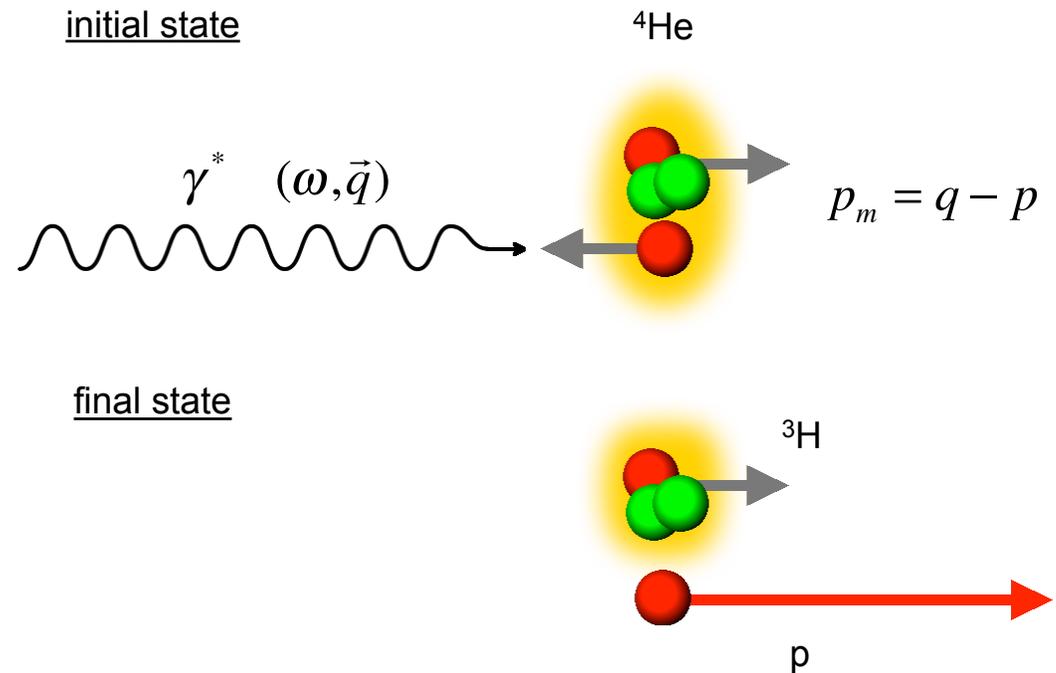
New experiment in Hall C will measure ^1H , ^2H , ^4He

- **Quasielastic** scattering
- **Parallel** kinematics
- $x > 1$, **spectator forward** to reduce inelastic channels (Δ production) and probe the genuine quasielastic channel*
- The off-shellness can be quantified as **nucleon virtuality**:

$$v = p^2 - m_p^2$$

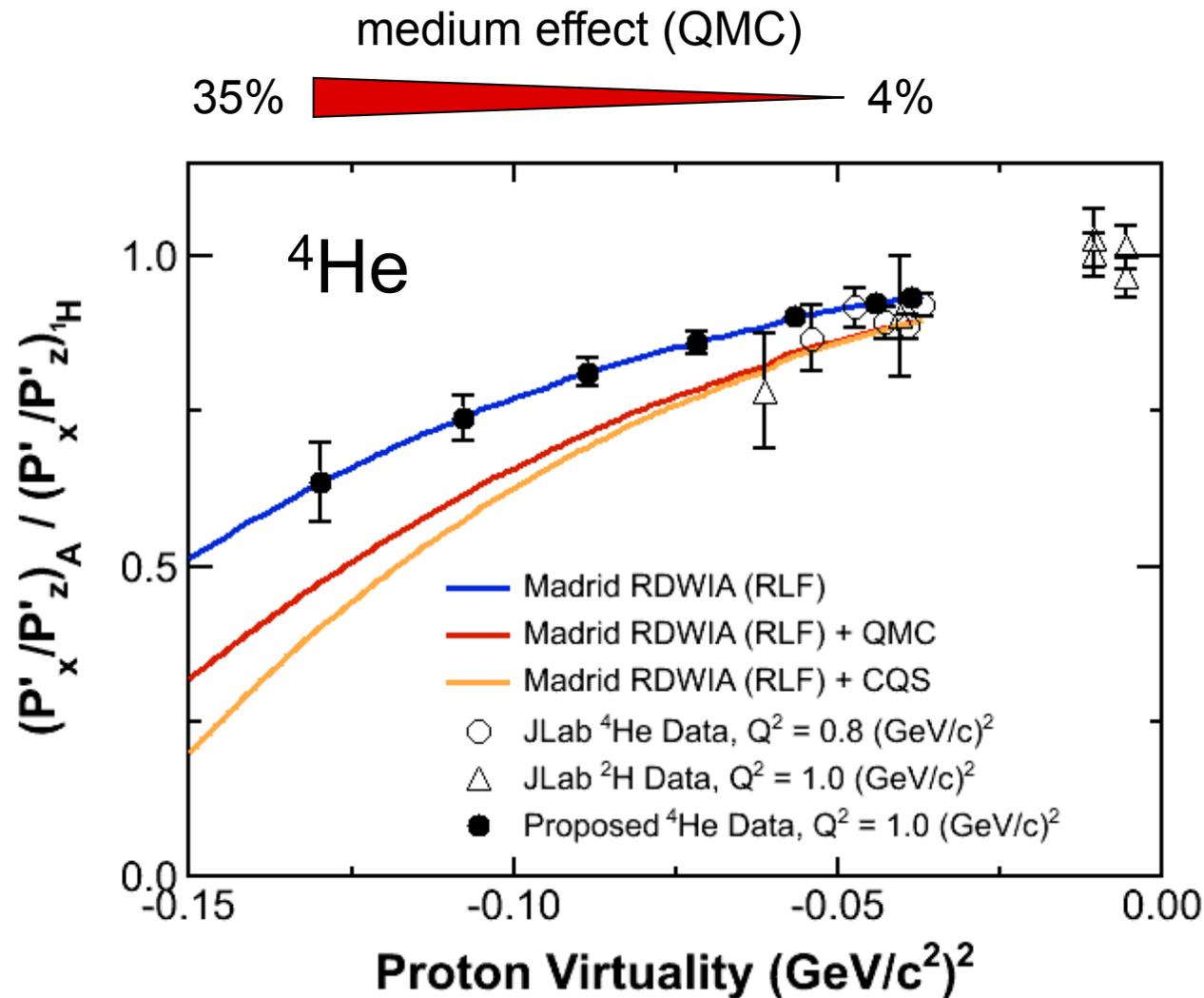
$$= \left(M_A - \sqrt{M_{A-1}^2 + \vec{p}_m^2} \right)^2 - \vec{p}_m^2 - m_p^2$$

*M. Sargsian, private communication
 C. Ciofi degli Atti, L.L. Frankfurt, L.P. Kaptari,
 M.I. Strikman, Phys. Rev. C **76**, 055206 (2007)



Q^2 (GeV/c) 2	p_m (MeV/c)	Targets
1.0	0, +140, +220	^4He , ^2H , ^1H
1.8	0	^4He , ^1H

1st Feature: Proton-virtuality coverage

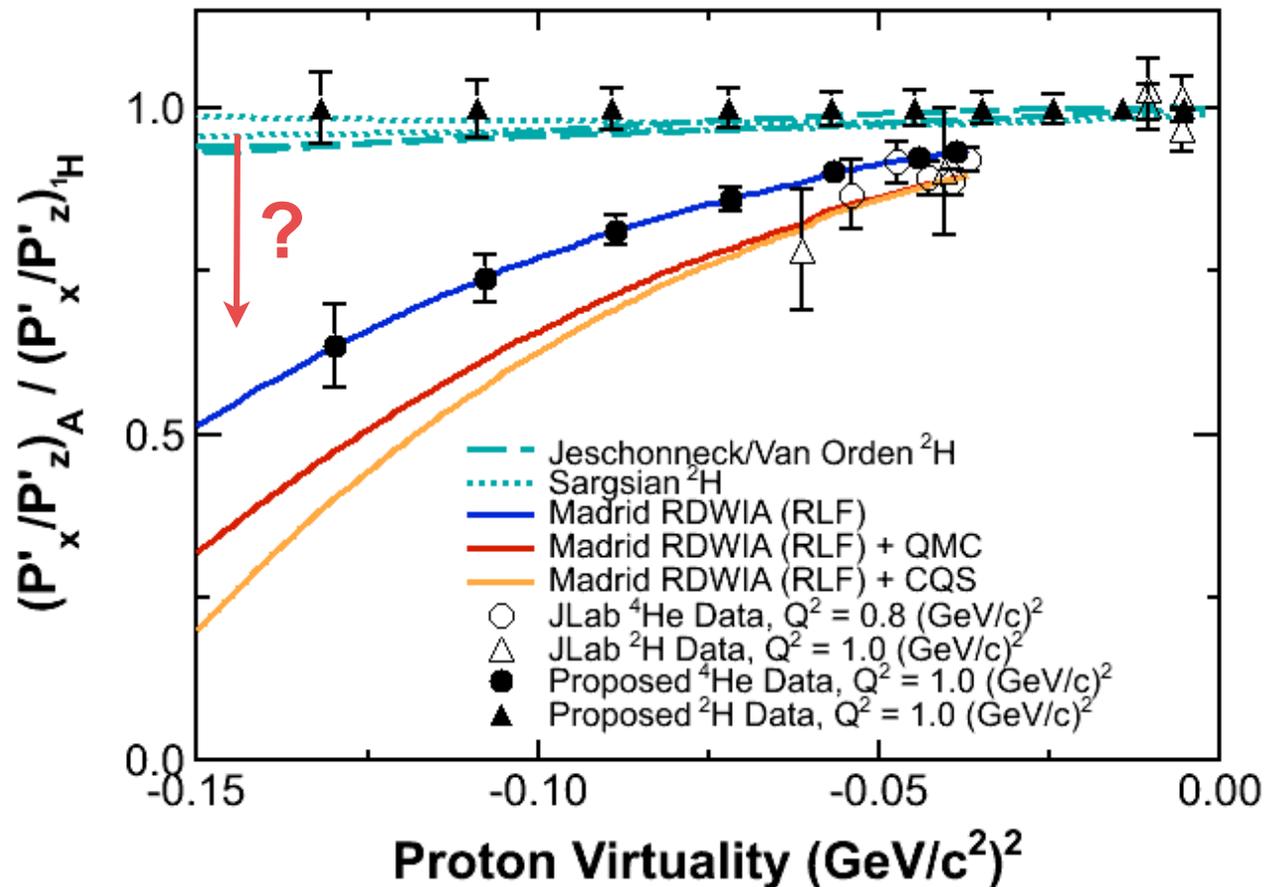


- **E11-002:**
 $Q^2 = 1.0 (\text{GeV}/c)^2$
 $p_m = 0, 140, 220 \text{ MeV}/c$
- Study the **expected strong dependence of medium effects on the momentum of the bound nucleon.**
- Previous ^2H data (\triangle) follow suggestively close the virtuality dependence of the ^4He data (\circ).

2nd Feature: ⁴He and ²H targets

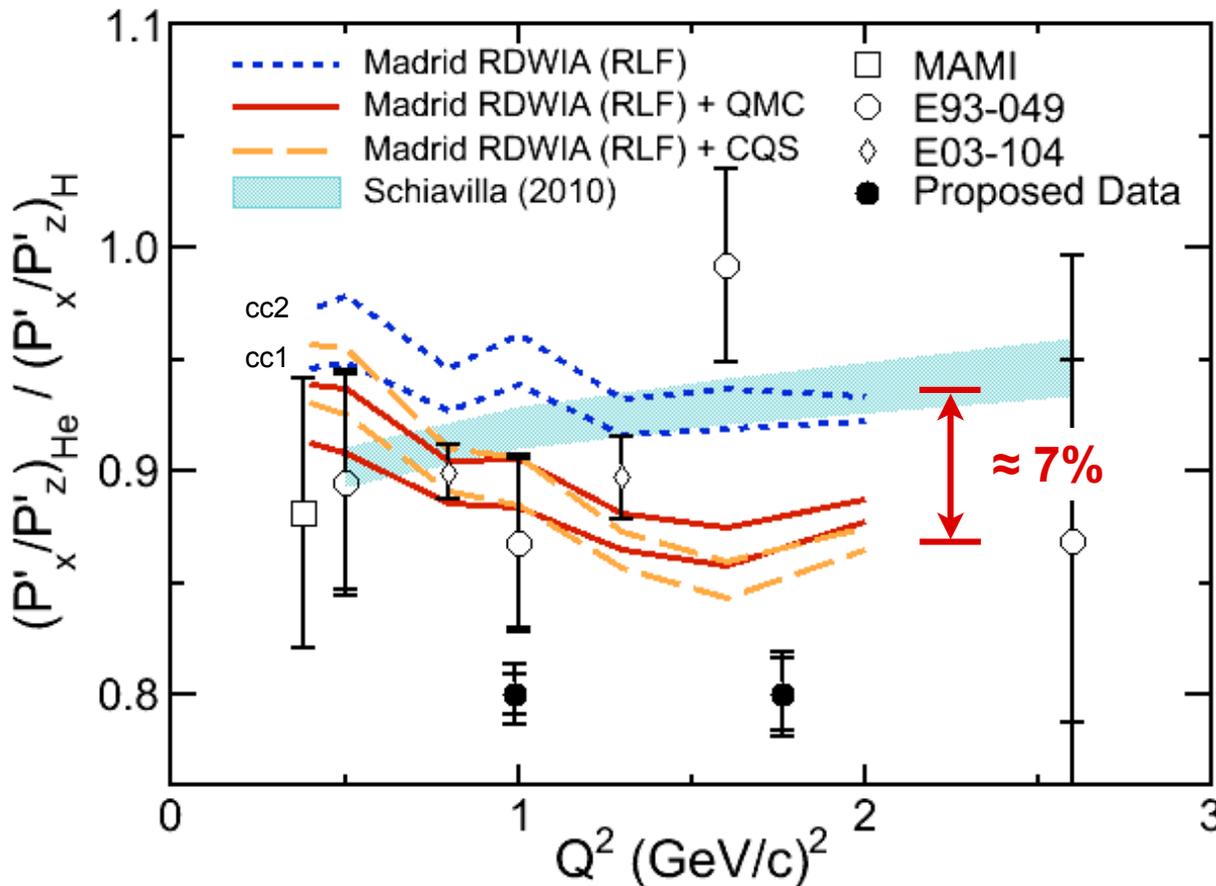
medium effect (QMC)

35%  4%



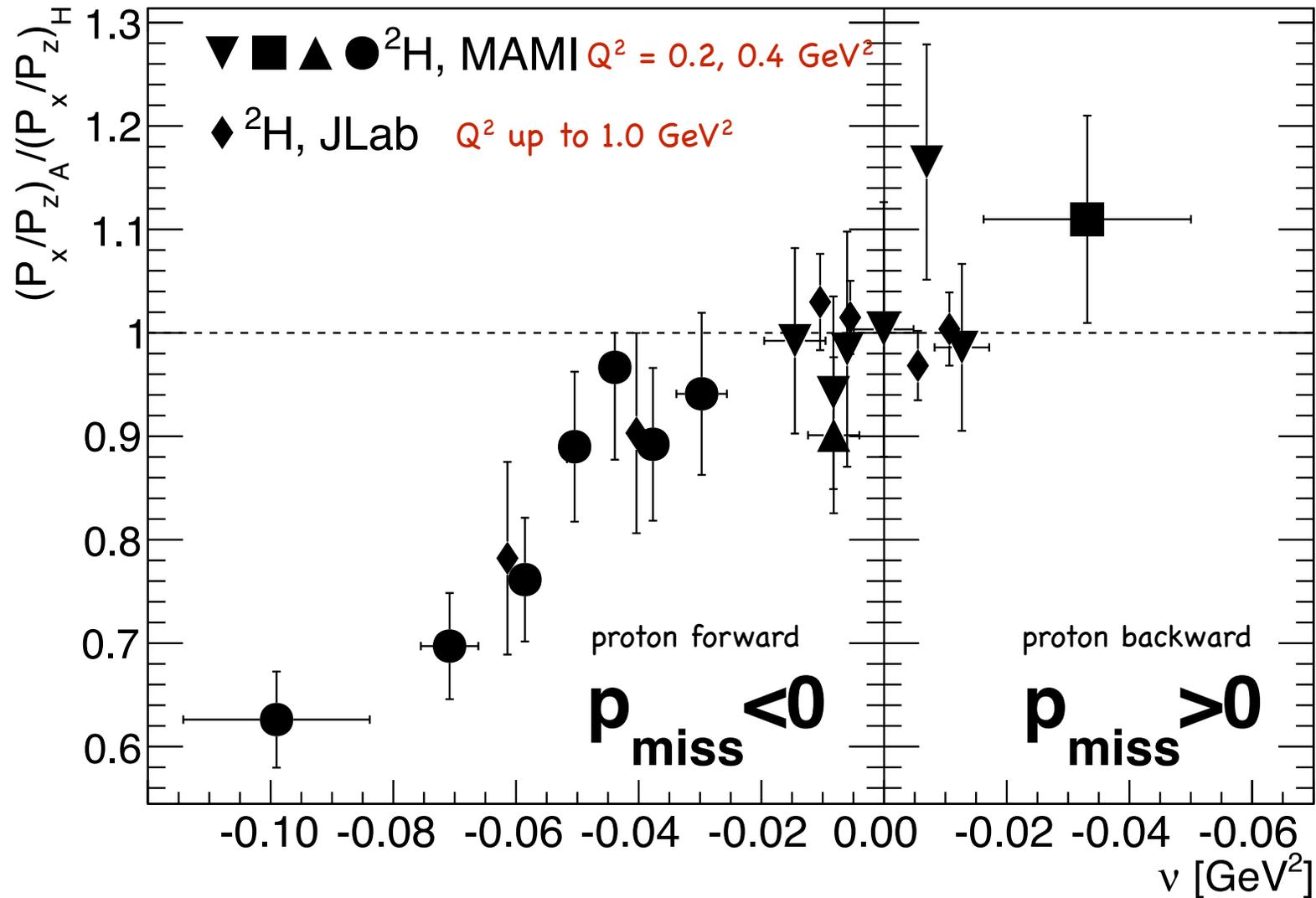
- **E11-002:**
Compare proton knock-out from dense and thin nuclei: ${}^4\text{He}(e,e'p){}^3\text{H}$ and ${}^2\text{H}(e,e'p)n$
- Modern, rigorous ${}^2\text{H}(e,e'p)n$ calculations show reaction-dynamics effects and FSI will change the ratio up to 5% (maximum 8%) in this kinematics
- Any **larger effects** (35%?) should be attributed to something else ...

3rd Feature: High- Q^2 point



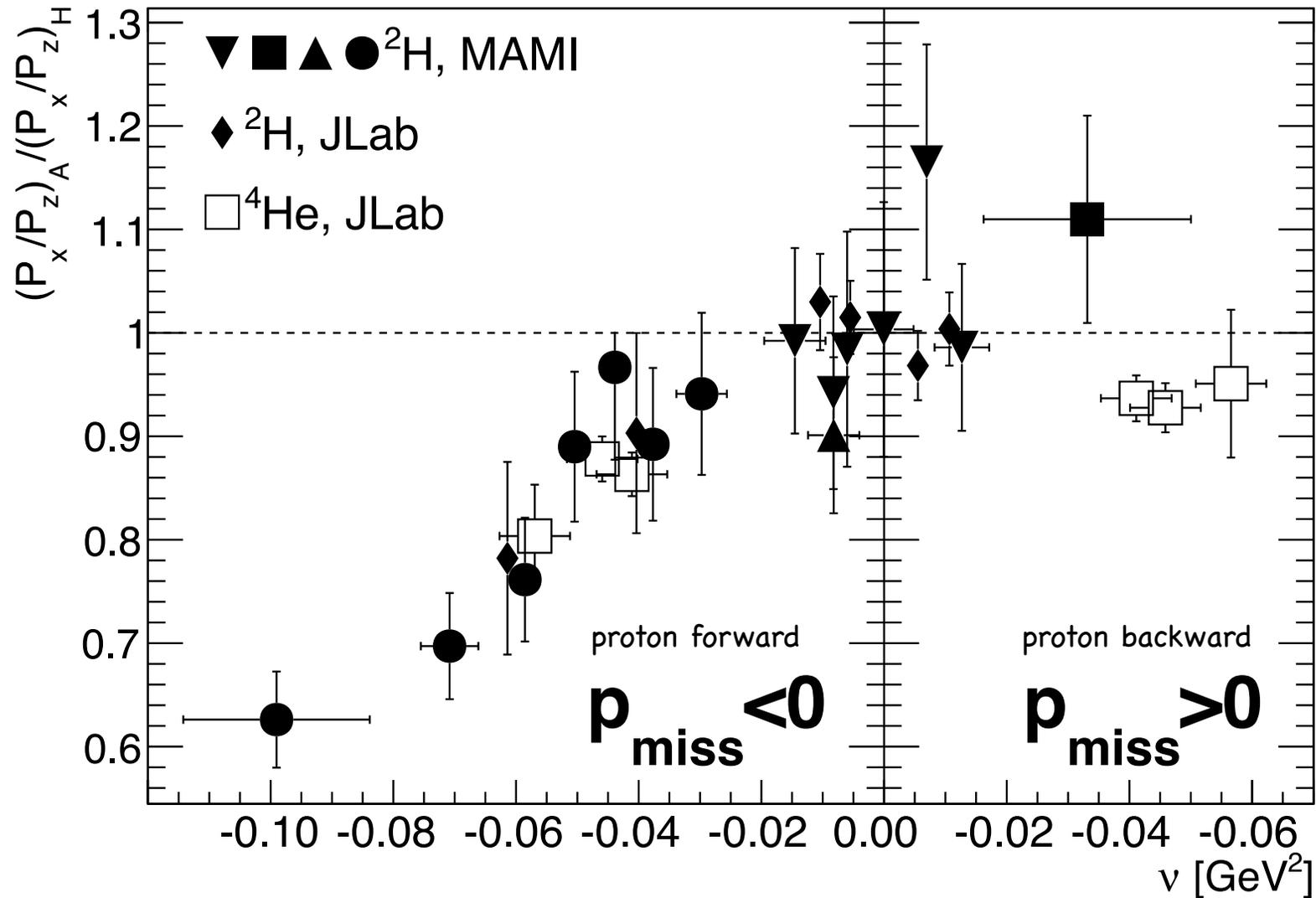
- Polarization-transfer data effectively described by **in-medium electromagnetic form factors** or **charge-exchange FSI**.
- For $Q^2 \geq 1.3$ (GeV/c)² **Madrid RDWIA** and **Schiavilla (2010)** results seem to agree.
- Additional data needed
 - **E11-002** will measure one new high-precision data point of the ⁴He polarization-transfer double ratio at $Q^2 = 1.8$ (GeV/c)².
 - Will it be **reduced by 7%** with respect to **Madrid RDWIA/Schiavilla**?

New MAMI Data: ^2H data virtuality dependent



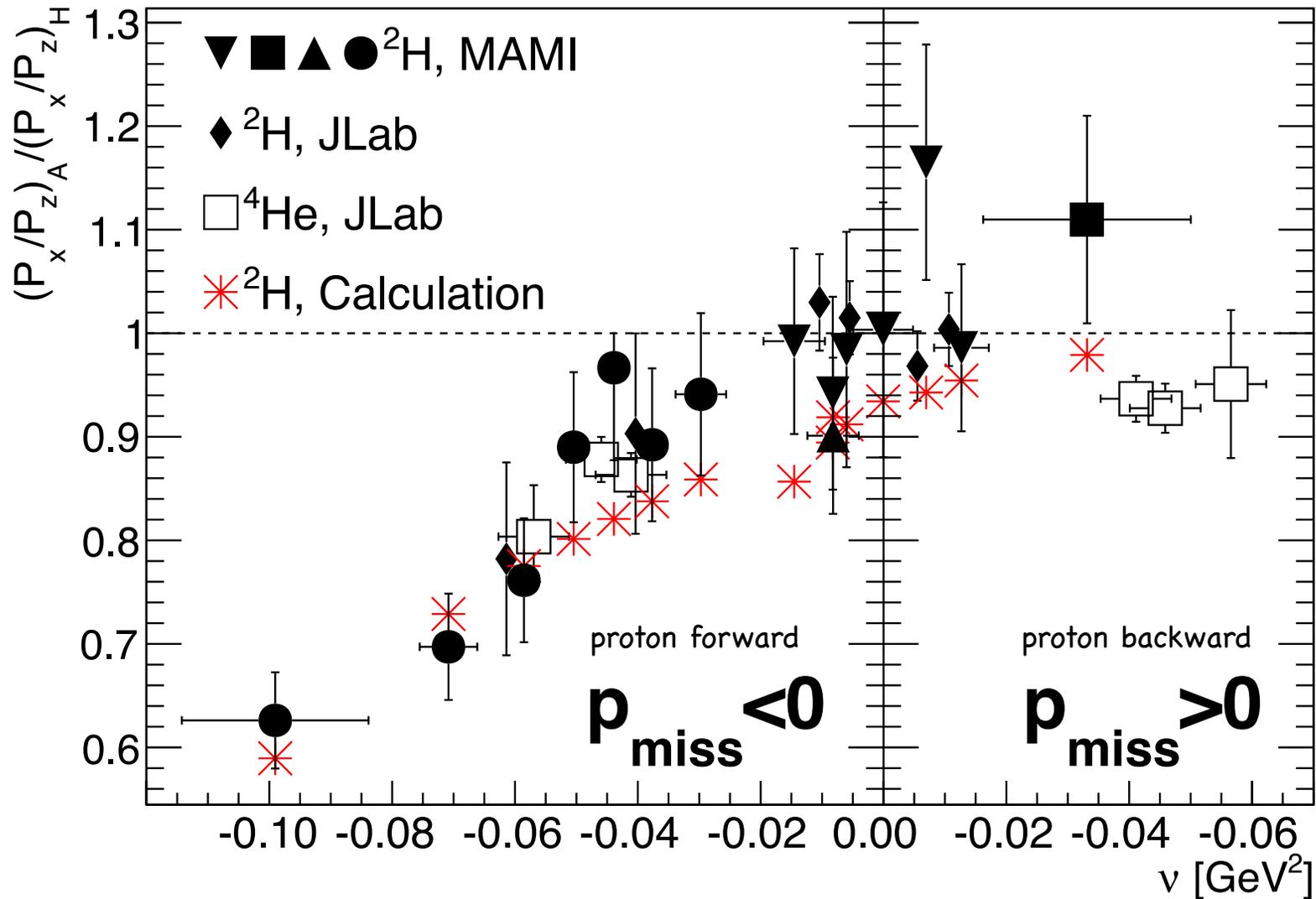
No significant Q^2 dependence

^2H data agree with ^4He data



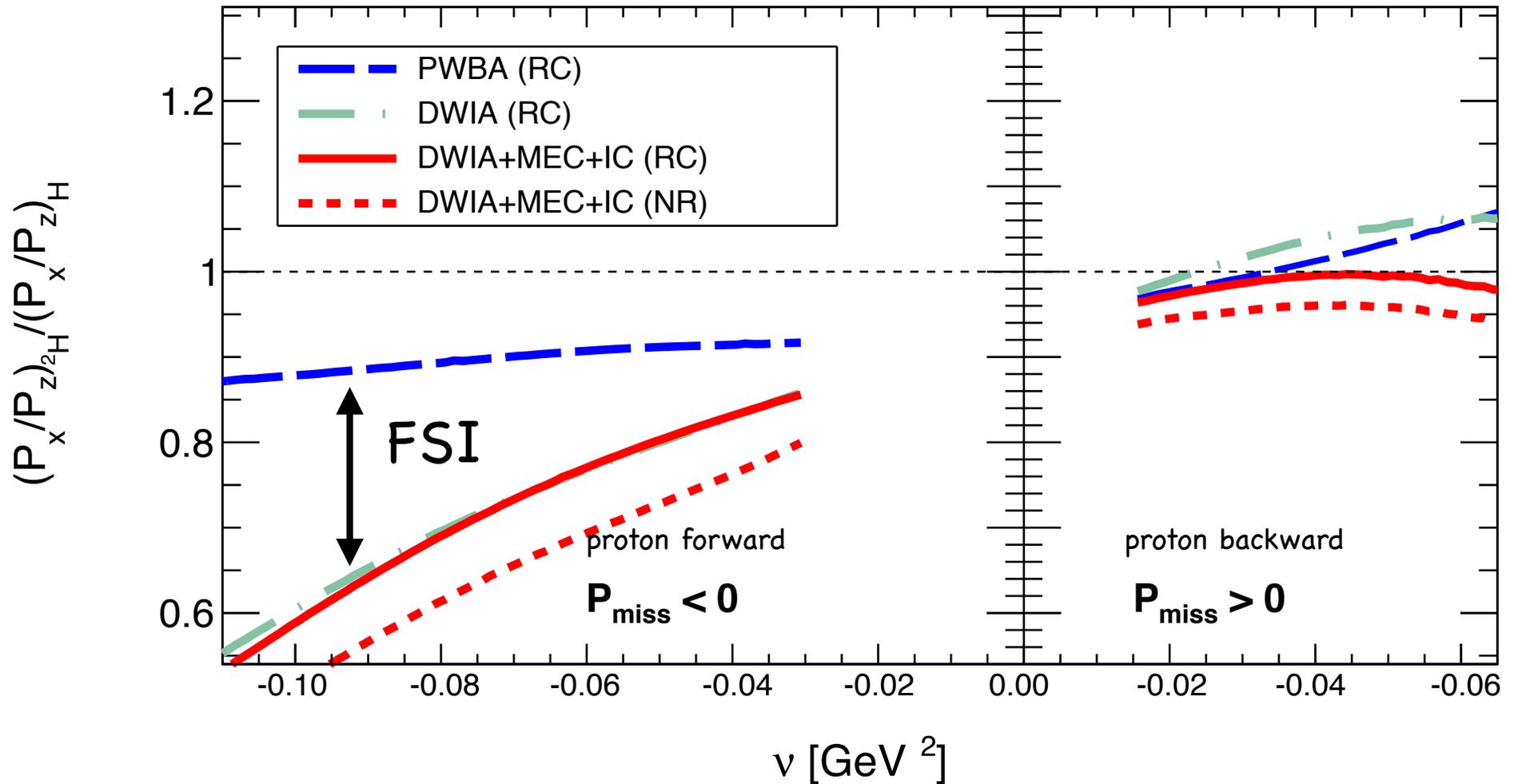
Results do not seem to depend on the nuclear density.

Model calculations on average 10% low



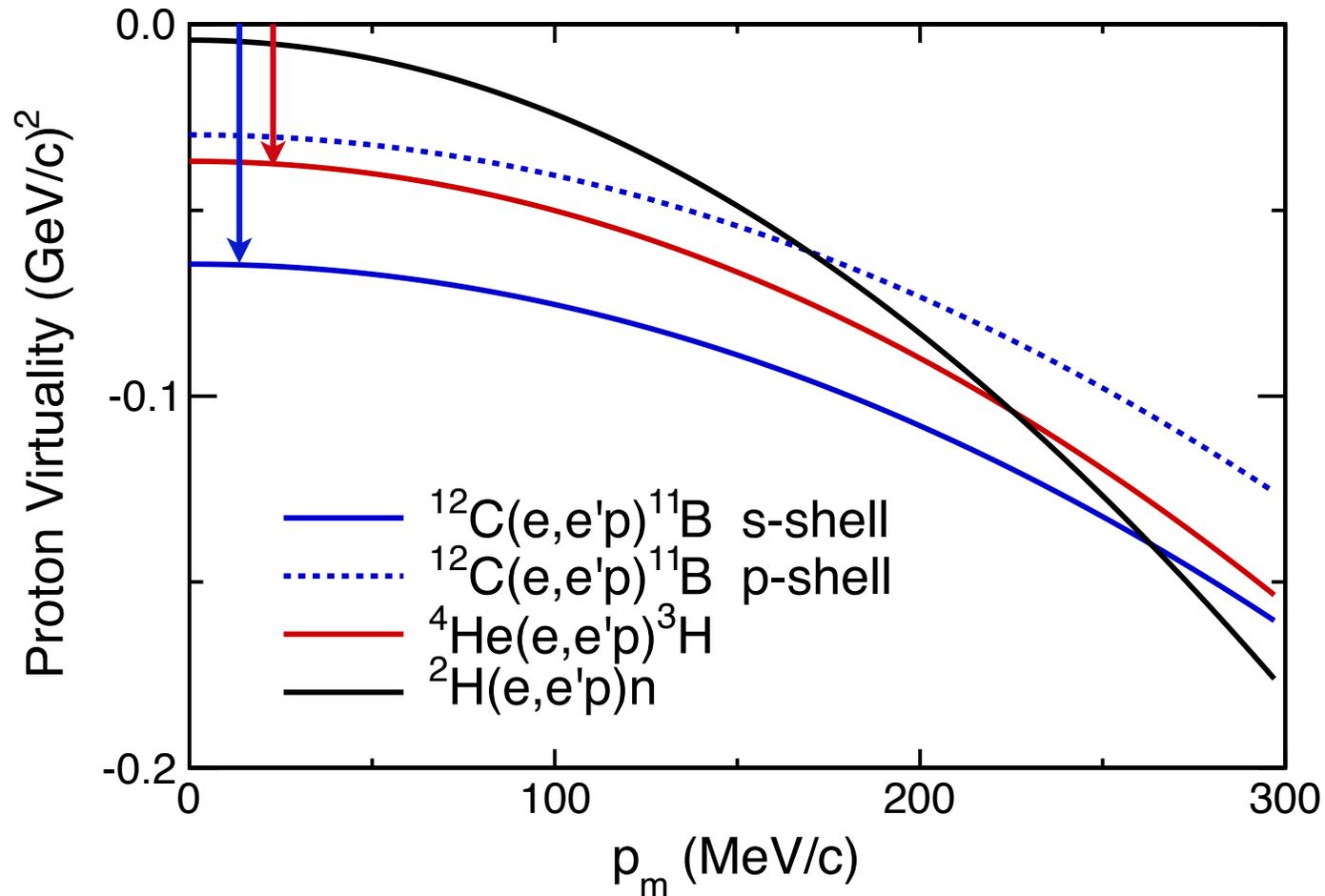
No need for medium-modified form factors, but certainly not excluded.

Results of H. Arenhövel calculations



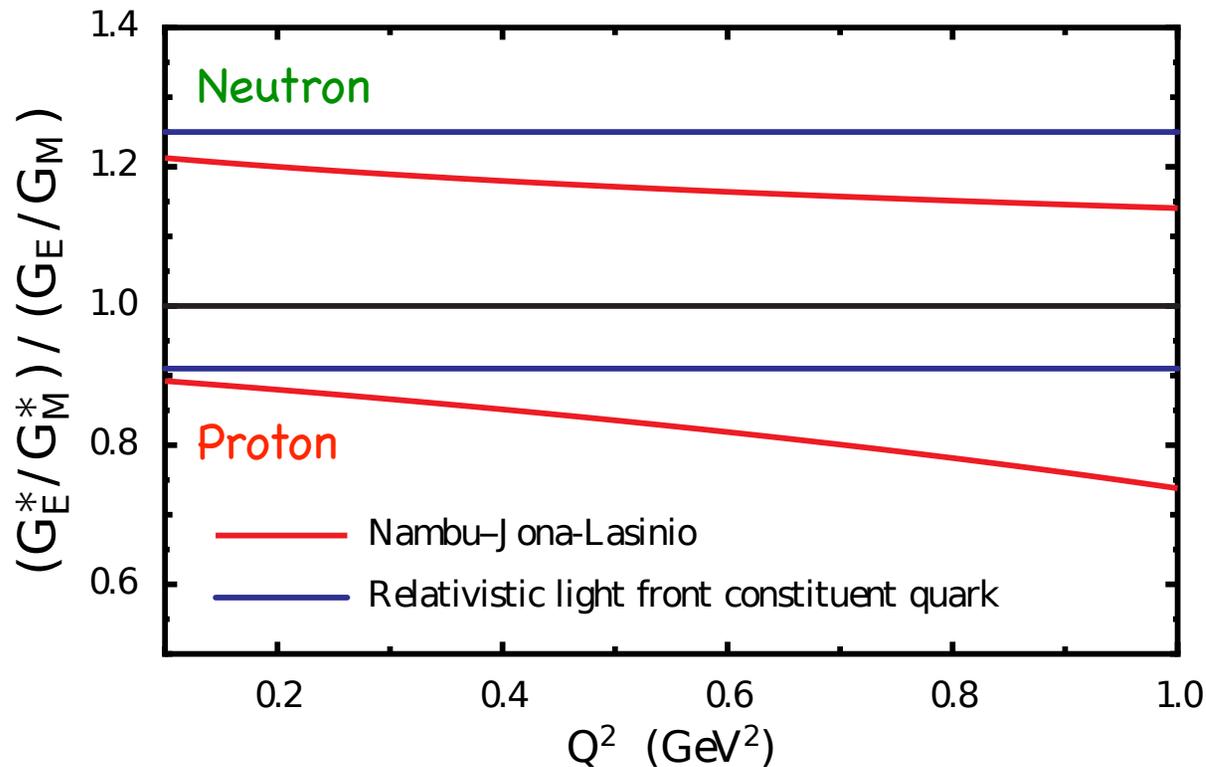
Final-state interactions are the major medium effect in the calculation.
 Medium modifications of the proton FF are expected to be small at the MAMI Q^2 .

Measurement of the $^{12}\text{C}(e,e'p)$ Reaction



- S-shell knockout in the $^{12}\text{C}(e,e'p)^{11}\text{B}$ reaction allows probing medium modifications of the P'_x/P'_z ratio at high proton virtualities.

Neutron in the Nuclear Medium



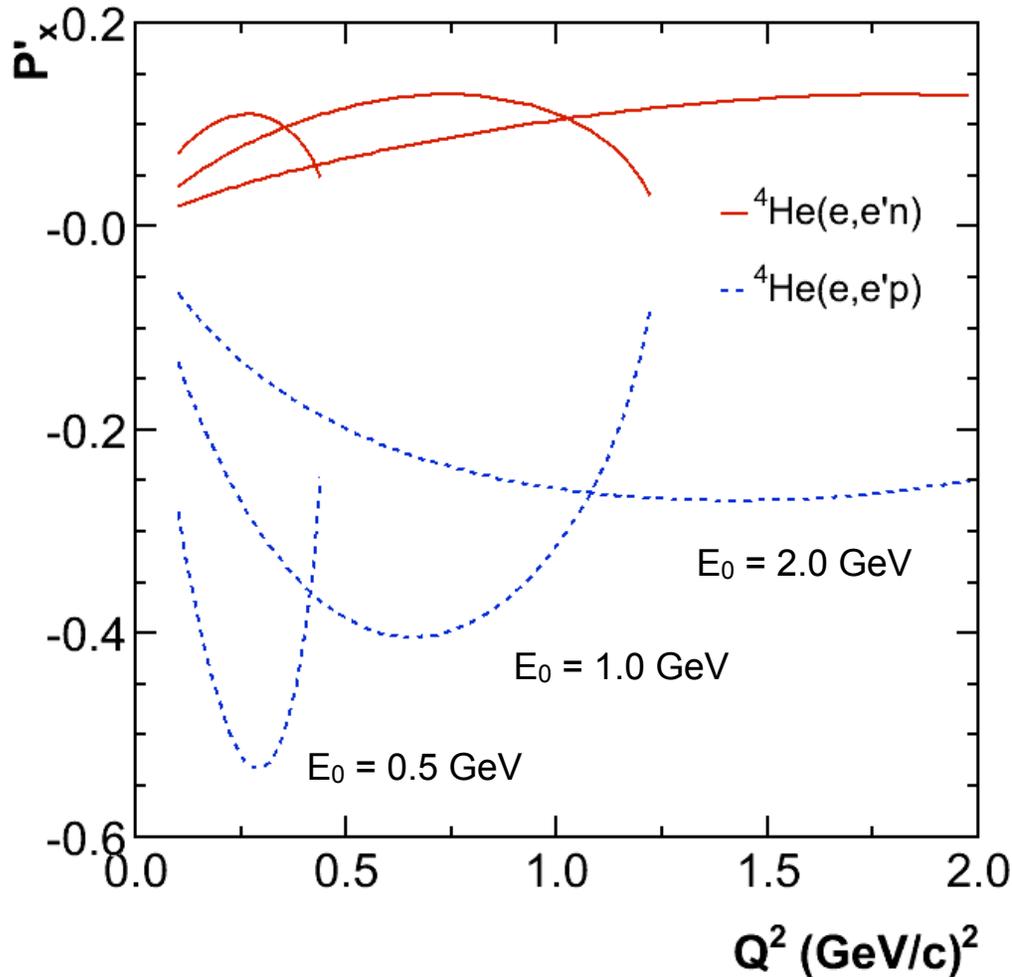
Neutron:
 $\approx +20\%$

Proton:
 $\approx -10\%$

- Different models for medium modification all give same result.
- Effect on **neutron** form factor ratio **very different** from the **proton**!
- ${}^4\text{He}(e,e'n){}^3\text{He}$: $G_E^n \approx 0$; very difficult measurement.

$$\frac{G_{En}}{G_{Mn}} = -\frac{P'_x (E_i + E_f)}{P'_z 2m} \tan \frac{\theta_e}{2}$$

${}^4\text{He}(e,e'n){}^3\text{He}$: Challenges and Choice of Q^2



$$P'_x = -2\sqrt{\tau(1+\tau)} \frac{\frac{G_E}{G_M}}{\left(\frac{G_E}{G_M}\right)^2 + \frac{\tau}{\epsilon}} \tan \frac{\theta_e}{2}$$

- Measure P'_x, P'_z to study possible neutron medium modifications
- $Q^2 = 0.1 \text{ (GeV/c)}^2$ - Theory calculation* best at low energy
- $Q^2 = 0.4 \text{ (GeV/c)}^2$ - Highest sensitivity to changes in magnetic FF
- $Q^2 = 0.8 \text{ (GeV/c)}^2, 1.3 \text{ (GeV/c)}^2$ - Direct comparison with $(e,e'p)$ results
- P_y in ${}^4\text{He}(e,e'n)$ could also provide crucial constraints on charge-exchange FSI

MAMI ?

JLab ?

*S. Bacca, N. Barnea, W. Leidemann, and G. Orlandini, PRL **102**, 162501 (2009)
 JLab LOI 10-007: G. Ron, D. Higinbotham, R. Gilman, S. Strauch, J. Lichtenstadt

Coulomb Sum Rule in quasi-elastic $A(e, e')$

$$S_L(|\mathbf{q}|) = \int_{\omega^+}^{|\mathbf{q}|} d\omega \frac{R_L(\omega, |\mathbf{q}|)}{ZG_{Ep}^2(Q^2) + NG_{En}^2(Q^2)}$$

Nonrelativistic expectation: S_L should approach unity for $|\mathbf{q}|$ much greater than the Fermi momentum.

Experimental findings controversial:

- ▶ No quenching in the data observed

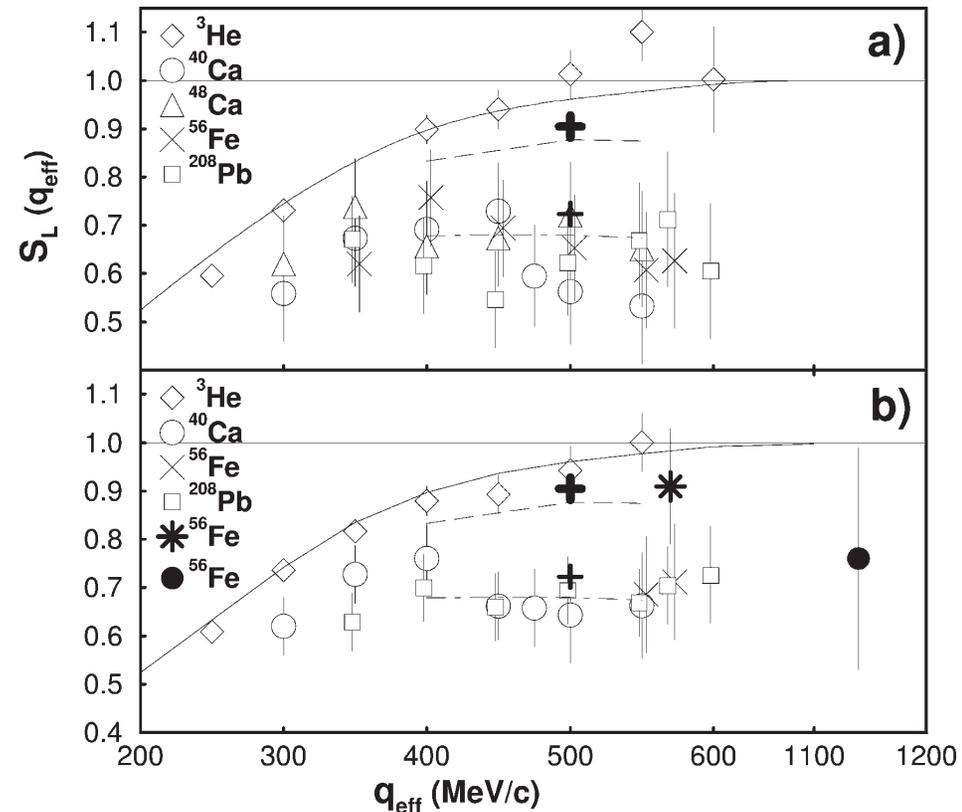
J. Jourdan, Nucl. Phys. A 603, 117 (1996)

- ▶ Quenching of S_L is experimentally established

J. Morgenstern, Z.-E. Meziani, Phys. Lett. B 515, 269 (2001)

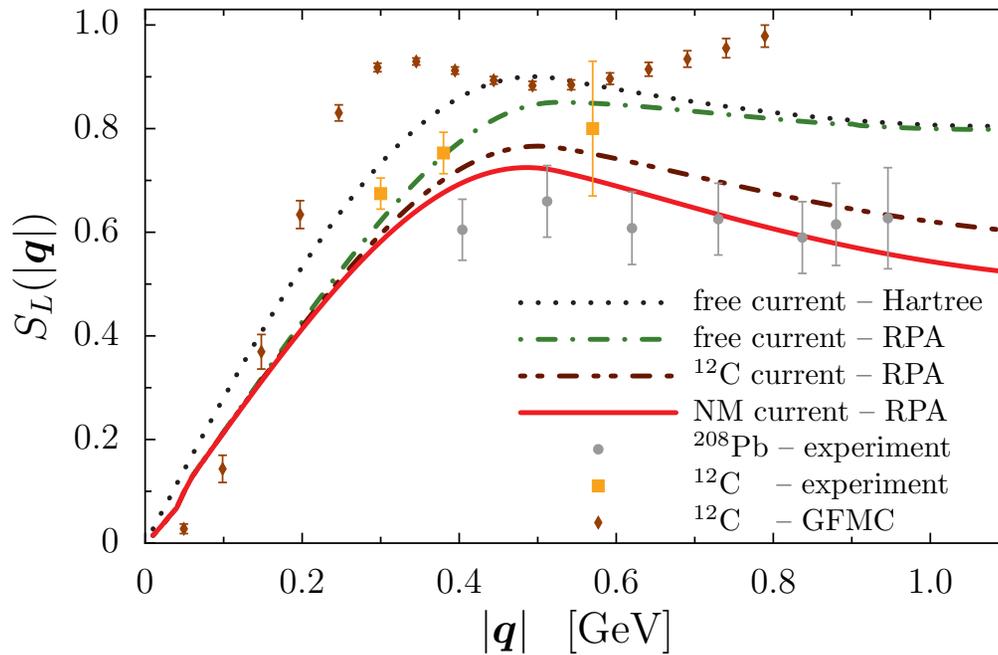
- ▶ Good agreement between theory and experiment for ${}^4\text{He}$ when using free-nucleon form factors

J. Carlson, J. Jourdan, R. Schiavilla, and I. Sick, Phys. Lett. B 553, 191 (2003)



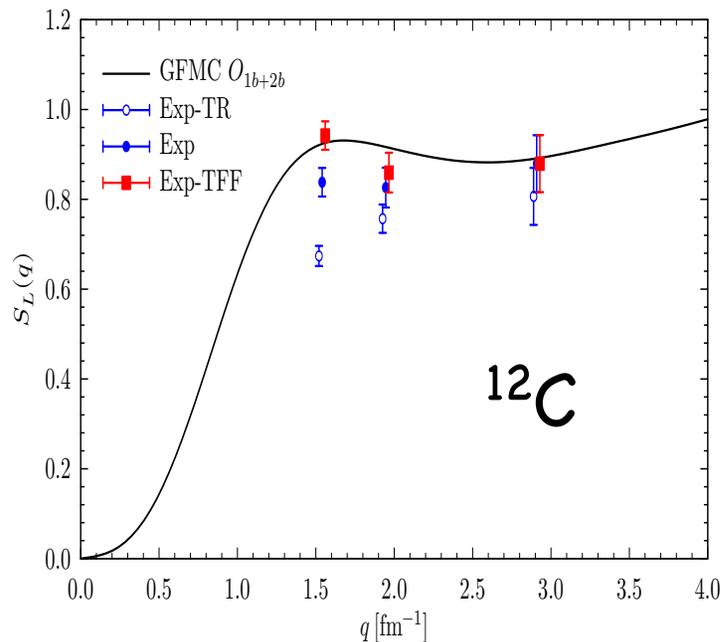
J. Morgenstern, Z.-E. Meziani,
Phys. Lett. B 515, 269 (2001)

Very different recent interpretations



“The observed quenching is directly associated with a softer F_{1p} in medium.”

Ian C. Cloët, Wolfgang Bentz, Anthony W. Thomas, *Phys. Phys. Rev. Lett.* **116**, 032701 (2016)



“The so-called quenching ... emerges in this study as a result of initial-state correlations and final-state interactions.”

A. Lovato, S. Gandolfi, J. Carlson, Steven C. Pieper, R. Schiavilla, *Phys. Rev. Lett.* **117**, 082501 (2016)

New Data are coming from Hall A E05-110

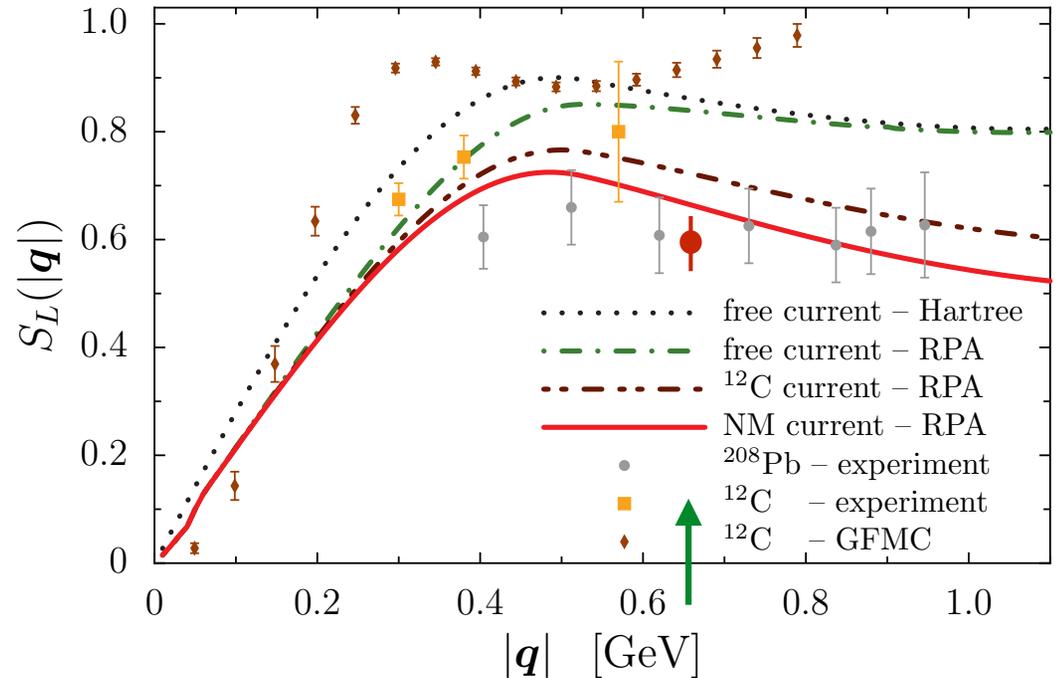
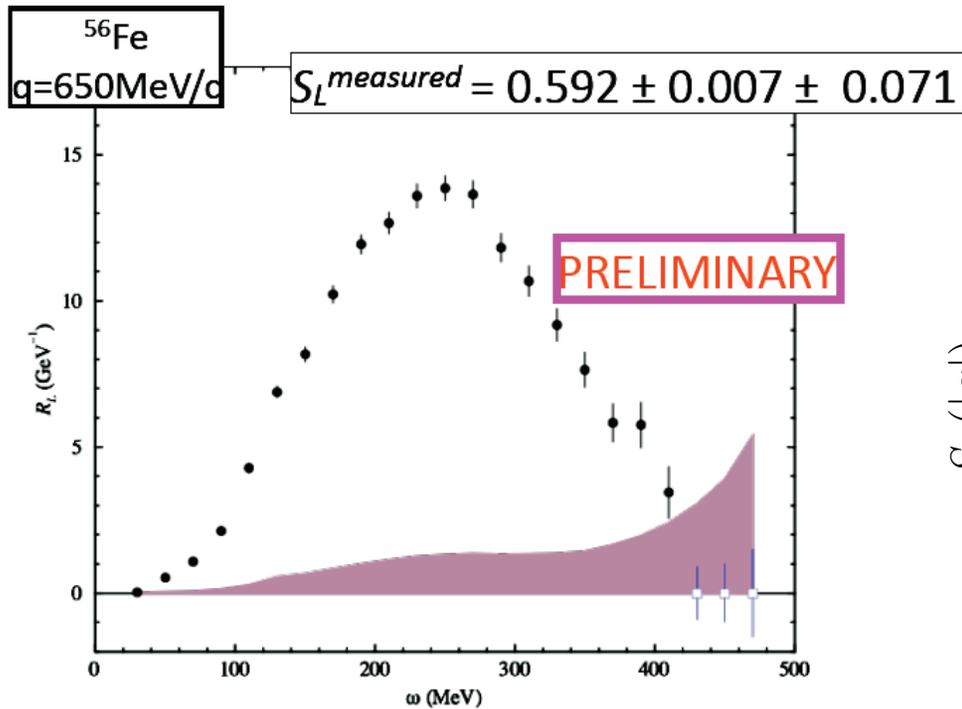


Figure from M. Paolone, HALL A/C SUMMER COLLABORATION MEETING 2016

- Four nuclei: ^4He , ^{12}C , ^{56}Fe , ^{256}Pb
- high momentum: $q = 650 \text{ MeV}/c$
- “Final results are just around the corner”

Future Steps

$$A(e, e')$$

- Finalize results from Hall A Coulomb Sum Rule experiment

$$A(e, e', \vec{p})$$

- Finalize MAMI ^2H and ^{12}C data analysis
- Re-defend Hall C ^4He , ^2H , ^1H polarization-transfer experiment
- Propose to include ^{12}C in Hall C experiment?

$$A(e, e', \vec{n})$$

- at MAMI?
- at JLab?