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# Array-conditioned deconvolution of multiple-component teleseismic data with application to the Slave craton

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Schlumberger-Doll Research

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SCIENCE

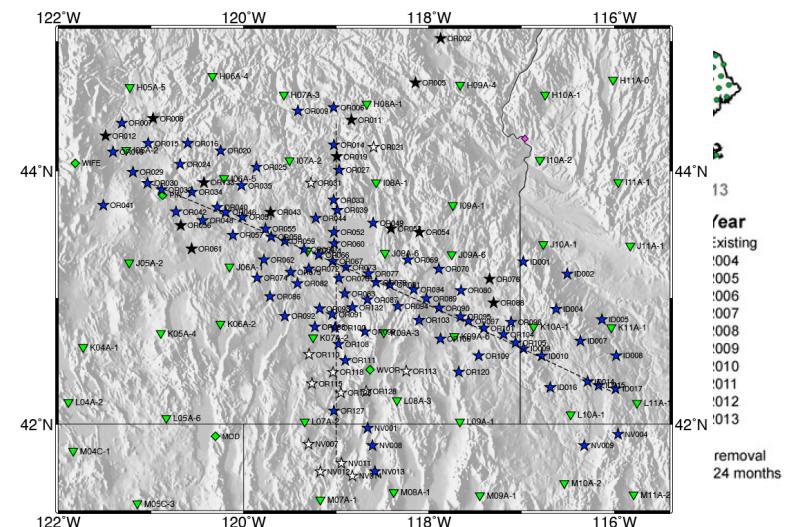
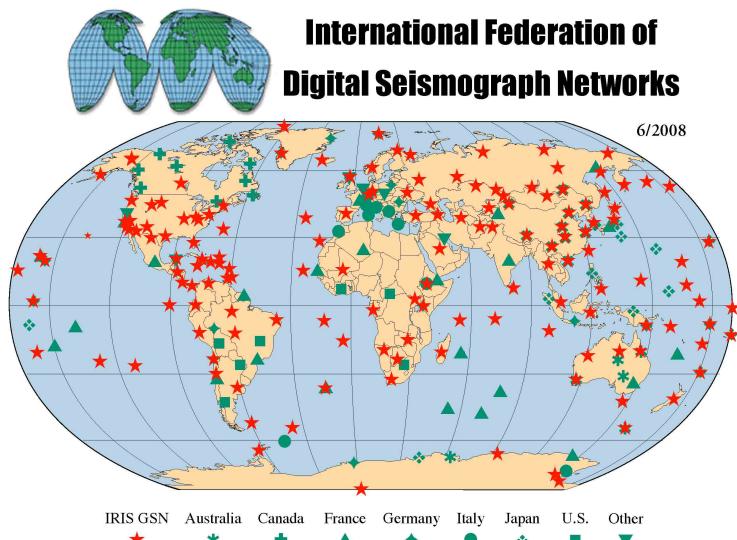
Schlumberger MIT

# Summary

- Examine the applicability of an exploration-oriented, multichannel deconvolution technique to teleseismic data
- Synthetic experiments show the effectiveness of this method for noisy teleseismic recordings.
- Application to the Slave craton array data improves the data processing workflow and increases the number of usable earthquakes.
- An effective, automatic means for processing large amount of data- it does not require ad-hoc regularization; it is achieved naturally by using the noise present in the array data itself.

# Motivation

From global seismic network to dense array experiments



High Lava Plains (HLP) experiment

<http://www.iris.edu/hq/programs/gsn/maps>

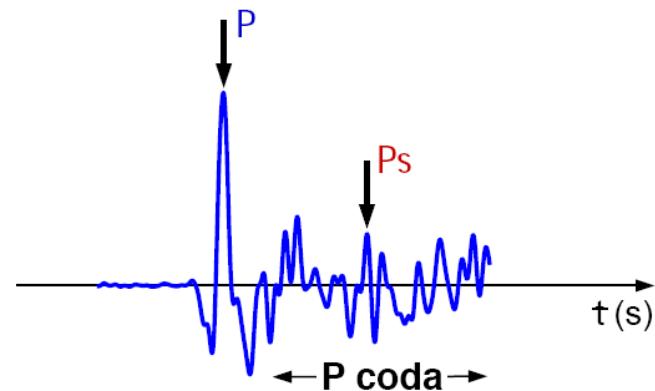
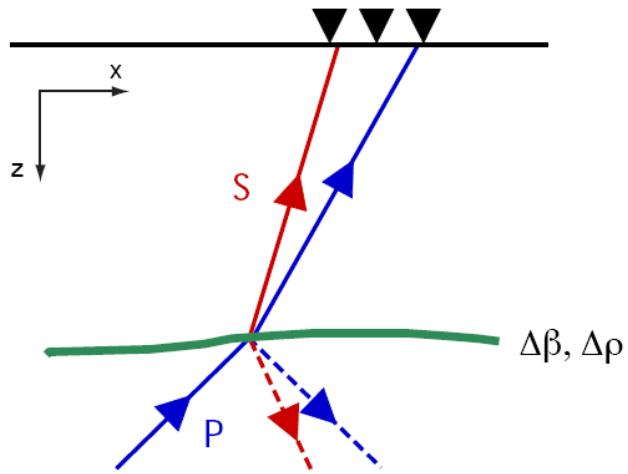
[http://www.iris.edu/USArray/landowners/ta\\_install\\_map.html](http://www.iris.edu/USArray/landowners/ta_install_map.html)

# IRIS PASSCAL funded projects (2008-2012)

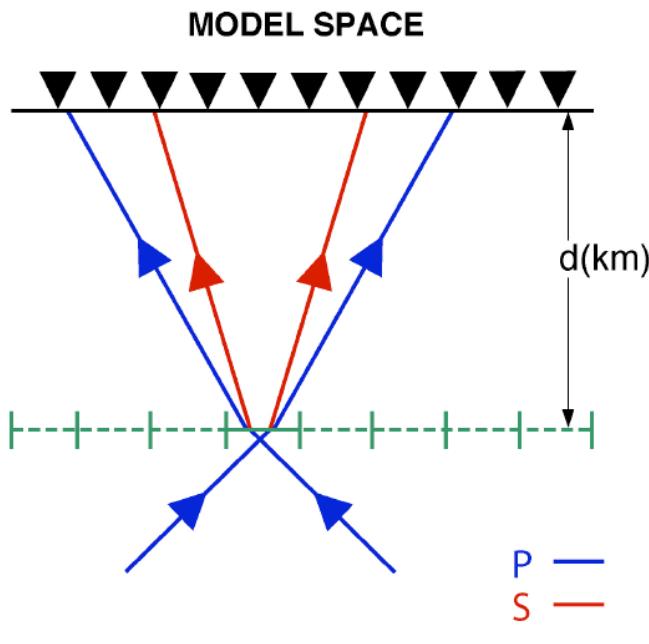


# Receiver function imaging

## Body wave conversions

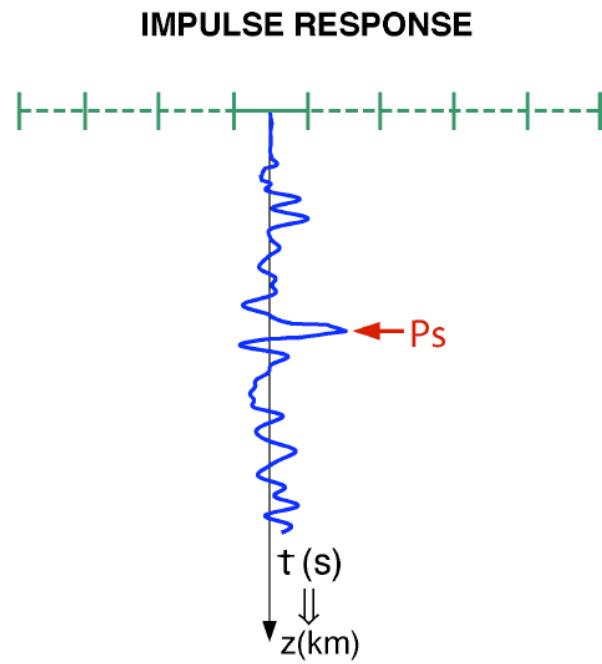


# Receiver function profile



Source normalization (deconvolution)

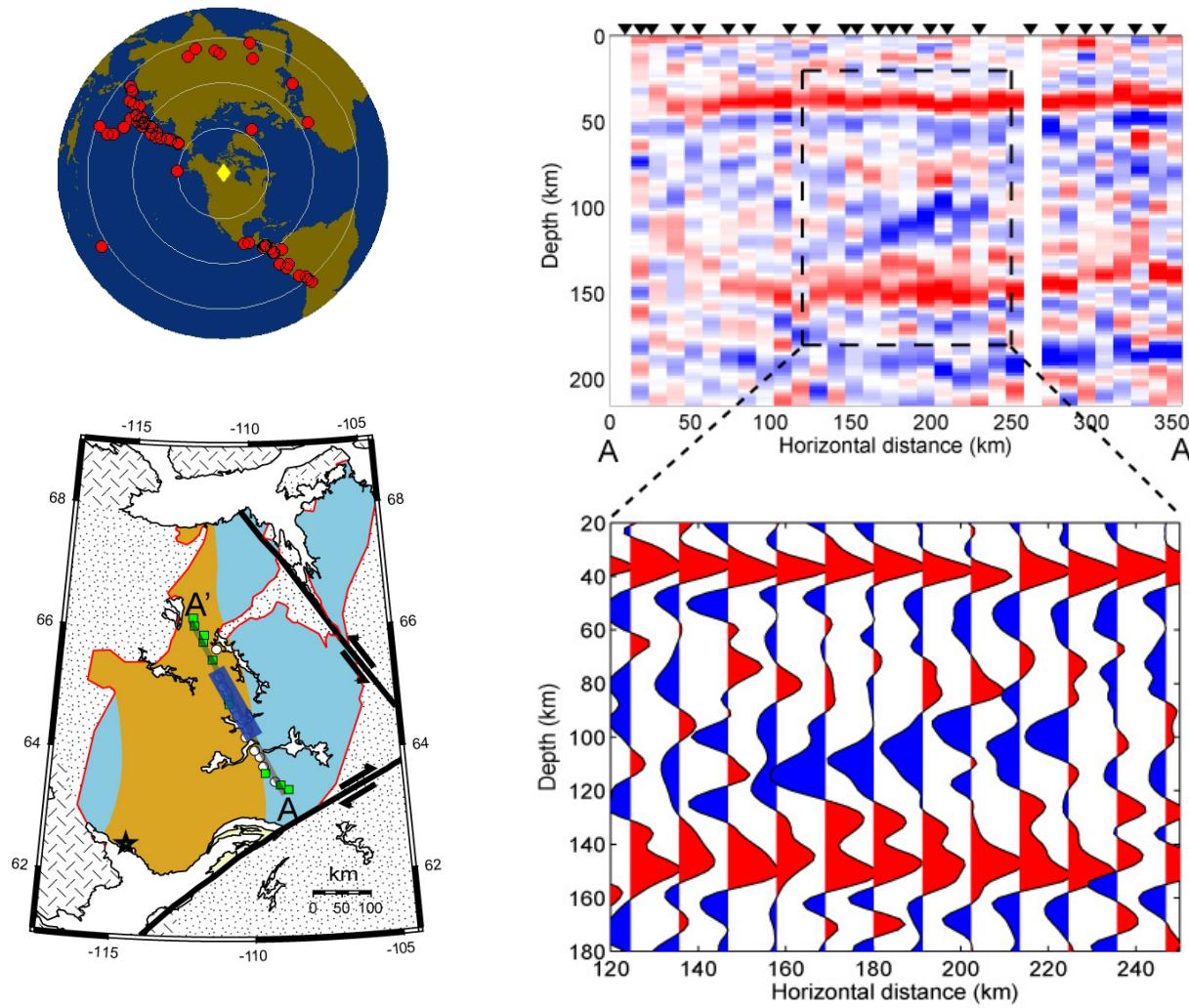
$$\hat{r}(\omega) = \frac{S(\omega)P^*(\omega)}{P(\omega)P^*(\omega) + \delta}$$



Stacking of normalized traces

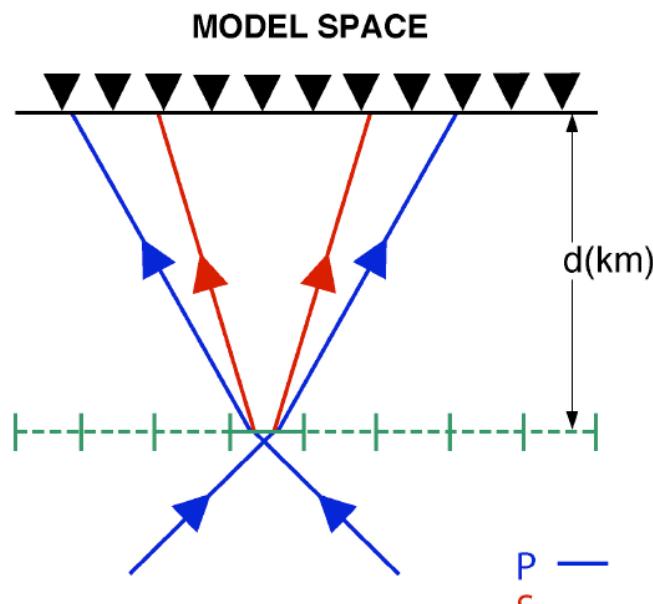
$$R(t) = R(h(t)) = F^{-1} \left[ \sum_{k=1}^N \hat{r}(\omega) e^{i\omega \Delta T_{P_S}(p_k, h(t))} \right]$$

# Receiver function profile: Slave craton



Chen, Rondenay et al. 2009 Science

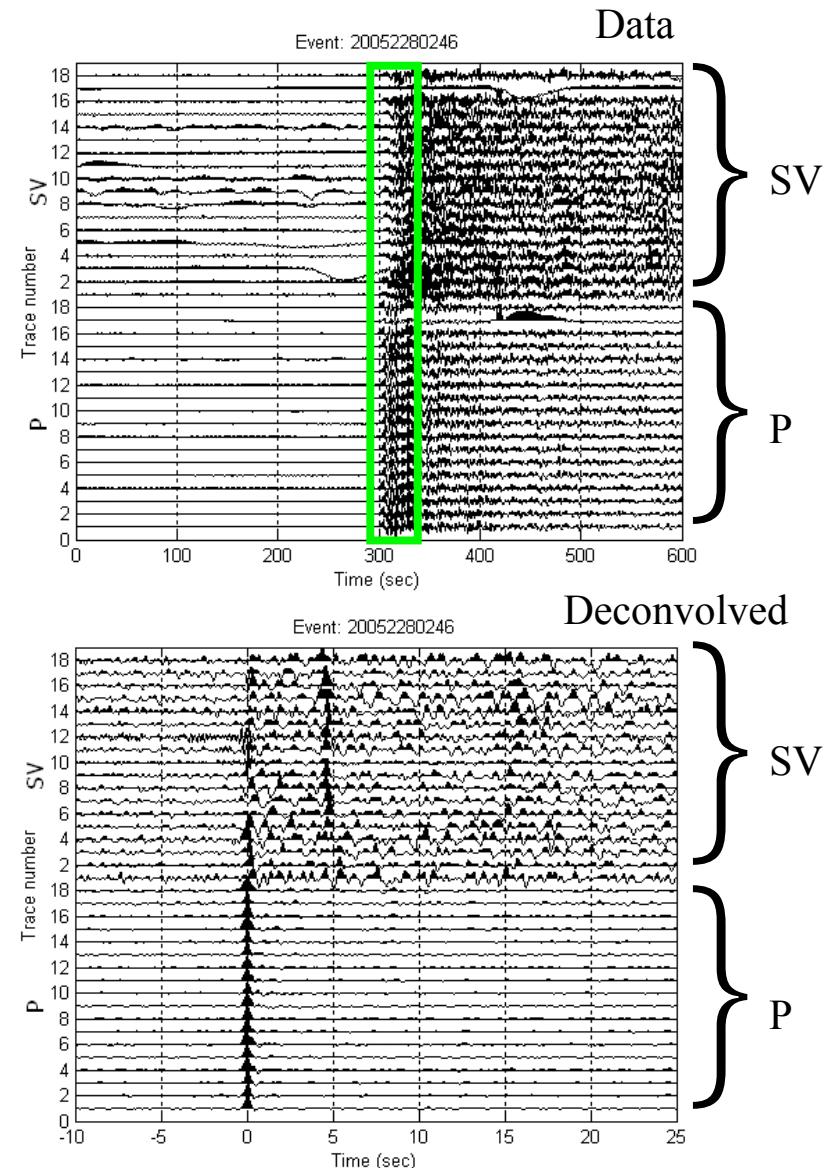
# Receiver function key step: Deconvolution



Source normalization (deconvolution)

$$\hat{r}(\omega) = \frac{w^*(\omega)}{w(\omega)w^*(\omega) + \delta} d(\omega)$$

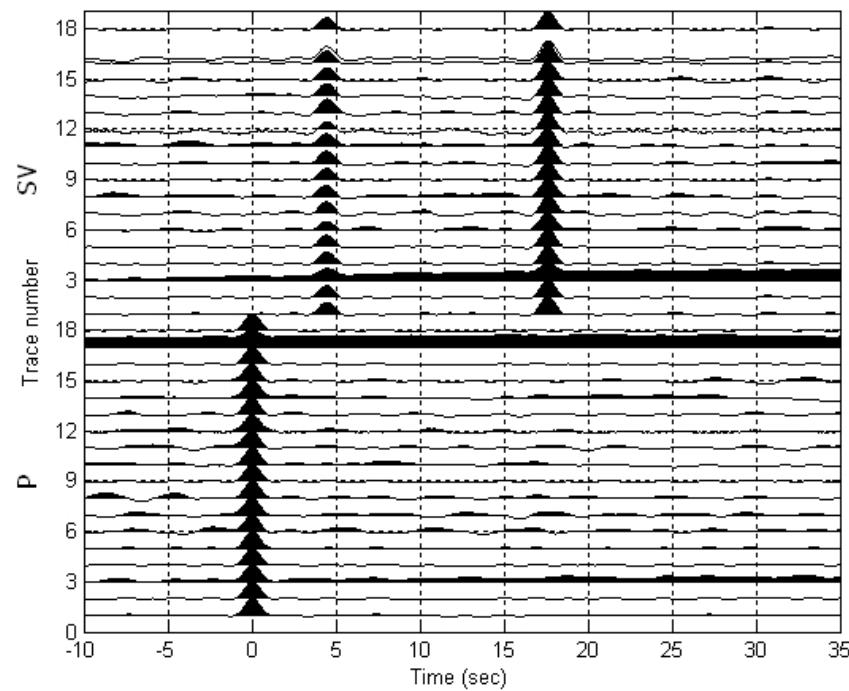
regularization



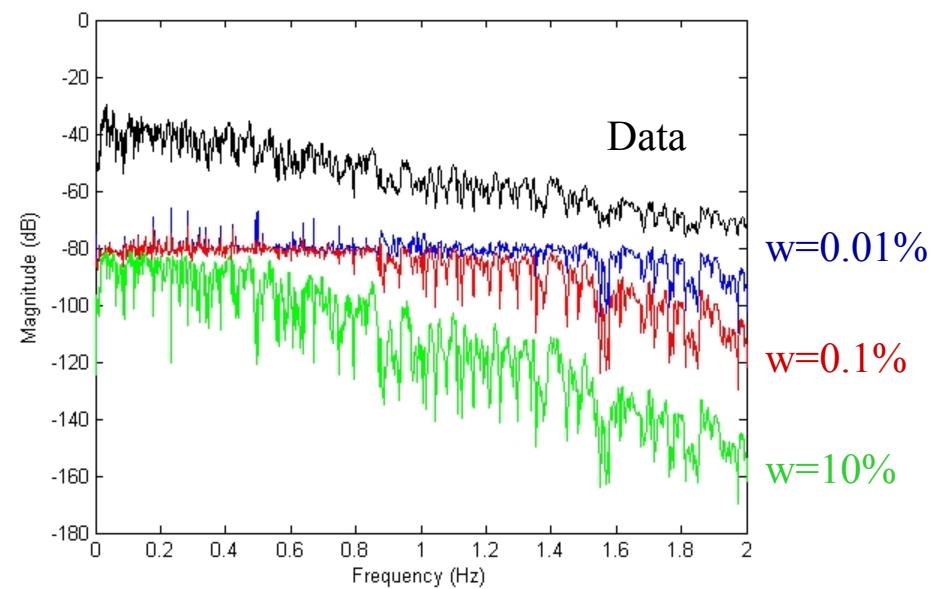
# Waterlevel (Wiener) deconvolution

Deconvolved data

$$\delta = 0.01\%$$



Amplitude spectrum



# Array-conditioned (multichannel) deconvolution

(Haldorsen, Miller & Walsh 1994; for vertical seismic profile)

Data model:

$$d_m(\omega) = w(\omega) + n_m(\omega).$$

To find a deconvolution filter such that

$$W(\omega)d_m(\omega) = 1.$$

The least-squares solution:

$$W(\omega) = \frac{\hat{w}^*(\omega)}{E_T(\omega)},$$

where

$$E_T(\omega) = \frac{1}{M} \sum_{m=1}^M |d_m(\omega)|^2.$$

Some rearrangements:

$$W(\omega) = \frac{\hat{w}^*(\omega)}{|\hat{w}(\omega)|^2} D(\omega), \quad \text{where} \quad D(\omega) = \frac{|\hat{w}(\omega)|^2}{E_T(\omega)}.$$

spiking decon filter      semblance

Semblance: data-adaptive filter that attenuates  
data at frequencies where  
signal-to-noise ratio is small

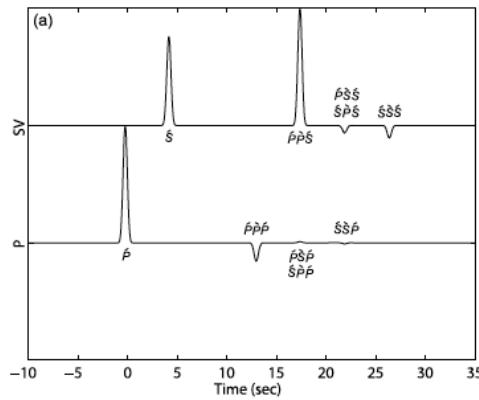
$$\rightarrow W(\omega) = \frac{\hat{w}^*(\omega)}{|\hat{w}(\omega)|^2 + E_N(\omega)}. \quad \text{cf.} \quad \hat{r}(\omega) = \frac{w^*(\omega)}{w(\omega)w^*(\omega) + \delta} d(\omega)$$

where

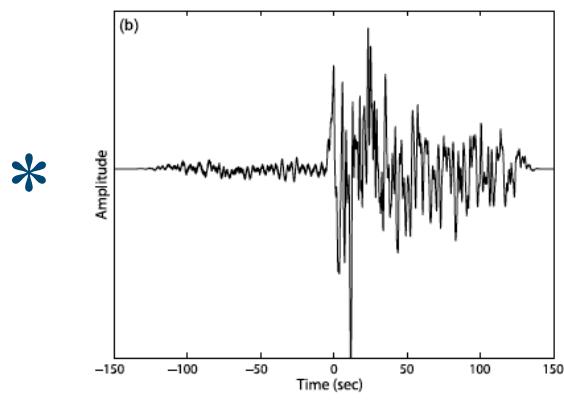
$$E_N(\omega) = \frac{1}{M} \sum_{m=1}^M |d_m(\omega) - w(\omega)|^2.$$

# Making synthetics

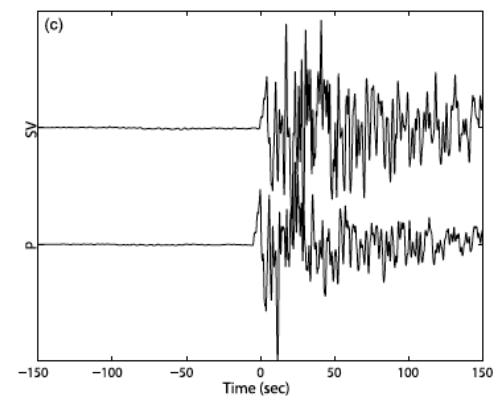
Impulse response



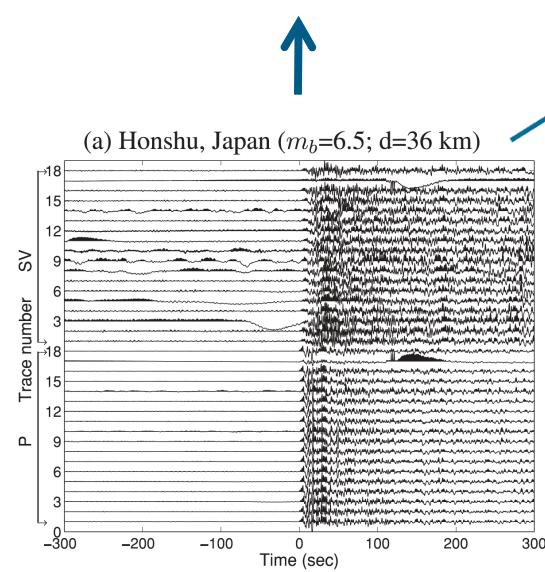
Source signature



'noise-free' synthetics

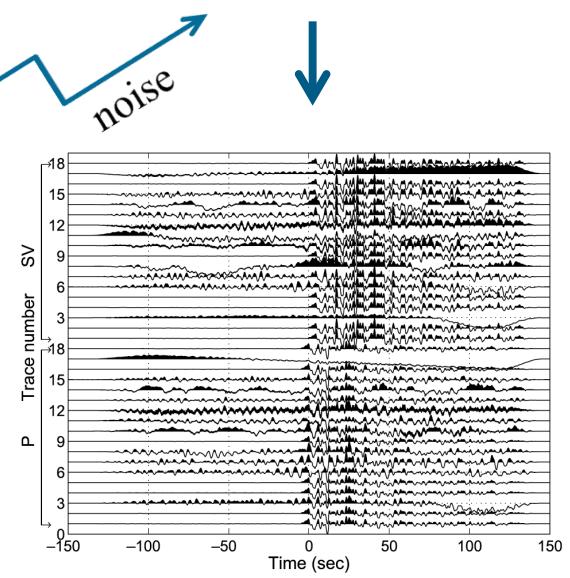


$$d_p(t) = \hat{w}(t) \times g_p(t) + \lambda N_p(t)$$



Chen et al. 2010 GJI

Teleseismic event

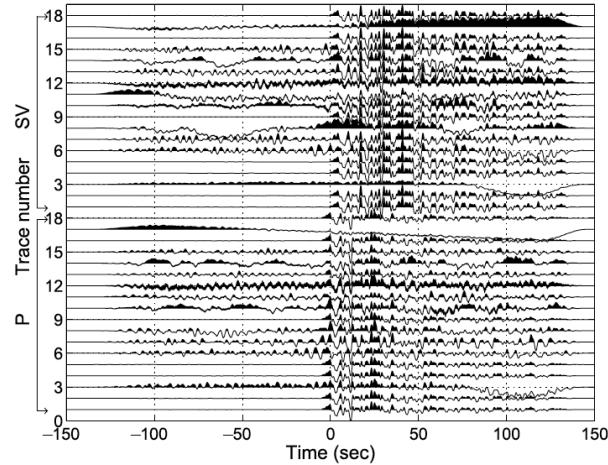


Complete synthetics

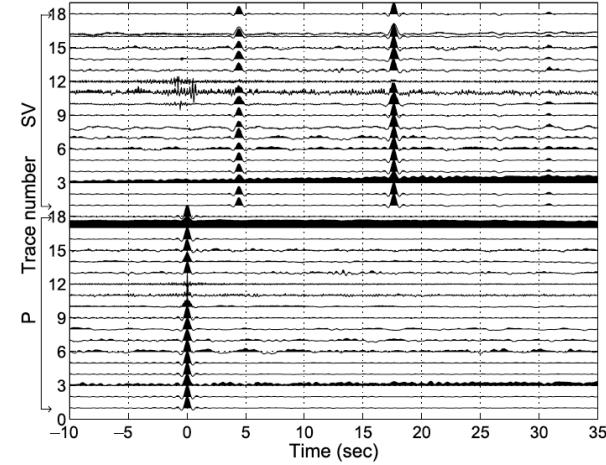
# Synthetics experiments

$$d_p(t) = \hat{w}(t) \times g_p(t) + \lambda N_p(t)$$

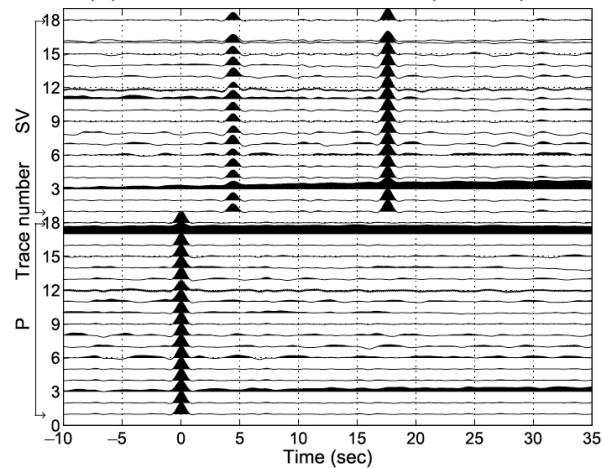
(a) Synthetics  $\lambda = 1$



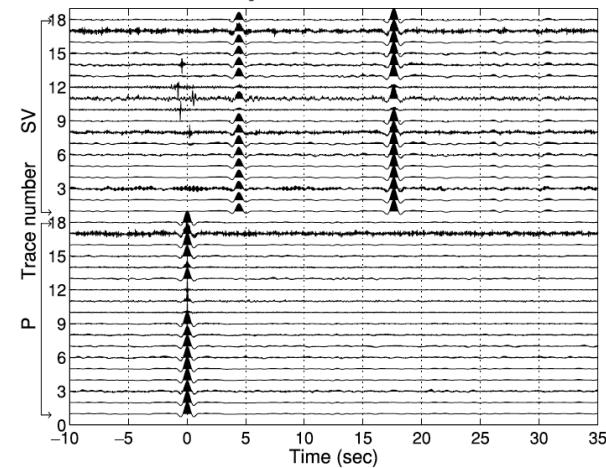
(b) GCV (1.121)



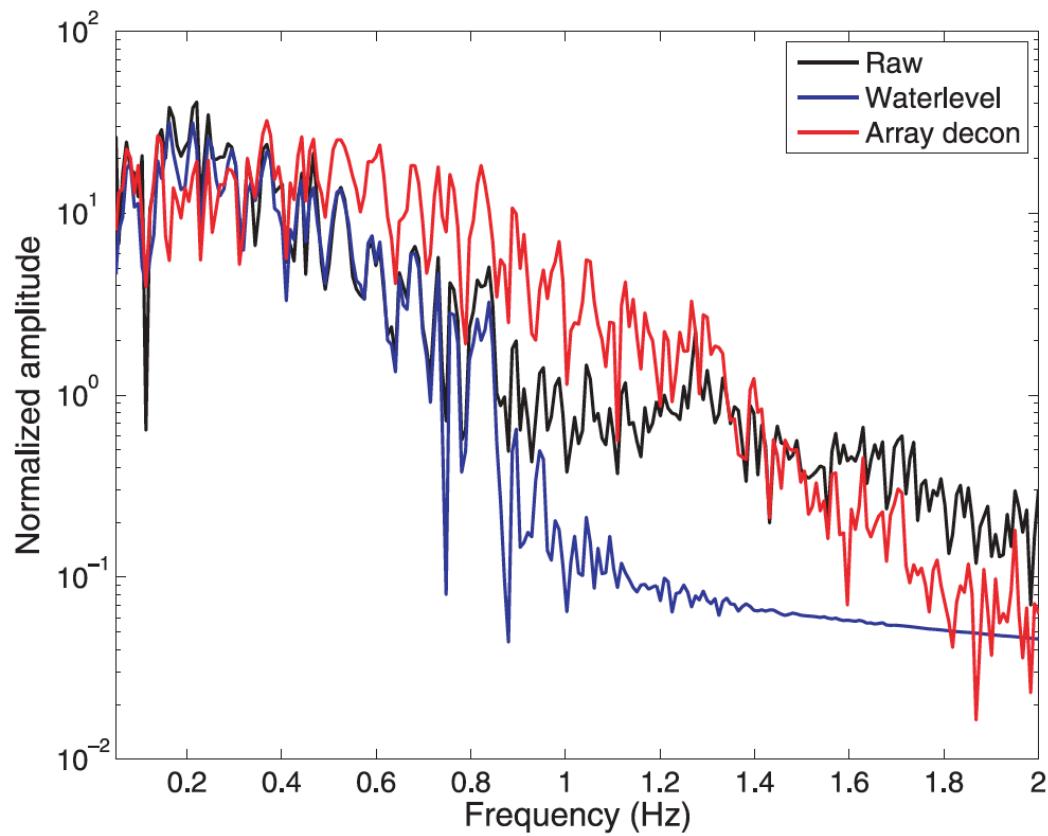
(c) Waterlevel  $\delta = 1\% (0.164)$

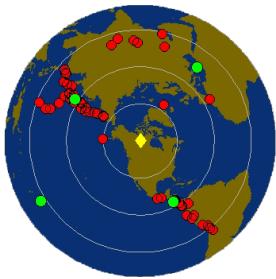


(d) Array decon (0.0003) ← variance



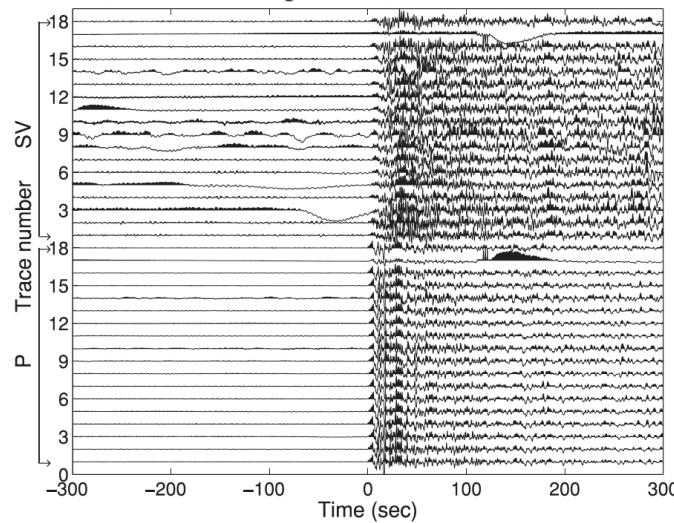
# Spectra of deconvolved traces



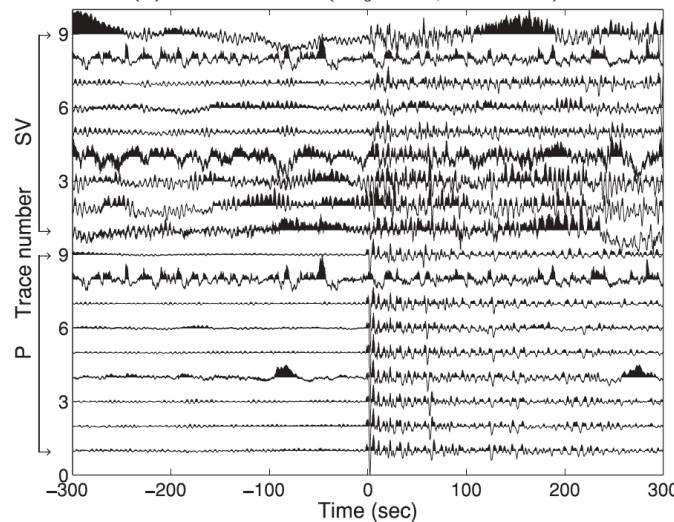


# Data examples

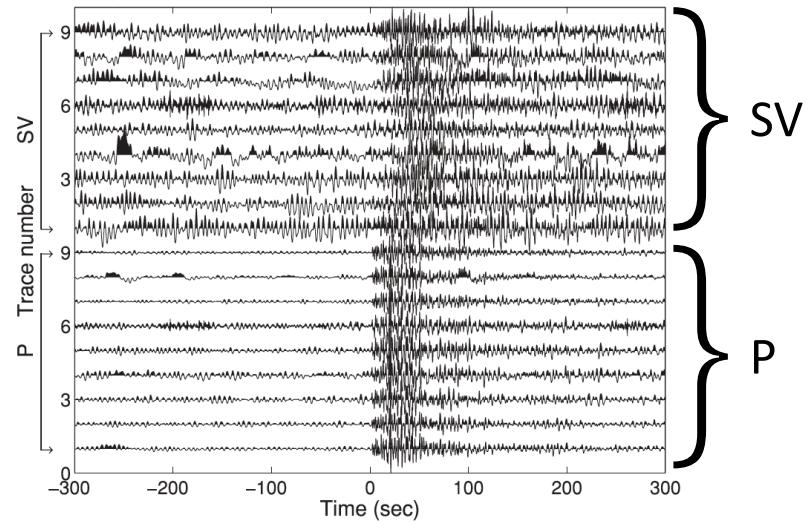
(a) Honshu, Japan ( $m_b=6.5$ ; d=36 km)



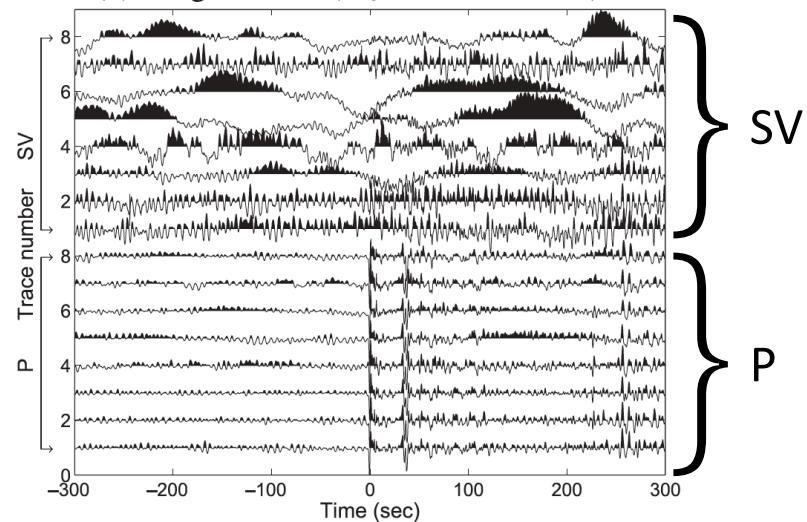
(c) Costa Rica ( $m_b=5.8$ ; d=9 km)



(b) Crete, Greece ( $m_b=5.9$ ; d=25 km)

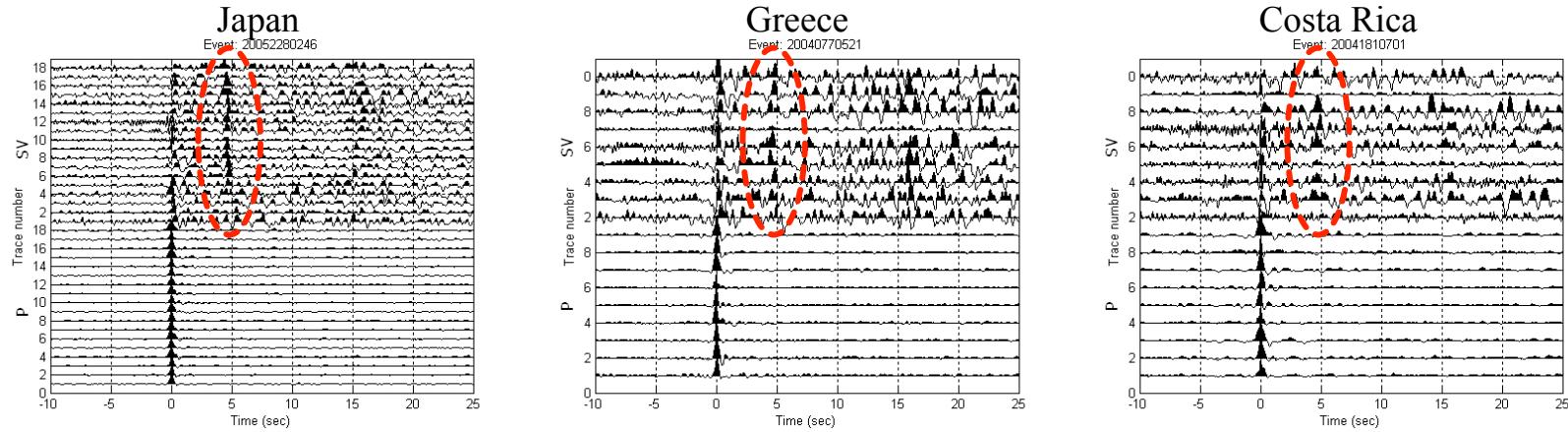


(d) Tonga Islands ( $m_b=6.3$ ; d=130 km)

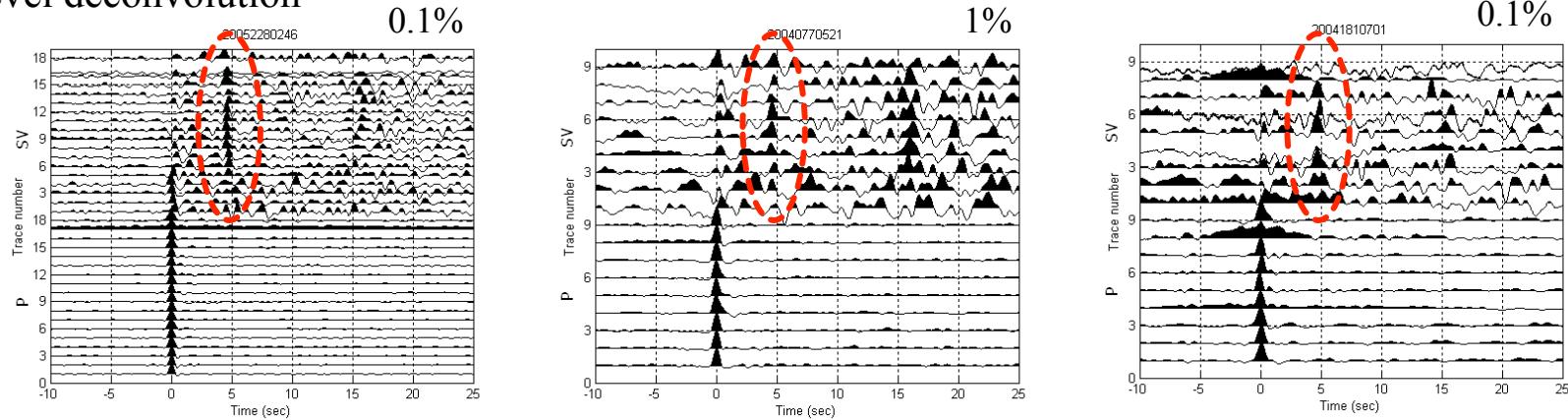


# Deconvolved results

## Array deconvolution

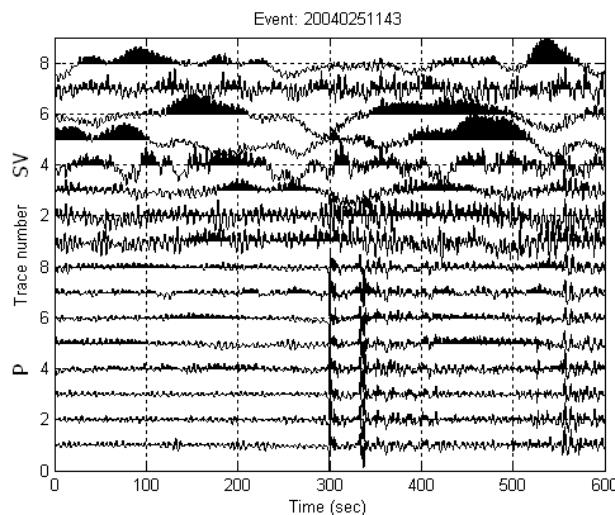


## Waterlevel deconvolution

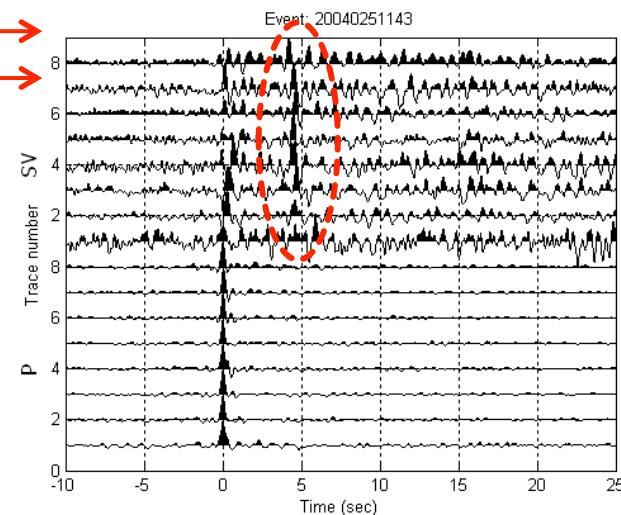


# Deconvolved results

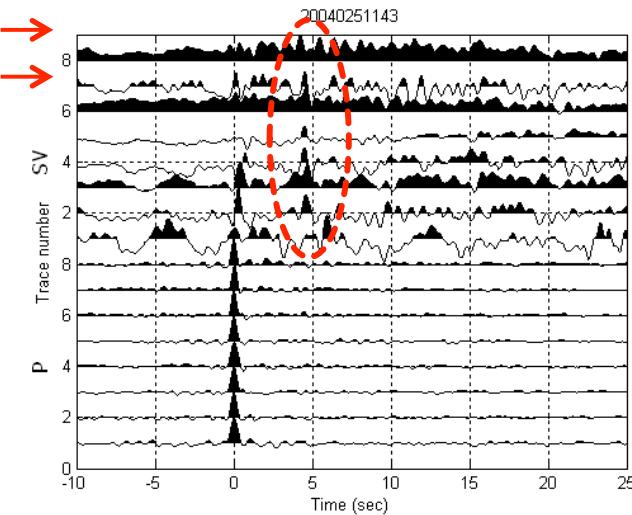
Tonga



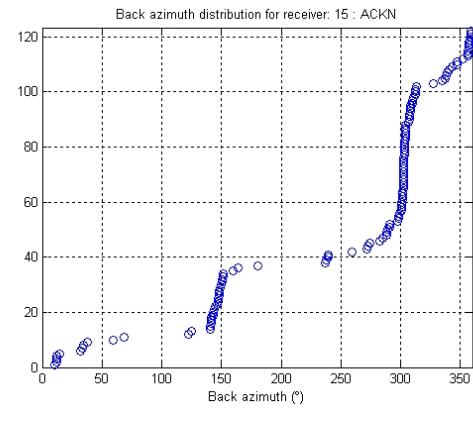
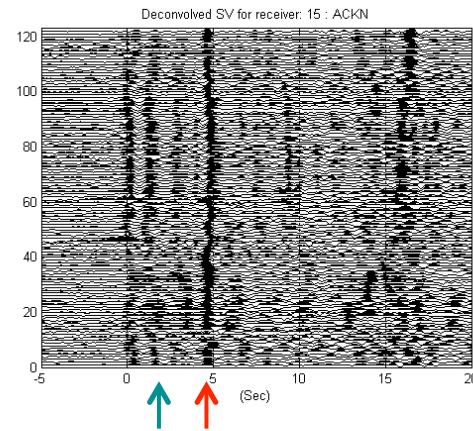
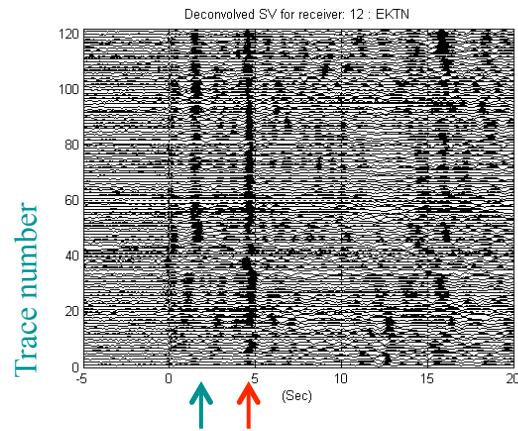
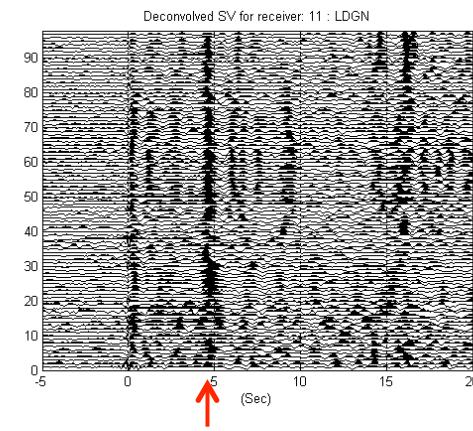
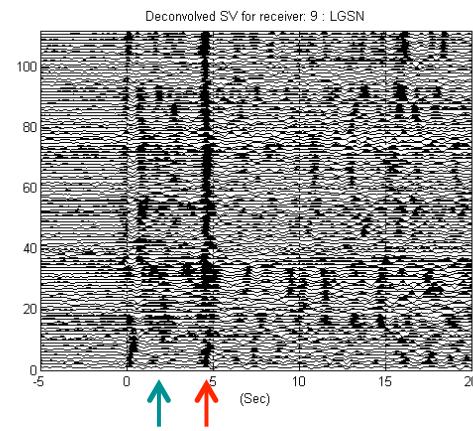
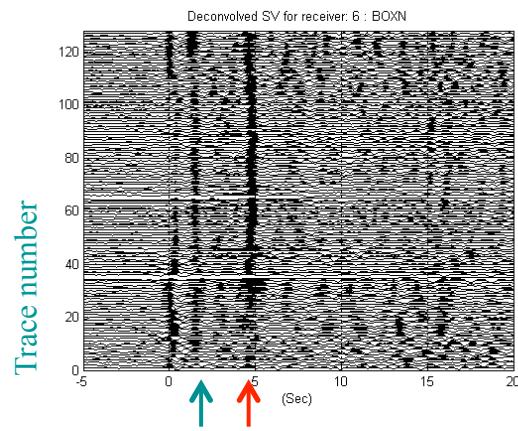
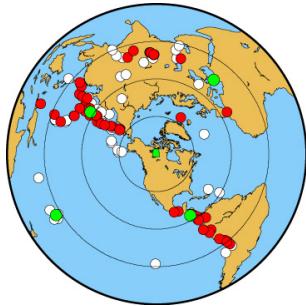
Array decon



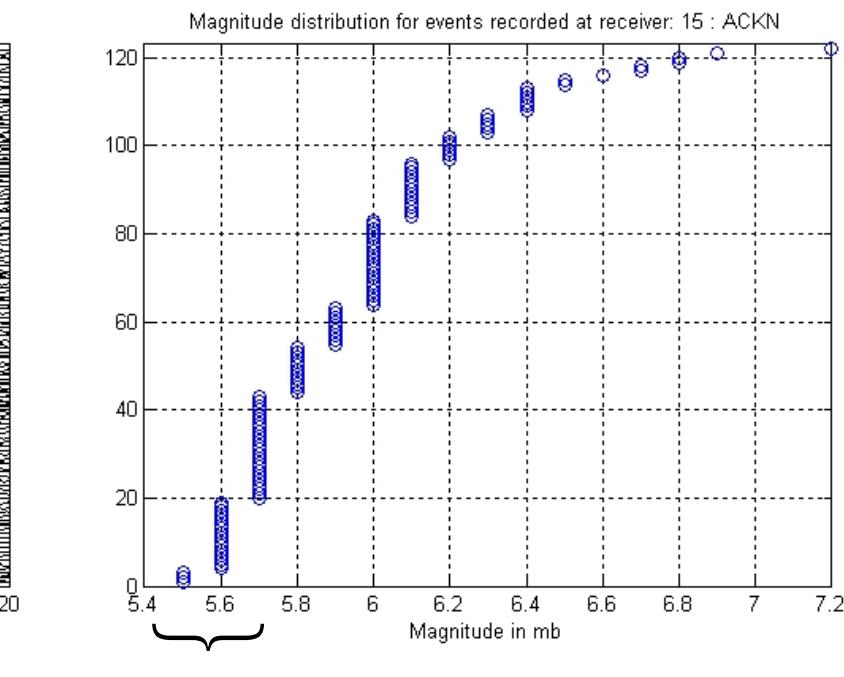
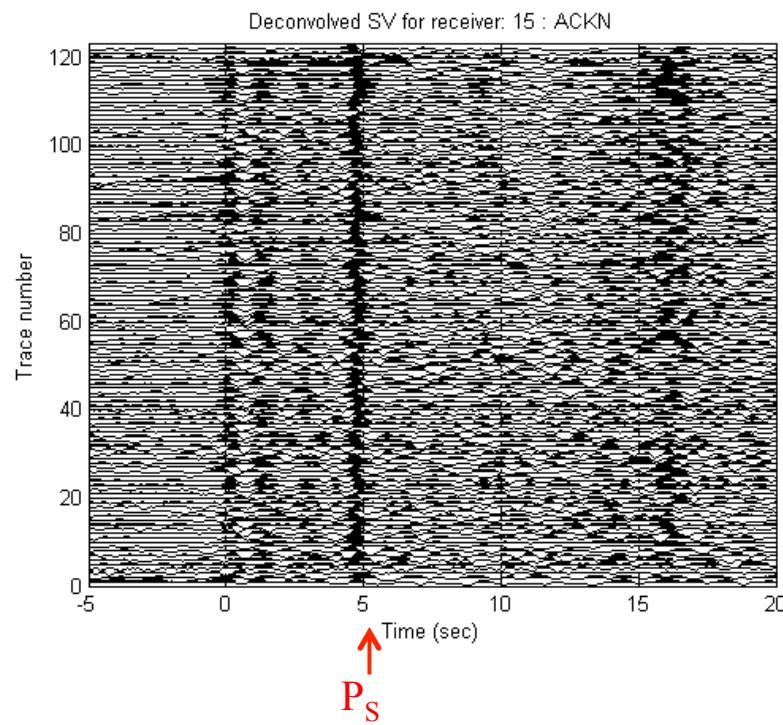
Waterlevel decon (0.01%)



# Deconvolved SV data (w.r.t. backazimuth)



# Deconvolved SV data (w.r.t. magnitude)



Additional usable eqks!

# Conclusions

- Array deconvolution technique constructs an inverse filter that automatically determines and subsequently attenuates the noise from data.
- This technique improves the efficiency and effectiveness of receiver function calculation and data preprocessing workflow.
- Helps to detect small-scale crustal heterogeneities beneath each receiver.
- Suitable for processing large amounts of data, e.g., those from USArray; and for smaller earthquakes.

Chen et al., GJI 182, 2010.