

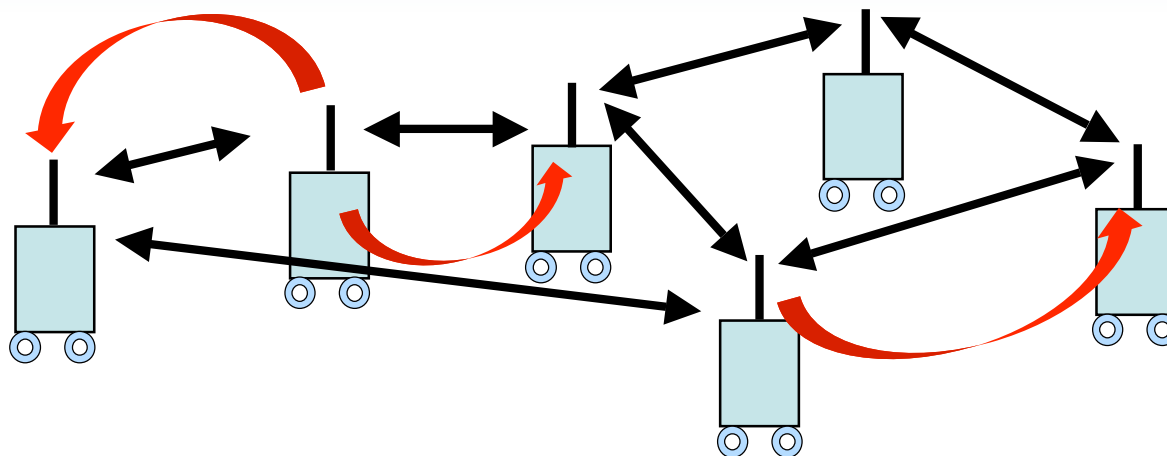
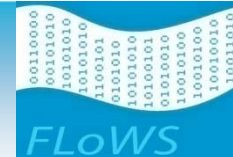
**Information Theory for Mobile Ad-Hoc Networks (ITMANET):  
*The FLoWS Project***

# **FLoWS Overview and Update**

**Andrea Goldsmith**



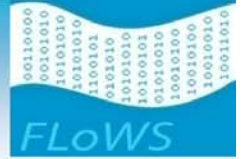
# DARPA's Grand Challenge



- Develop and exploit a more powerful information theory for mobile wireless networks.
- Anticipated byproducts include new separation theorems to inform wireless network "layering" as well as new protocol ideas.

***Hypothesis: A better understanding of MANET capacity limits will lead to better network design and deployment.***

# Limitations in Existing Theory

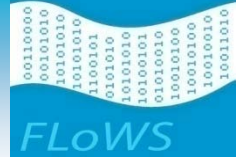


- Much progress in finding the Shannon capacity limits of wireless single and multiuser *channels*
- Little known about these limits for mobile wireless *networks*, even for simple (canonical) models
- Shannon's capacity definition based on infinite delay and asymptotically small error was brilliant!
  - Has also been limiting
  - Cause of unconsummated union between networks and information theory
  - What is the alternative?

**Capacity beyond Shannon**

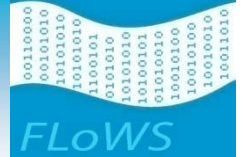


# FLoWS Program Objectives



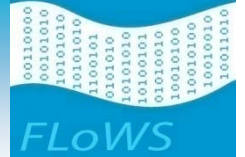
- Develop tractable and insightful metrics and models for MANET information theory.
- Define fundamental performance limits for MANETs in terms of desired objective metrics.
- Obtain upper and lower performance bounds for these metrics for a given set of MANET models.
- Define the negotiation between the application and network for resource allocation and performance optimization of our given metrics
- Bound the cost of using our set of metrics as the interface between the network and applications.

# Thrust Objectives and Scope

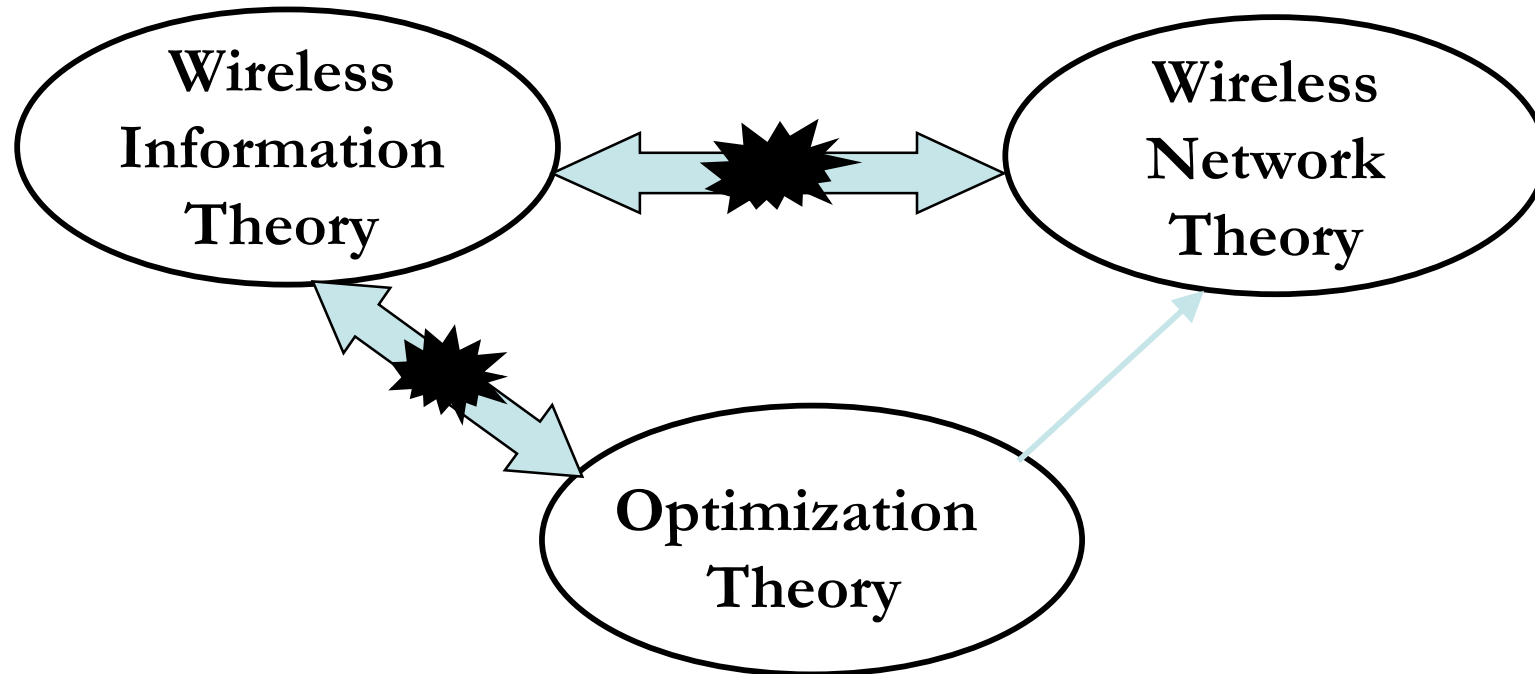


- **Models and Metrics** (Leads: Effros and Goldsmith):
  - **Objective:** Develop a set of metrics for dynamic networks that capture requirements of current and future applications
  - **Scope:** Develop a set of models for MANETs that are tractable yet lead to general design and performance insights
- **New Paradigms for Upper Bounds** (Leads: Koetter and Medard)
  - **Objective:** Obtain bounds on a diversity of objectively-defined metrics for complex interconnected systems.
  - **Scope:** A comprehensive theory for upper bounding the performance limits of MANETs
- **Layerless Dynamic Networks** (Lead: Zheng)
  - **Objective:** Design for networks as a single dynamic probabilistic mapping, without pre-assigned layered structure
  - **Scope:** Remove layering and statics from MANET information theory.
- **Application Metrics and Network Performance** (Lead: Ozdaglar)
  - **Objective:** Provide an interface between application metrics and network performance
  - **Scope:** Develop a theory of generalized rate distortion, separation, and network optimization for MANETs

# Today's Unconsummated Unions

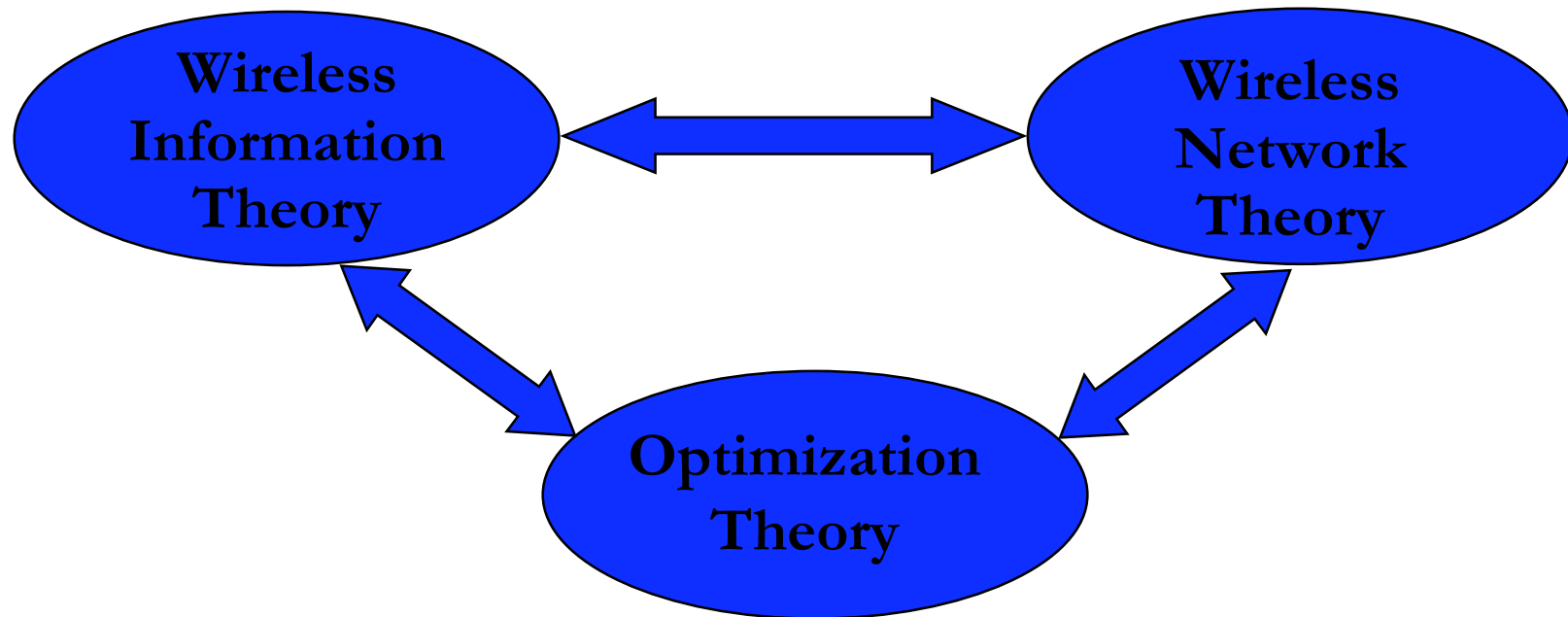
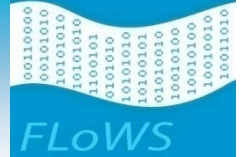


**B. Hajek and A. Ephremides, "Information theory and communications networks: An unconsummated union," *IEEE Trans. Inf. Theory*, Oct. 1998.**



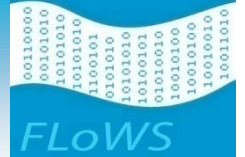
- Success on narrowly-defined information theory of wireless networks.
- Large body of wireless (and wired) network theory that is ad-hoc, lacks a basis in fundamentals, and lacks an objective success criteria.
- Little cross-disciplinary work spanning these fields, except applying optimization techniques to existing wireless network designs.

# Challenge: Consummate Union



- When capacity is not the only metric, network theory is needed to deal with delay, random traffic, and application requirements
- Optimization provides the missing link for consummation
  - Becomes a menage-a-trois

# Optimization as the missing link



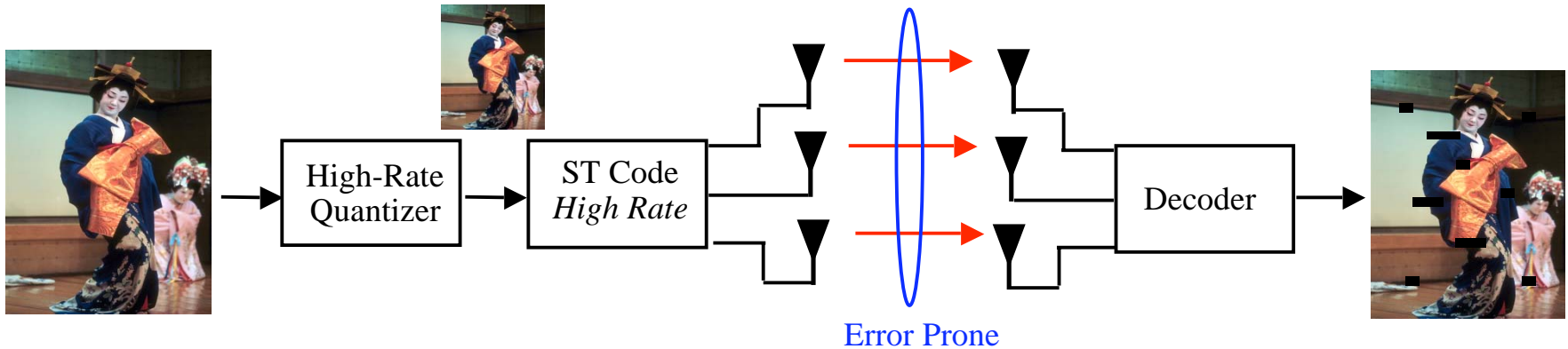
- Shannon capacity analysis generally becomes intractable for more than a few nodes, except in scaling laws.
- Capacity results are generally built around asymptotics
  - Asymptotically large blocklength/delay
  - Asymptotically high SNR
  - Asymptotically small probability of error
  - Infinitely many users
  - Infinite data backed up
- These asymptotics usually make all the interesting wireless and networking problems go away
  - Shannon theory generally breaks down when delay, error, or user/traffic dynamics must be considered

**Optimization tools can be highly adept at obtaining fundamental limits when the Shannon tools break down**

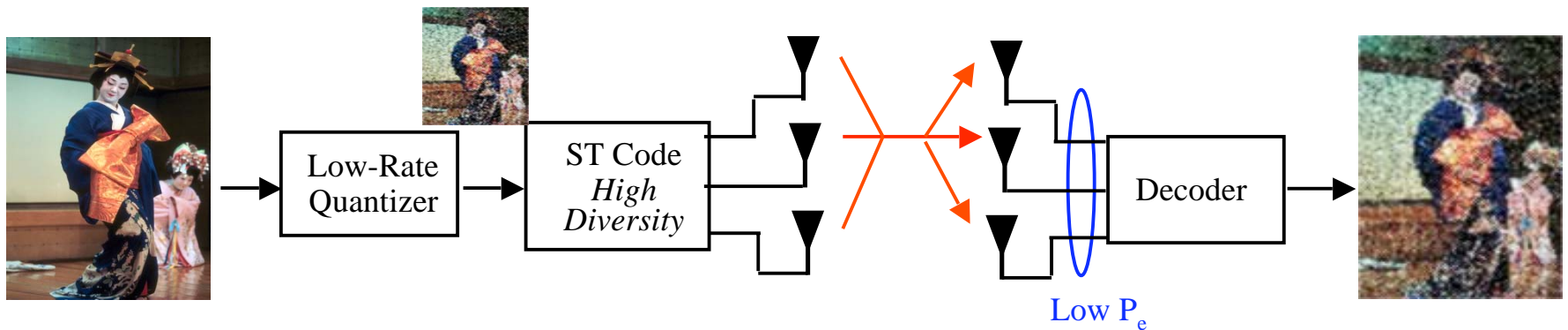


# Example: MIMO Tradeoffs

- Use antennas for multiplexing:

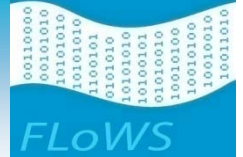


- Use antennas for diversity

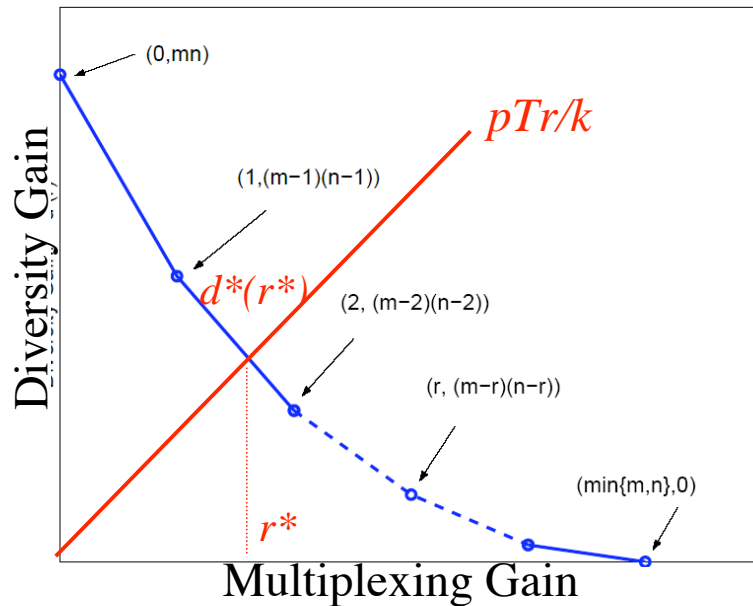


How should antennas be used? Depends on higher layer metrics

# Minimizing End-to-End Distortion

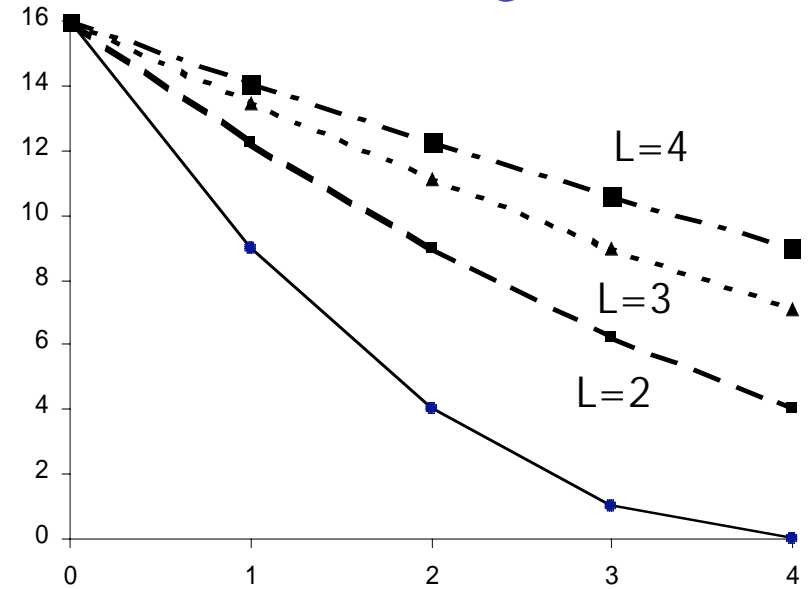


## Diversity-Multiplexing Tradeoff at high SNR



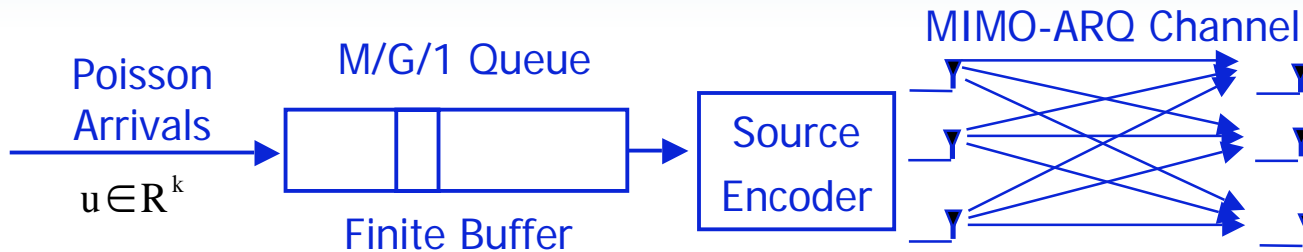
- Can obtain closed-form expression for optimal operating point on tradeoff curve to minimize end-to-end distortion
- Separate source/channel coding optimal
- Minimum distortion is  $-d^*(r^*)$
- *At moderate SNR, solve via optimization*

## Diversity-Multiplexing-ARQ Tradeoff at high SNR

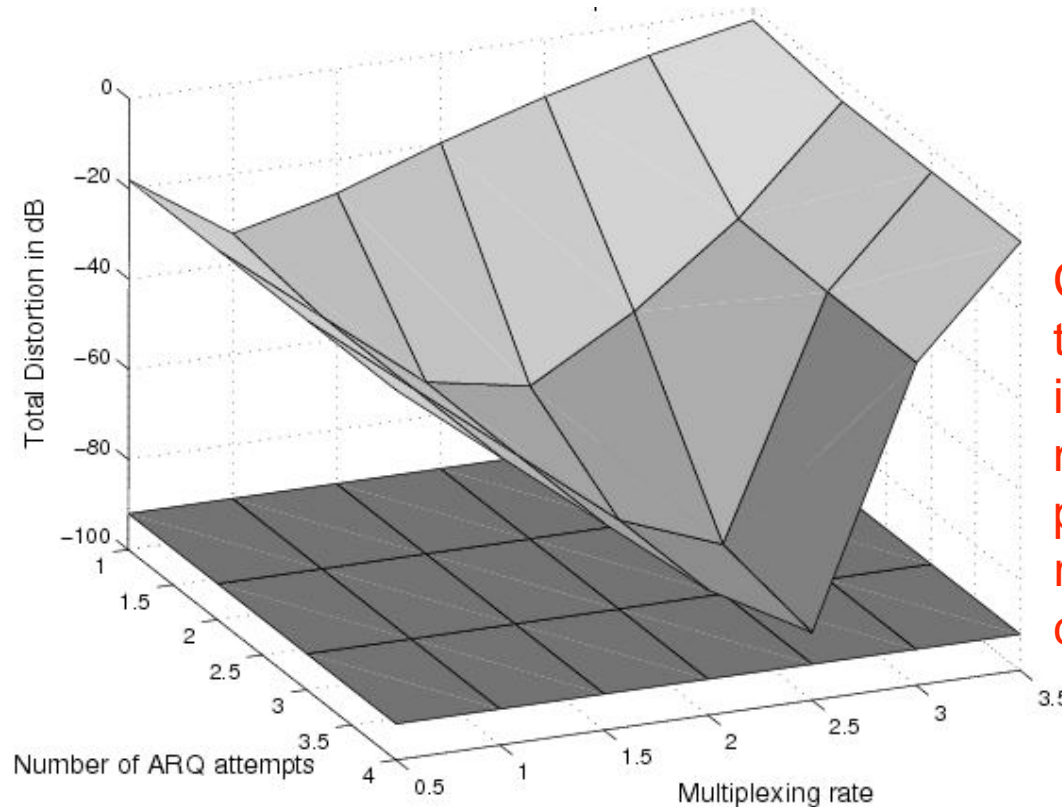


- Allows a diversity/multiplexing/delay tradeoff analysis
- High SNR leads to rare ARQ errors
- Effectively removes delay; “free” retransmissions (Bernashev, 1976)
- *Cannot capture queuing impact with high SNR (Shannon) analysis!*

# Can solve with optimization tools

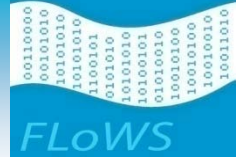


$$\text{Min } D_{\tau}(F, \text{SNR}) \leq D_s(F) + P_e(\text{SNR}) + P\{\text{Delay} > k\}.$$



Connects to Shannon-theoretic results; indicate where ARQ is most useful, and provides insight into refining analysis for closed-form soln.

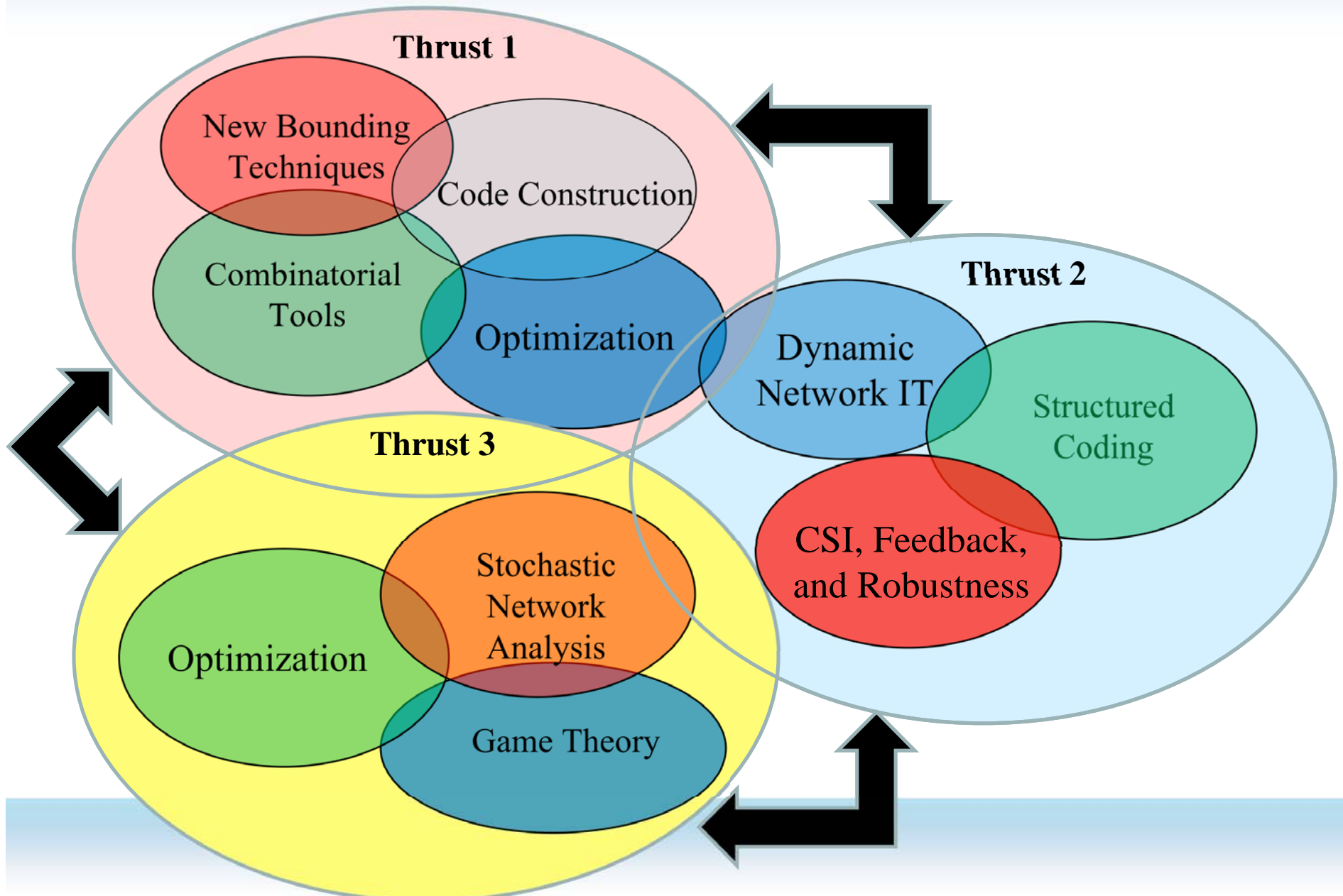
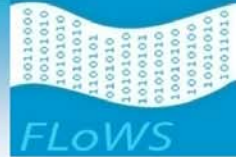
# Progress since July



- A wealth of results extending prior our work, developing new ideas, and forging new synergies within and between our thrust areas
- New and ongoing collaborations among PIs, including student/postdoc exchanges
- Overview paper
  - Co-authors: Effros, Goldsmith, Medard
  - Targeted for Scientific American (or similar publication)
  - Outline complete and writing begun; plan to complete in Jan.
- JSAC Tutorial on MANET Capacity with Cognitive Radios
  - Co-authors: S. Jafar, I. Maric, and A. Goldsmith
  - Paper will be submitted at the end of December
- Website updated with July PI meeting slides, recent publications, recent results, and thrust area descriptions\*

\*After this meeting.

# Thrust Synergies and New Intellectual Tools



# Thrust 0: New Models and Metrics



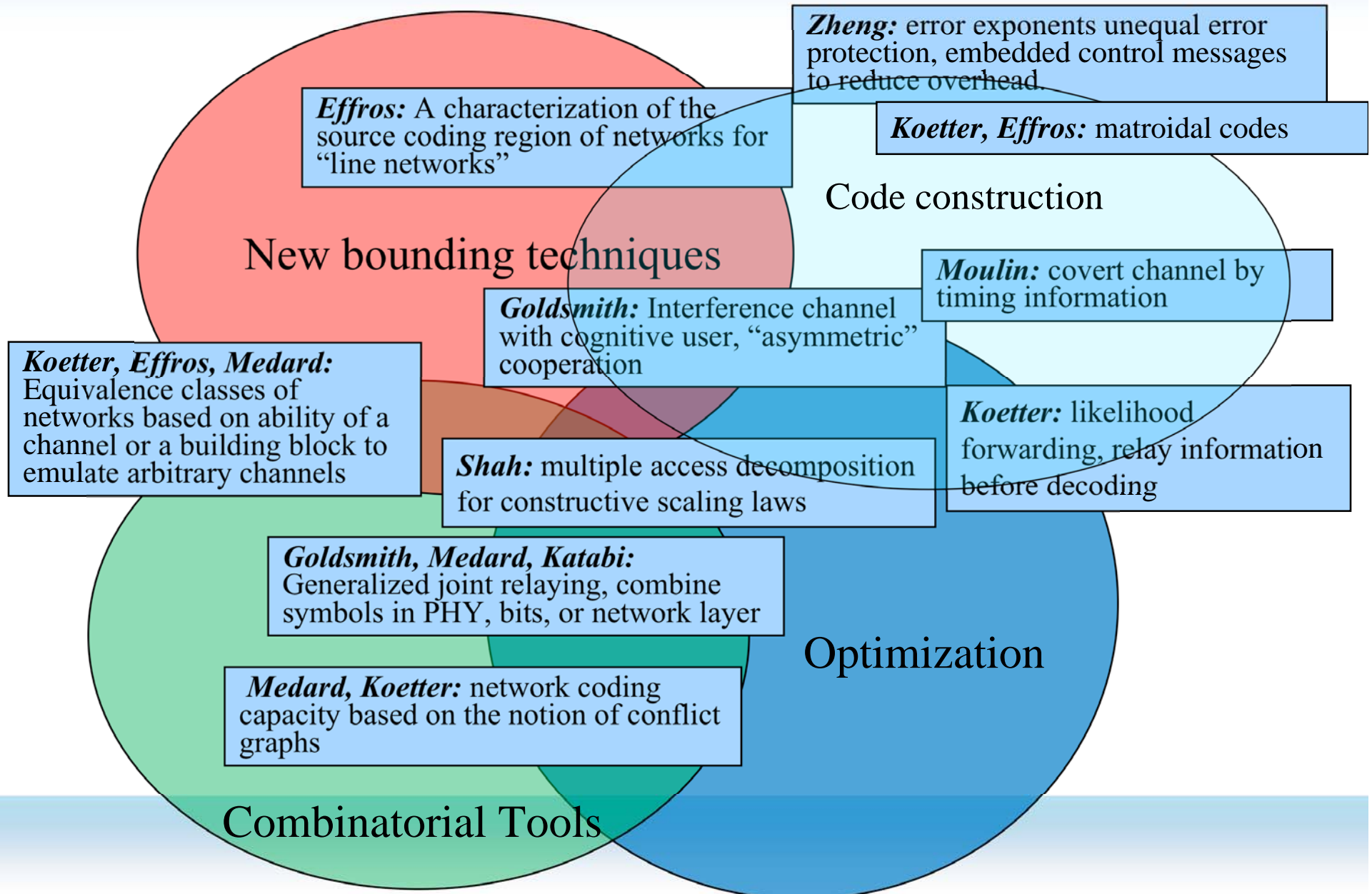
## *New Models*

- Finite-state Markov dynamics in multiuser channels
- Fading channels with unknown statistics
- Cognitive transmitters
- Large networks with arbitrary node placement
- Arbitrary data flows
- Multicast traffic

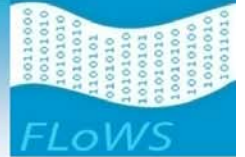
## *New Metrics*

- Generalized Capacity and UEP
- Capacity Region for Scaling Laws
- Throughput vs. Delay
- Generalized Distortion
- Queuing Distortion
- Multiperiod Network Utility
- Quantized Utility
- Game-theoretic equilibrium
- Oblivious equilibrium

# Thrust 1 Synergies and Results



# Thrust 2 Synergies and Results



## *Dynamic Network Information Theory*

**Goldsmith, Medard, Katabi:**  
Joint relaying, combine symbols in PHY, bits, or network layer

**Coleman:** Rate Distortion of Poisson Processes

**Zheng:** Euclidean Information Theory

**Goldsmith:** Degraded FS Broadcast Channels

**Goldsmith:** Cognitive users and interference

**Moulin:** Information flow via timing

**Coleman:** Joint Source/Channel Coding in Networks

**Goldsmith:** Feedback and Directed Information

**Effros, Goldsmith:** Generalized capacity, distortion, and joint source/channel coding.

**Moulin:** Universal Decoding in MANETs

**Meyn, Zheng, Medard:** mismatched receiver, online robust algorithm to combat imperfect channel info.

**Goldsmith:** Broadcasting with layered source code, graceful degradation for weaker users

**Zheng:** Embedded Coding and UEP

*Structured coding*

*CSI, feedback, and robustness*



# Thrust 3 Synergies and Results



## Optimization Theory

Distributed efficient algorithms for resource allocation

**Boyd:** Dynamic and stochastic network utility maximization with delivery constraints

**Ozdaglar:** Distributed optimization algorithms for general metrics and with quantized information

**Boyd, Goldsmith:** Network utility maximization with adaptive modulation

**Medard, Ozdaglar:** Efficient resource allocation in non-fading and fading MAC channels using optimization methods and rate-splitting

**Shah:** Optimal capacity scaling for arbitrary node placement and arbitrary multi-commodity flows

**Goldsmith, Johari:** Game-theoretic model for cognitive radio design with incomplete channel information

**Shah:** Low complexity throughput and delay efficient scheduling

**Johari:** Dynamics and equilibria in stochastic games

**Meyn:** Generalized Max-Weight policies with performance optimization

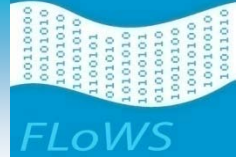
## Stochastic Network Analysis

Flow-based models and queuing dynamics

## Game Theory

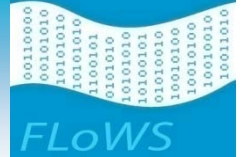
New resource allocation paradigm that focuses on heterogeneity and competition

# Progress Criteria: Phase 1



- Develop tractable and insightful metrics and models that expand the definition of information theory to encompass the degrees of freedom, constraints, and dynamics inherent to wireless networks ✓
- Develop new upper bounding techniques for MANET capacity and other performance metrics and evaluate these bounds for small to medium sized networks under relatively simple assumptions. ✓
- Develop new achievability results for key performance metrics by optimizing dynamic node cooperation and resource allocation over available degrees of freedom. ✓
- Use rate distortion theory and network utilization to optimize the interface between networks and applications. ✓
- Use new theory along all three thrusts to characterize trade-offs between delay, energy and capacity, and possibly other metrics. ✓
- Demonstrate significant performance gains in key performance metrics based on our developed theory in each thrust area. ✓
- Use the new MANET information theory and its associated insights to obtain breakthroughs in wireless network design. ✓

# Posters



- Thrust 1

- Network Capacity Equivalence: *Koetter, Effros and Medard*
- General capacity using network coding: *Medard*
- On Matroidal Solutions for Network Coding: *Cohen, Effros, ElRouayheb and Koetter* (Also Thrust 2)
- The Intermediate Density Scaling Regime: *Johari*
- On Optimal Capacity Scaling in Arbitrary Wireless Networks: *U. Niesen, P. Gupta and D. Shah* (Also Thrust 3)

- Thrust 2

- Euclidean Information Theory: *Zheng*
- The Degraded Finite-State Broadcast Channel: *Dabora and Goldsmith*
- Feedback and Directed Information in Wireless Networks: *Permuter, Weissman, and Goldsmith* (Also Thrust 1)
- Universal Decoding in MANETS: *Moulin*
- Capacity of Interference Channels with Cognitive Transmitters: *Maric, Goldsmith, Shamai, Kramer* (Also Thrust 1)
- General Relaying for Multicast in Wireless Networks: *Maric, Goldsmith, and Medard* (Also Thrust 1)
- Capacity and Queue-based Codes for Timing Channels: *Moulin*

# Posters (Cont'd)

- Thrust 2 (Cont's)

- Rate Distortion of Poisson Processes under Queuing Distortion: *Coleman, Kiyavash, and Subramanian*
- Embedded Coding and UEP: *Borade and Zheng* (Also Thrust 1)
- Joint Source/Channel Coding in Networks: *Coleman*
- Capacity, Source/Channel Coding, and Separation: *Liang, Goldsmith, and Effros* (Also Thrust 1)

- Thrust 3

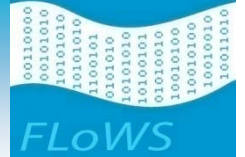
- Utility Maximization and Cross-Layer Optimization in Dynamic Networks: *Boyd* (Also Thrust 2 and 1)
- Network Utility Maximization and Adaptive Modulation: *O'Neil, Goldsmith, and Boyd* (Also Thrust 2)
- Wireless networks: Algorithmic trade-off between Throughput and Delay: *D. Shah, D. Tse, J. Tsitsiklis* (Also Thrust 1)
- Optimizing MaxWeight: Routing Implementation: *Meyn and Chen* (Also Thrust 1)
- Distributed Control and Optimization Methods for Wireless Networks: *Ozdaglar*
- Incomplete information, dynamics, and wireless games: *Adlakha, Johari, and Goldsmith*
- Oblivious Equilibrium for General Stochastic Games: *Johari*

**Information Theory for Mobile Ad-Hoc Networks (ITMANET):  
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**Project Summary**

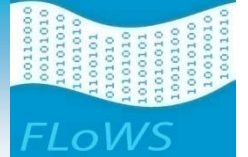


# Project Summary



- We have made substantial progress on many topics within our thrust areas: satisfied progress criteria
- Synergies between thrusts are emerging, in particular the role of optimization in consummating the union
- Ongoing challenges to be addressed (food for thought)
  - How to define and address reliability explicitly: what is fundamental?
  - Models: What common canonical models are useful for information theory and networking
  - Design and “verification” for robustness to models
  - Along what axes should separation be defined?
    - Protocol/function layers, time, space, ...

# Also in Team Meeting



- Dynamics in equivalence classes
- Reliability in our project, particularly DNUM
- Red teaming (format and specific feedback)

# Thanks to Chris

**For your vision, inspiration,  
and leadership  
in creating and managing  
the ITMANET program**



**Information Theory for Mobile Ad-Hoc Networks (ITMANET):  
*The FLoWS Project***

**Team Meeting**

MANET Metrics

Constraints

Capacity and Fundamental Limits

New Paradigms for Upper Bounds

Layerless Dynamic Networks

Application Metrics and Network Performance

Capacity

Upper Bound

Lower Bound

Metric 1 (Delay, Power, Robustness, ...)

Models and Dynamics

Degrees of Freedom

Metric 2

End-to-End Performance and Network Utility

Capacity

$(C^*, D^*, E^*)$

Metric 1

$$Utility = U(C, D, E)$$

Metric 2

Application Metrics

Metrics

Models

New MANET Theory

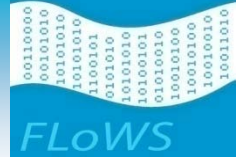
**FLows**  
Fundamental Limits of Wireless Systems



# R<sup>3</sup>: Robustness/Reliability/Resilience

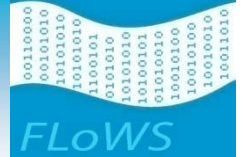
- Definition: Graceful performance degradation in the face of modeling errors and uncertainty
  - Performance refers to both capacity and **policies**.
  - Modeling errors/uncertainties include model variations, dynamics, lack/imperfections of knowledge, model-free notion
- How to fundamentally address robustness
  - Design to be robust to sensitivity in modeling
  - Explicitly include robustness mechanisms in design
    - Feedback
  - At PHY layer: universality, UEP, outage, worst-case, inherently-robust capacity definitions, ARQ...
  - At NET layer: incorporate link dynamics, pessimistic distributions, Expectation to induce risk aversion, (rateless) coding across the network, network management

# What is $R^3$ (Subject to some debate)



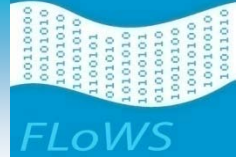
- Robustness: Optimizing against a parametric class of models
- Reliability: Good performance for unanticipated events
- Resilience: Graceful degradation with respect to imperfections in model assumptions

# Separation



- Definition
  - Breaking a large problem into smaller problems
  - What is the price?
  - Examples
    - Equivalence results (Channel vs. network coding)
    - All Optimization work (PHY vs. Network)
    - Hierarchical Scaling Laws (spatial)
    - Generalized capacity and separation (channel vs. source coding)
    - MAC under uncertainty (timescale separation)
    - DNUM (timescale separation)
    - Workload relaxation (spatial decomposition)
- What are the right axes?
  - PHY vs. Network vs. Application
  - Spatial separation
  - Timescales

# Next Steps



- Start work related to Phase 2 goals
- Develop further the synergies between thrusts that have emerged, and develop new ones.
- Clearly articulate
  - Lessons learned from CBMANET, and how to incorporate them into our work
  - What metrics we are taking into account, and which ones we aren't.
  - More on robustness, separation, and canonical models.