

# Information Theory for Mobile Ad-Hoc Networks (ITMANET): *The FLoWS Project*

## Thrust 3 Intro: Application Metrics and Network Performance

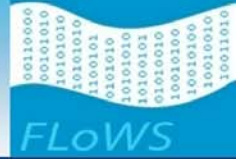
Asu Ozdaglar

Joint with D. Shah



- Objective:
  - Developing a framework for optimizing **heterogeneous and dynamically varying application metrics** and **ensuring efficient operation** of large-scale decentralized networks with uncertain capabilities and capacities
  - Providing an interface between application metrics and network capabilities
    - Focus on a direct involvement of the application in the network, defining services in terms of the **function** required rather than **rates** or other proxies
- **Application and Network Metrics:** utility functions of users-applications, distortion, delay, network stability, energy...
- **We envision a universal algorithmic architecture:**
  - Capable of balancing (or trading off) application requirements and network resources
  - Adaptable to variations on the network and user side
  - Operable in a decentralized manner, scalable
  - Robust against non-cooperative behavior

# Prior Work



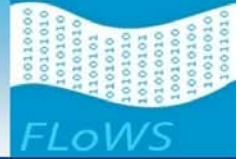
- Decoupled/layered approach to resource allocation
  - Highly suboptimal and inefficient
- More recent trend:
  - Formulate resource allocation problem as one optimization problem and use decompositions based on separable structure
  - This approach **fails for wireless networks** due to:
    - Need for distributed asynchronous implementations
    - Externalities/couplings that disturb separable structure
    - Stochastic elements
- No analysis of robustness against dynamic changes and noncooperative behavior and competition

# Intellectual Tools and Focus Areas



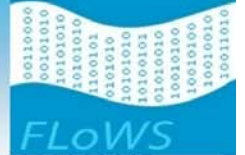
- Optimization and Control Theory
  - Decentralized algorithms robust against variations in network topology, channel characteristics, and capacities
  - Ensuring rapid convergence
  - Optimization for heterogeneous preferences
- Performance (stability) analysis of network algorithms
  - At micro-level: understanding queuing dynamics
  - At macro-level: understanding effect on flow-level network behavior
- Game Theory
  - Dealing with noncooperative strategic users
  - Dynamics and equilibrium

# Individual PI Presentations



- **Shah**, “Fundamental Performance Limits and Reality”
- **Meyn**, “Optimizing MaxWeight for Resource Allocation”
- **Boyd**, “Large Scale Network Utility Maximization”
- **Ozdaglar**, “Distributed Asynchronous Optimization Methods for General Performance Metrics”
- **Johari**, “Incomplete Information, Dynamics, and Wireless Games”

# Wireless networks: Algorithmic trade-off between Throughput and Delay



STATUS QUO

Among two important performance metrics of wireless networks, throughput and delay, only **throughput is well-understood** in terms of fundamental limits and algorithm design.

**Delay is far from being well-understood.**



NEW INSIGHTS

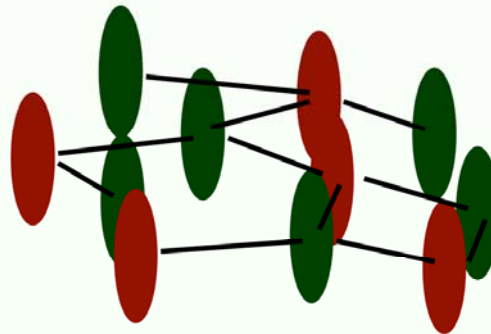
1. Arbitrary networks: High-throughput is **easy**, low delay is **hard**.
2. Practical networks: distributed high-throughput low delay is **possible**.



## ACHIEVEMENT DESCRIPTION

### MAIN RESULT:

1. High-throughput low delay algorithm for arbitrary wireless network is computationally intractable.
2. Wireless networks deployed in geographic area (in arbitrary manner) have high-throughput and low-delay algorithm distributed algorithms for scheduling and cross-layer design.



### HOW IT WORKS:

1. Intractability follows by identifying computational hardness in scheduling through a novel equivalence relation.
2. Geometry in wireless networks allows for simple, high-performance algorithm design.

### ASSUMPTIONS AND LIMITATIONS:

1. Wireless network with interference model.

END-OF-PHASE GOAL

1. Computational intractability of high throughput, low delay algorithm for wireless network under SINR model.
2. Simple algorithms for practical networks under SINR model.



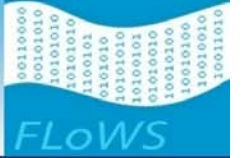
COMMUNITY CHALLENGE

**Computational intractability of information theoretic capacity achieving codes for wireless networks.**

Algorithmic limitations for wireless network

- Primary performance metric in a wireless network
  - Throughput and delay
  - Necessary for quality-of-service guarantee, buffer-design, etc.
  - Further, algorithm should be implementable (distributed)
- However, thus far most of the work has concentrated on designing throughput optimal algorithms
  - Low delay algorithm design is a lot harder
  - *An analogy*: being ahead of all in a marathon throughout the race (low delay) versus completing the race first (high throughput)
- One of the main reason for such status
  - Lack of good tools for delay analysis
  - Hence lack of insight about what causes high delay
  - As well as inability to understand finer throughput delay tradeoff

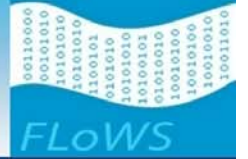
# Summary of Results



- First, we establish that
  - It is possible to have very simple, distributed throughput optimal algorithm for any network
    - throughput is easy
- To understand interaction with throughput and delay
  - We introduce new tools from computational complexity
  - We establish computational impossibility of designing high throughput, low delay algorithm for arbitrary network
- However, the relevant question is: are practical networks hard ?
  - We obtain novel algorithms using graph theoretic properties of practical networks
    - these are simple, distributed; throughput and delay optimal



# End-of-Phase Goals



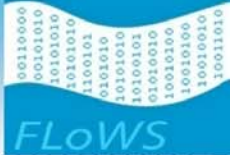
## Goal 1.

Establish that it is not possible to design computationally efficient high throughput and low delay algorithm for wireless network under physical (SINR) model

## Goal 2.

Design simple and distributed throughput-delay optimal algorithm for practical wireless network topologies under physical model

# Wireless networks: Algorithmic trade-off between Throughput and Delay



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NEW INSIGHTS

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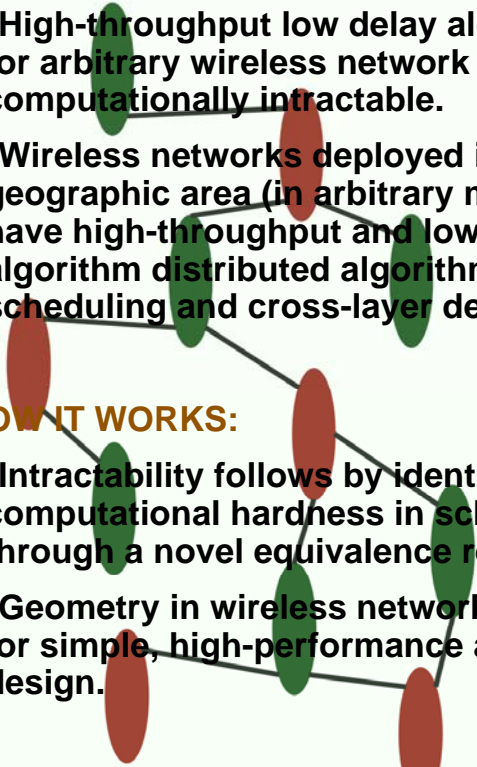
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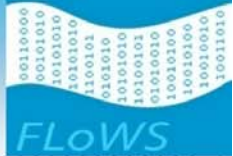


COMMUNITY CHALLENGE

**Computational intractability of information theoretic capacity achieving codes for wireless networks.**

Algorithmic limitations for wireless network

# Optimizing MaxWeight



STATUS QUO

What is the state of the art and what are its limitations?

Static routing: *ignores dynamics*

MW routing: *inflexible with respect to performance improvement*

Subramanian & Leigh 2007: *MW can be irrational*



NEW INSIGHTS

What are the key new insights?

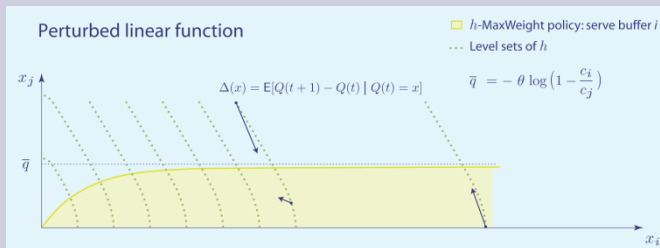
MW = *Myopic* for a fluid model. Many such policies share the desirable properties of MW



## ACHIEVEMENT DESCRIPTION

### MAIN RESULT:

- Geometric characterization of myopic policy with optimal throughput
- Perturbation technique to generate functions with appropriate geometry
- Application to policy synthesis for approximately optimal performance in heavy traffic



### HOW IT WORKS:

- Key analytical tool is Lyapunov theory for Markov processes
- For approximate optimality, *workload relaxation*
- Relaxation also provides tool for visualization of high dimensional dynamics. Optimal solutions evolve in region containing *monotone region* for the effective cost.

END-OF-PHASE GOAL



- Decentralized implementation: Policy can be designed to use available information.
- Adaptation - on-line policy improvement
- Full analysis of multiple bottlenecks
- Integration with Network Coding projects: *Can we code around network hot-spots?*



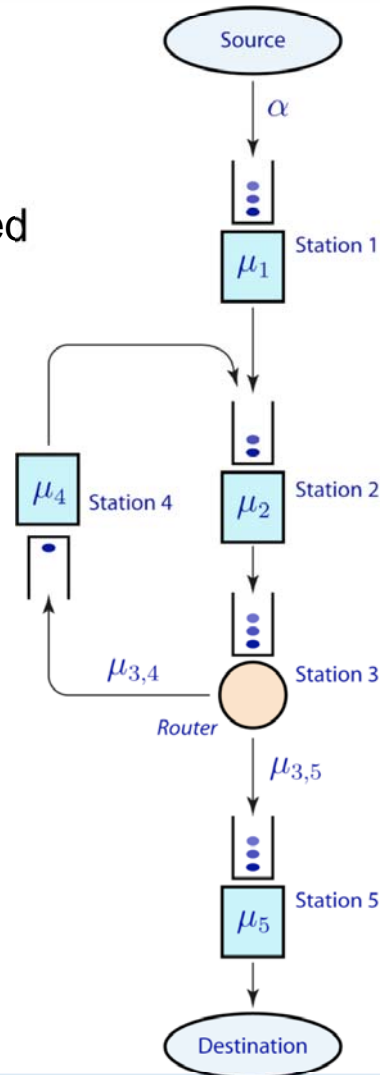
COMMUNITY CHALLENGE

- Un-consummated union challenge: Integrate coding and resource allocation methodology
- Generally, solutions to complex decision problems should offer insight

# MaxWeight: What requires optimizing?

Routing requires *information*.  
In the MaxWeight policy, this information is obtained through queue length values. This can lead to irrational behavior when information is scarce.

Example (Subramanian and Leith, 2007, submitted).  
*MaxWeight or Backpressure routing will send packets upstream!*



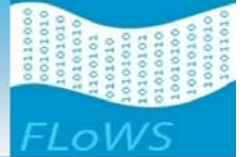
Questions addressed:

- Why does MW work?
- How can it be generalized and improved?
- Performance evaluation?

Analysis based on *new geometric insight*, and the *workload relaxation*

MaxWeight can be improved once it is better understood

# Optimizing MaxWeight

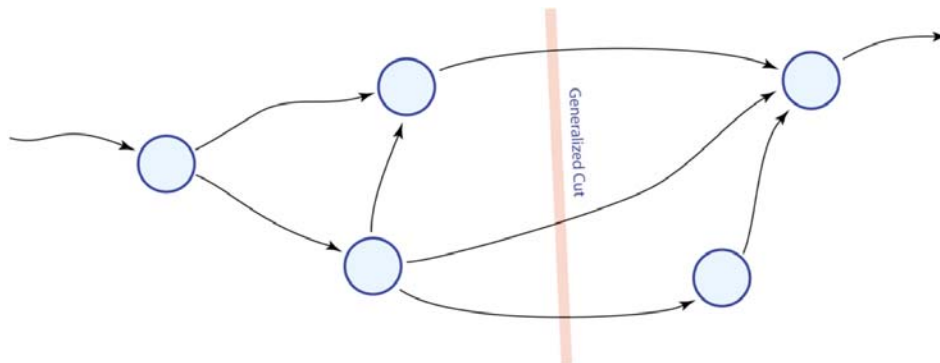


- Perturbation technique: If  $h_0$  is any monotone convex function

$$h(x) = h_0(\tilde{x}), \quad \tilde{x}_i = x_i + \theta^{-1}(e^{-\theta x_i} - 1)$$

The function  $h$  serves as a Lyapunov function in a stability analysis  
Chosen for mathematical elegance - many other possibilities!

- Optimization: Generalized min-cut to construct workload.

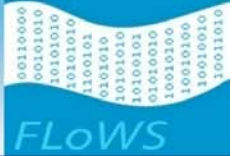


Asymptotic optimal policy is a function of workload. Implementation will require message passing, or other techniques to share information regarding dynamic hot-spots

- Learning locations of hot-spots can simplify network coding



# Summaries and challenges



**KEY CONCLUSION:** Resource allocation for optimal throughput can be attained in many ways. *Some are better than others!*

**LYAPUNOV THEORY:** Quadratic Lyapunov function effective since it mirrors actual solution to DP equation. A tighter approximation results in better performance

**RELAXATION:** Workload relaxation enables construction of reduced-order model for which solution to the DP equation is obvious, provided there is a single bottleneck.



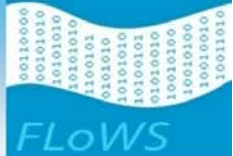
**HOW BAD IS THE REAL WORLD?** In the example of V&S, about 15% of packets are routed upstream. We discovered this increases dramatically with volatility. Is this seen in practice?

**CAN WE LEARN?** Especially when there is only a single bottleneck, key information for optimization is easy to identify. How can this information be shared?

**CAN WE CODE?** With the identification of dynamic bottlenecks, it is then evident where the capacity region can be improved

**Largest current research bottleneck concerns learning dynamic bottleneck location and workload**

# Large-Scale Network Utility Maximization (NUM)



STATUS QUO

Dual decomposition is a widely used method for congestion control.

It is first order and decentralized.

Deals only with strictly concave utilities.



NEW INSIGHTS

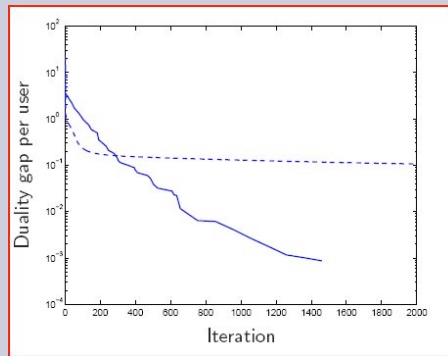
A second order, primal-dual method performs better under wider network conditions (congested networks for instance). It is also able to handle not strictly concave utility functions.



## ACHIEVEMENT DESCRIPTION

### MAIN RESULT:

Developed a primal-dual interior-point method for large-scale NUM, that outperforms dual decomposition.



### HOW IT WORKS:

Attempts to solve approximate optimality conditions at each iteration.

Computes search direction using preconditioned conjugate gradient method.

Can scale up to networks of 1,000,000 flows, or even more!

### ASSUMPTIONS AND LIMITATIONS:

Algorithm is scalable, performs better but centralized.

END-OF-PHASE GOAL

An attempt to get a decentralized heuristic based on this method.

Including further extensions, like piecewise linear utility functions, link delay.



COMMUNITY CHALLENGE

**Convergence issues of first order methods could render them impractical.**

Towards second order methods for Network Utility Maximization

# An Interior-Point Method for Large-Scale Network Utility Maximization

Argyrios Zymnis Nikolaos Trichakis

**Stephen Boyd** Dan O' Neill

Electrical Engineering Department

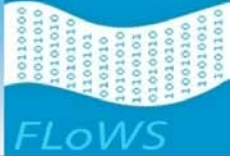
Stanford University

ITMANET PI

Meeting 07/26/07



# NUM problem



$$\begin{aligned} &\text{maximize} && U(f) = \sum_{j=1}^n U_j(f_j) \\ &\text{subject to} && Rf \leq c, \quad f \geq 0 \end{aligned}$$

- share resources
- dual decomposition
  - distributed, scalable
  - converges to global optimum
  - can back interpret protocols via  $U_j$
  - will “track” changes in problem data  $U$ ,  $R$ , or  $c$

who can ask for more?

# The bad news



- Requires  $U_j$  to be strictly concave
- first order method; can converge slowly
  - fast convergence for “symmetric” problems
  - slow convergence for “asymmetric” problems (e.g., bottlenecks or long routes)
- hence, “tracks” changes very poorly

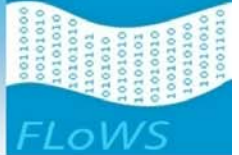
is this the price we have to pay for a distributed, scalable algorithm?

# What we did

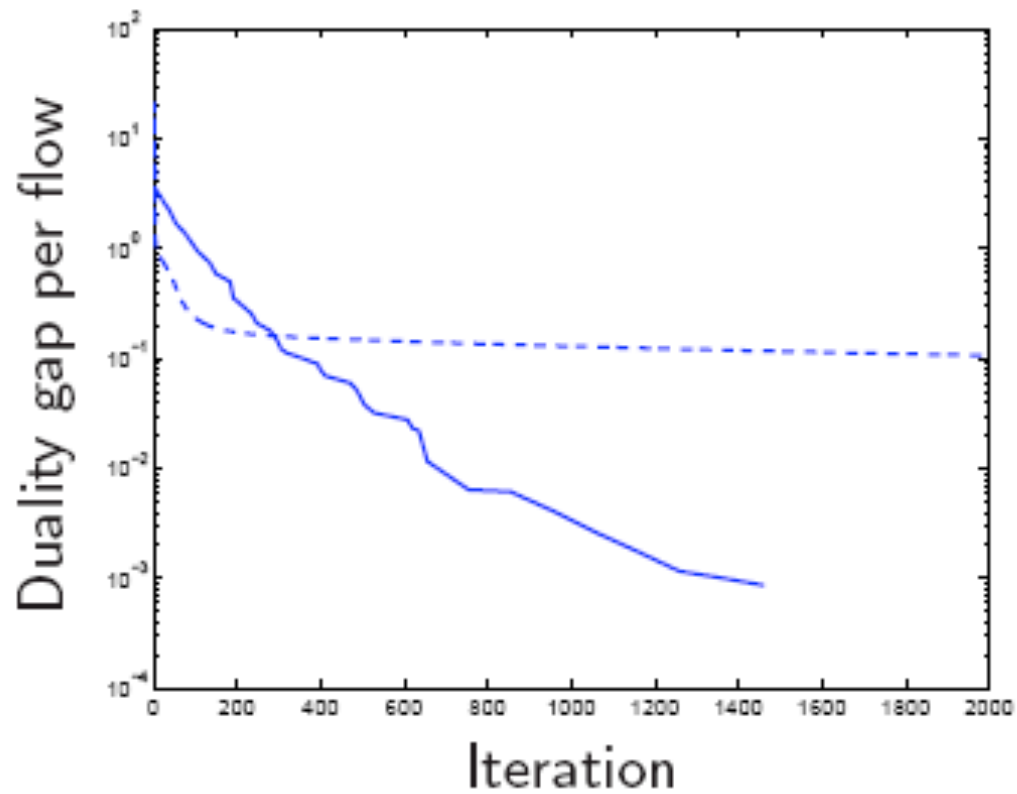


- worked out a scalable **but not decentralized** interior-point method for NUM
- second order method; handles asymmetries well
- fast convergence, independent of problem dimensions or data (!!)
  - scales to  $10^6$  or more flows
  - can optimize over  $10^3$  flows in  $<10^{-3}$  sec (estimated)
- similar computational complexity per iteration to dual decomposition
- can track problem data very fast

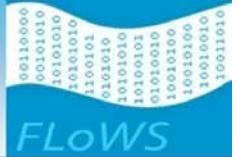
# Typical convergence



- $10^5$  flows,  $2 \cdot 10^5$  links
- 200 congested links (each with  $3 \cdot 10^4$  flows)

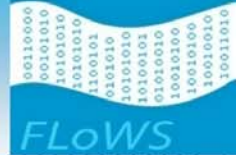


# So what?

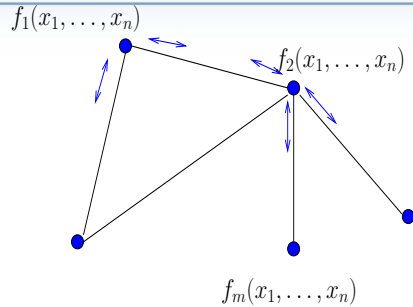


- we could actually evaluate convergence of dual decomposition for large networks
- dual decomposition is OK for “symmetric” data, for others not
- we guess there are practical uses
  - ability to quickly track optimum makes up for communication overhead
- centralized optimization and dual decomposition
  - not one versus the other
  - can apply dual decomposition at higher granularity;
  - whole subnets optimized quickly and centrally

# Distributed Asynchronous Optimization Methods for General Performance Metrics



STATUS QUO



Existing methodology based on Lagrangian relaxation and duality does not lend itself to distributed algorithms for general non-separable (coupled) user performance metrics in wireless networks with time-varying connectivity



NEW INSIGHTS

Subgradient methods with simple consensus (averaging) policies lead to decentralized algorithms that

- optimize general performance metrics,
- are robust against changes in network topology



## ACHIEVEMENT DESCRIPTION

### MAIN RESULT:

- Development of a distributed computational method for optimizing the sum of performance measures of users
- The method operates **asynchronously** under **time-varying connectivity**
- We provide **convergence rate results** that explicitly characterize the impact of the system and algorithm parameters on the quality of generated solutions.

### HOW IT WORKS:

- Each user maintains an information state, which is an estimate of the optimal solution.
- The update rule for each user involves combining his information state with that of his current neighbors and performing a subgradient step using his local performance measure.

### ASSUMPTIONS AND LIMITATIONS:

- The model is unconstrained.
- The communication bandwidth constraints have not been taken into account.

END-OF-PHASE GOAL

- We will extend the model to include local (potentially time-varying) constraints for each user.
- We will explore the effect of bandwidth constraints (i.e., quantized information exchange) on the performance of the algorithms.



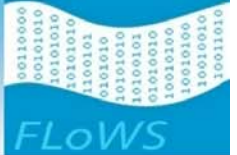
COMMUNITY CHALLENGE

*Design of optimization algorithms that address the challenges and constraints associated with large-scale time-varying networks*

**Distributed optimization algorithms for general performance metrics and time-varying connectivity**



# Incomplete information, dynamics, and wireless games



STATUS QUO

Previous work studied ad hoc wireless resource competition among multiple nodes using game theoretic techniques, but typically in a stationary setting, where each node knows all other's channel conditions (see Huang et al., Etkin et al.)

We aim to understand the importance of a lack of information about channel conditions over time.

NEW INSIGHTS

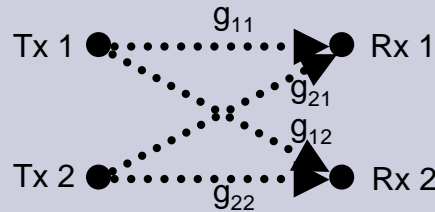
We bring in the importance of incomplete channel information via the use of both static and dynamic *Bayesian games*, and in particular exploit results on reputation effects in economics to study primary/secondary competition.

(S. Adlakha, R. Johari, A. Goldsmith)

## FLAWS ACHIEVEMENT(S)

**MAIN RESULT:** *The presence of incomplete channel information among nodes, as well as dynamic interaction among nodes, can dramatically alter the game theoretic conclusions drawn in standard complete information settings.*

**Example:** A primary user may deter entry by secondary users at some cost to himself, even if it is not immediately in his best interest to do so.



**HOW IT WORKS:** We use the theory of *Bayesian games* to find symmetric equilibria of a Bayesian Gaussian interference game.

We use the theory of *reputation effects in dynamic games of incomplete information* model to study the behavior of a primary user interacting with multiple secondary users.

### ASSUMPTIONS AND LIMITATIONS:

We assume one primary and several secondaries arriving over time; we assume the channel remains stationary over several periods of interaction between primary and secondary.

Key assumption (and limitation): there is no "protocol" for transmission, so all other transmission treated as pure noise (hence the Gaussian interference model).

END-OF-PHASE GOAL

We need to extend the model to handle not only a finite horizon model, but also an infinite horizon model with changing channel conditions.

Journal paper is being prepared for submission to JSAC.

Longer term: we need to focus more on implications for *algorithm design for ad hoc wireless nodes in a reactive environment*. Our insights set a foundation for this.

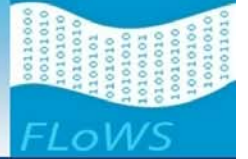
COMMUNITY CHALLENGE

**Status quo is useless for designing node strategies.**

**Employ methods from learning and dynamic equilibrium in large games to build better algorithms for competition and cooperation.**

**Real environments are reactive and non-stationary; this dramatically changes incentives and game theoretic predictions**

# Part I: Bayesian Gaussian interference game



- Assume transmit/receive pair 1 observes the incident gains  $g_{11}$ ,  $g_{21}$ , but not  $g_{22}$  or  $g_{12}$  (similarly for Tx/Rx pair 2); assume flat fading
- This is a Bayesian game:  
Once random gains are realized, each TR pair knows its own gains but not the gains of the other
- This is a supermodular Bayesian game; in particular, local search dynamics converge (see also R. Berry's work)
- Nodes can either use a single channel, or spread power across all channels

*Theorem:* equal spreading is unique symmetric equilibrium



## Part II: Reputation effects in a dynamic game



- Now assume Tx/Rx 1 = primary, Tx/Rx 2 = secondary; same system model, but now assume only 2 channels
- Primary is *long-lived* and *fully rational*
- Secondary user is *myopic* (only optimizes one period payoff), but *history-aware* (remembers the past)
- Secondary user decides each period whether to “enter” (i.e., transmit), or “leave” (i.e., stay silent)
- Secondary user is assumed to have a cost for power consumption
- Primary user can “share” (give up a channel to secondary) or “spread” (spread power equally over channels)

## Part II: Reputation effects in a dynamic game

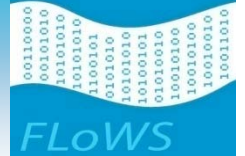


When both  $g_{12}$ ,  $g_{21}$  are large,  
there can be a *reputation effect*.

Despite the fact that the primary would be better off sharing (in one period) if secondary enters, the primary may choose to spread (“act” threatening) *because this deters future entry by the secondary*

Key point:

This cannot happen in a complete information model!  
(For complete information case, see Etkin et al.)



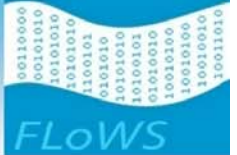
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## Application Metrics and Network Performance Summary



- **New Distributed Optimization Models for Resource Allocation**
  - Building an algorithmic architecture that is robust against changes in network structure, optimizes general performance measures, scalable, and distributed
  - Incorporating networked-system constraints (e.g., asynchronism, stochastic elements, communication bandwidth constraints) in algorithm design, and quantifying the impact on performance
- **Flow-based Models and Queuing Dynamics**
  - Designing macro (flow) and micro (queuing) level network algorithms to yield desired performance
  - Integration of macro and micro level models
- **New Resource Allocation Paradigm with Focus on Heterogeneous and Non-cooperative Nature of Users**
  - Understanding when local competition yields globally desirable outcomes
  - Studying the dynamics that achieve the equilibrium

# Achievements Overview



## Optimization Theory

Distributed efficient algorithms for resource allocation

**Boyd:** Efficient second order methods for flow control

**Shah:** Throughput analysis of flow-level models with heterogeneous users

**Shah:** Low complexity throughput and delay efficient scheduling

**Meyn:** Generalized Max-Weight to tradeoff information and performance

**Ozdaglar, Shah:** Distributed scheduling and flow control to balance user and network performance

**Ozdaglar:** Distributed asynchronous optimization algorithms for general metrics and time-varying connectivity

**Goldsmith, Johari:** Game-theoretic model for cognitive radio design in the presence of incomplete channel information

**Johari:** Topology formation model with application goals such as connectivity and cost of routing and link maintenance

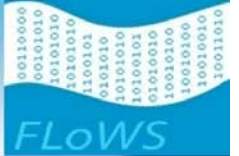
## Stochastic Network Analysis

Flow-based models and queuing dynamics

## Game Theory

New resource allocation paradigm that focuses on heterogeneity and competition

# Thrust Synergies



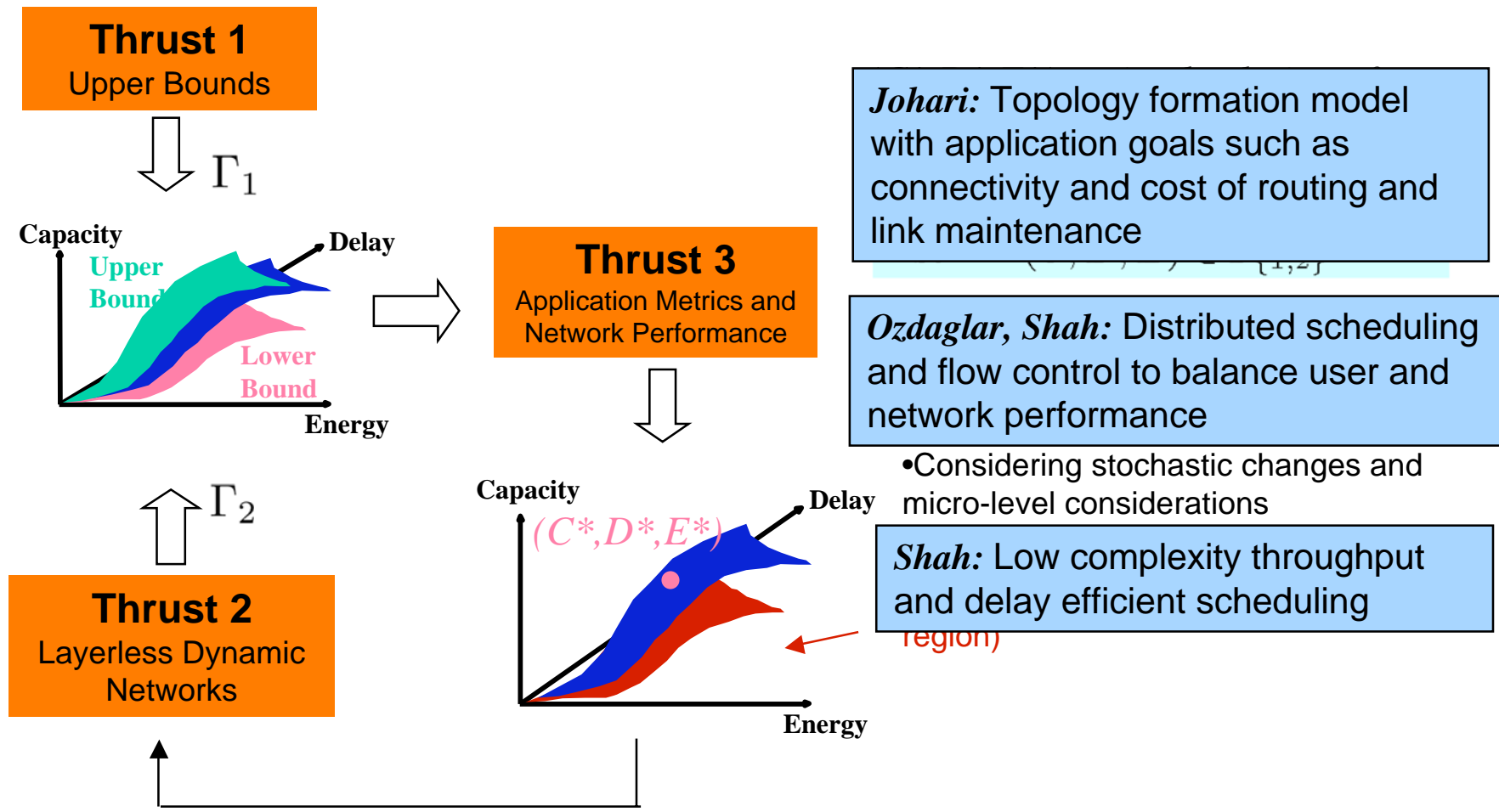
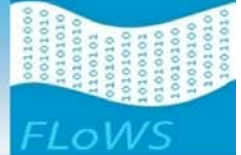
- General objective of the thrust requires:
  - Flow-level algorithms for optimizing heterogeneous application metrics
  - Packet-level algorithms for ensuring efficient and stable functioning of the network
  - Integration of application metrics and network capabilities
- Our thrust achieves these objectives through an algorithmic approach based on:
  - Development of efficient distributed optimization and control algorithms
  - Stochastic network analysis for stability and efficiency
  - Synergy in the integration of the macro and micro level models and of algorithmic optimization and stability analysis
  - Game-theoretic analysis of equilibrium models for
    - robustness against adversarial, competitive, and non-compliant behavior
    - modeling information structures

# Synergies with Other Thrusts



- Resource negotiation for performance tradeoffs
  - Thrust 1 provides upper bounds on “performance region”
  - Thrust 2 provides achievable region
  - Thrust 3 chooses operating point on these regions
- Algorithms for implementing “building blocks” within network context
  - Thrust 2 uses information-theoretic analysis to provide closed-form or asymptotic solutions for canonical networks
  - Thrust 3 designs algorithms to incorporate these insights/building blocks into a network
- Algorithmic constraints may introduce new performance metrics for data processing in Thrust 2

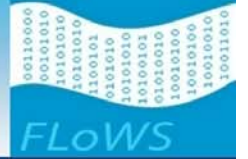
# Thrust Synergies: An Example



Algorithmic constraints and sensitivity analysis may change the dimension of performance region

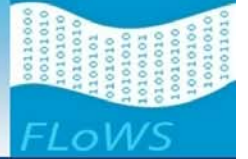


# Roadmap for Phase 1



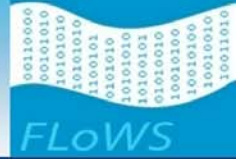
- Decentralized implementations for fast second order optimization methods
- Incorporation of networked-system constraints (bandwidth limitations, delays, stochastic elements) on distributed algorithm design
- High throughput low delay distributed scheduling algorithms in the presence of interference effects
- Decentralized implementations for generalized max-weight policies
- Design of dynamic algorithms for achieving equilibrium in game-theoretic models

# Recent Publications



- Abhishek, S. Adlakha, Johari, and Weintraub, “Oblivious Equilibrium for General Stochastic Games with Many Players,” submitted to Allerton 2007.
- Adlakha, Johari, and Goldsmith, “Competition Between Wireless Devices with Incomplete Channel Knowledge,” submitted to IEEE JSAC 2007.
- Ahmed, Eryilmaz, Ozdaglar, and Medard, “Economic Gains from Network Coding in Wireless Networks,” submitted for publication 2007 (also appeared in Allerton 2006)
- Arcaute, Johari, and Mannor, “Network Formation: Bilateral Contracting and Myopic Dynamics” submitted to IEEE TAC 2007.
- Bayati, Prabhakar, Shah and Sharma, “Iterative Scheduling Algorithms,” IEEE Infocom, 2007.
- Bayati, Shah and Sharma, “Maximum Weight Matching via Max-Product Belief Propagation,” To appear in IEEE Information Theory Transactions, 2007.
- Coleman, Martinian, and Ordentlich, "Joint Source-Channel Decoding for Transmitting Correlated Sources over Broadcast Networks", submitted January 2007, IEEE Transactions on Information Theory (also appeared in 2006 International Symposium on Information Theory, Seattle, WA, July 10-14, 2006).

# Recent Publications



- Doshi, Shah and Medard, "Source Coding with Distortion through Graph Coloring," IEEE ISIT, 2007.
- Doshi, Shah, Medard and Jaggi, "Distributed Functional Compression through Graph coloring," DCC, 2007.
- Doshi, Shah, Medard and Jaggi, "Graph Coloring and Conditional Graph Entropy," Asilomar conference, 2006, pp: 2137-2141.
- Eryilmaz A., Ozdaglar A., Modiano E., "Polynomial Complexity Algorithms for Full Utilization of Multi-hop Wireless Networks," IEEE Infocom, 2007.
- Meyn S., "Stability and Asymptotic Optimality of Generalized MaxWeight Policies", submitted for publication, 2006
- Meyn. Control techniques for complex networks. To appear, Cambridge University Press, 2007.
- Mosk-Aoyama and Shah, "Computing Separable Functions via Gossip," Under preparation. Preliminary version appeared in ACM PODC, 2006.
- Nedic and Ozdaglar, "Distributed Asynchronous Subgradient Methods for Multi-Agent Optimization," submitted for publication, 2007.