

Vulnerability Analysis Of Optimal Power Flow Problem Under Cyber-Physical Security Attacks

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Vulnerable Electricity Networks: Key issues

- ▶ In addition to reliability failures, power grids are increasingly vulnerable to cyber-physical security (CPS) attacks
- ▶ Such CPS attacks can be modeled as bilevel optimization problems
- ▶ We present two CPS attack scenarios
 - ▶ Dynamic Line Rating (DLR) Manipulation
 - ▶ Distributed Energy Resource (DER) disruption
- ▶ Structural insights allow for greedy and efficient (approximate) algorithms

Two motivating attack models



California Sniper Attack



Ukraine Cyber Attack

Related work

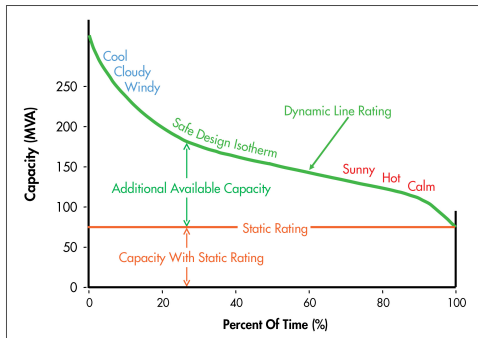
- ▶ A. Verma, D. Bienstock: N-k vulnerability problem
 - ▶ Attacker disrupts generators or manipulates line impedances to maximimize load shedding
 - ▶ DC Power Flow approximation
- ▶ S.Wright et al.: Vulnerability Analysis of Power Systems
 - ▶ Attacker increases the line impedances to maximimize
 - ▶ Loss of voltage regulation, OR Load shedding
 - ▶ Use both active and reactive power
- ▶ R. Baldick, K. Wood, D. Bienstock: Network Interdiction, Cascades

Use bilevel optimization models with outer problem as attack model, and the inner problem being optimal power flow **(OPF) problem**

- ▶ Ensure demand is fully met while minimizing costs subject to generator, capacity, supply-demand balance, power flow constraints

DLR Manipulations in Transmission Networks

Figure 1: Tapping into existing capacity above the static rating



Source: Valley Group

Line capacity violations have caused cascading failures in the past, e.g., July 2012 blackout in India

Bilevel problem (Stackelberg game)

- ▶ **Leader:** Attacker compromises the DLRs using false data injection attack;
- ▶ **Follower:** Defender's economic dispatch solution is optimal for new *manipulated* system, but possibly infeasible for the old *actual* system.

Problem statement:

- ▶ Determine an optimal **attack plan** to minimize line rating violations

Solution Approaches

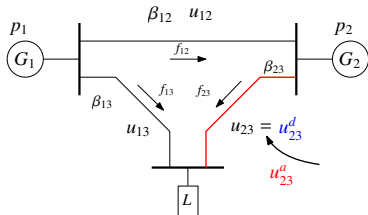
Benders Decomposition (Kevin Wood et al.)

- ▶ Alternately consider follower problem, with fixed attacker actions, and master problem with fixed defender actions
- ▶ Sequentially generate Benders cut for the Master Problem until zero optimality gap
- ▶ Results in systematic vertex enumeration of the inner problem

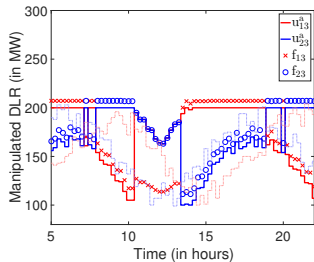
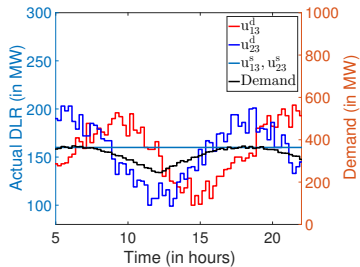
Kuhn-Tucker Single-level reformulation (Bard et al.)

- ▶ Apply KKT optimality conditions for the inner problem, and reformulate complementarity constraints
- ▶ Use Branch-n-Bound techniques to solve the resulting Mixed-Integer Linear Program (MILP)

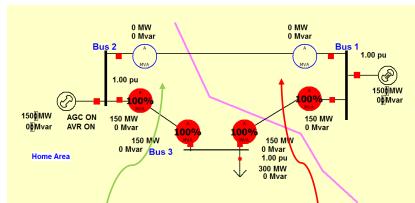
Insights



- ▶ Attacker strategy, by and large, exhibits a bang-bang policy
 - ▶ Some DLRs are set to maximum
 - ▶ Other DLRs are set to minimum (as long as feasible operating point exists)
- ▶ Similar results hold for larger (118 node) testcase



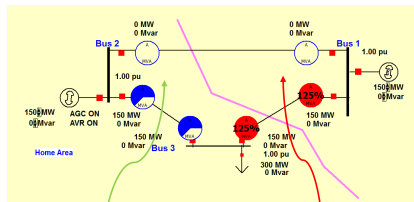
Implementation of attack in Powerworld simulator



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06410AF0 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
06410B00 00 00 00 00 00 00 00 00 01 00 00 00 00 00 00 00
06410B10 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
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06410850 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
06410860 00 00 00 00 00 00 00 00 00 01 00 00 00 00 00 00
06410870 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
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(c) Pre-attack system state (safe).



```
06410AE0 01 00 00 00 C0 65 79 09 00 00 00 00 00 00 00 00
06410AF0 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00 00
06410B00 00 00 00 00 00 00 00 00 01 00 00 00 00 00 00 00
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(d) Post-attack system state (unsafe).