

Anisotropic static and dynamic moduli
measured on shale plugs cut parallel and
perpendicular to bedding

or

Serendipity in the quest for C13

Doug Miller¹, Richard Plumb² and Greg Boitnott³

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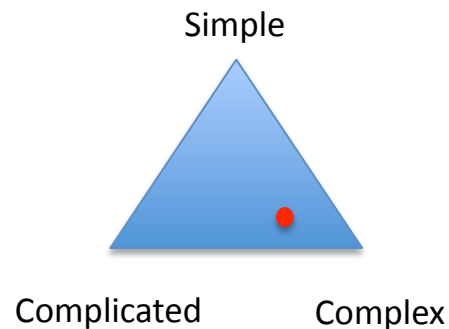
¹ MIT-E.A.P.S., ² Plumb Geomechanics & MIT-C.E.E., ³ New England Research

Serendipity

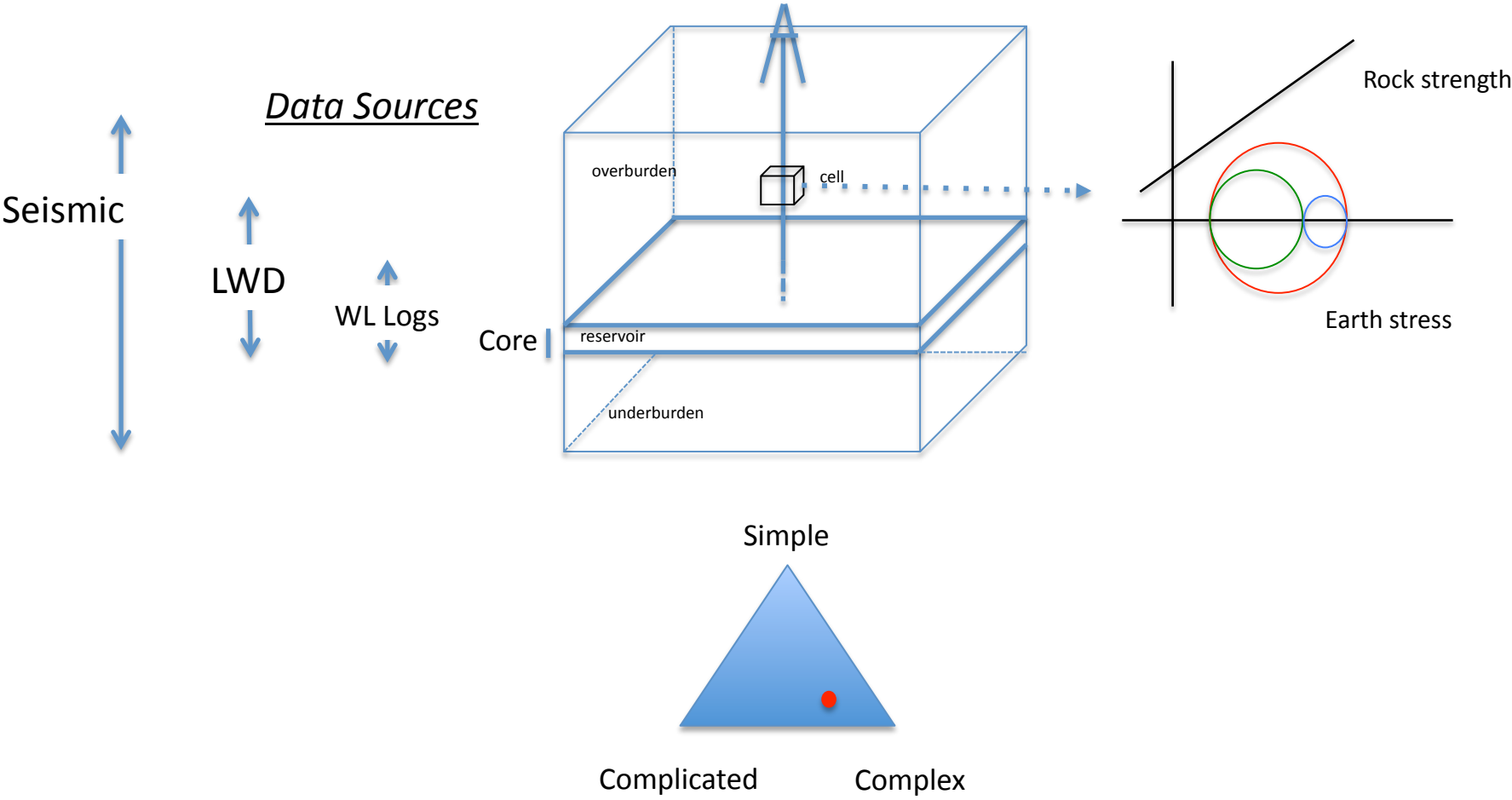
The faculty of finding valuable or agreeable things not sought for

Background/Motivation

- Exploration well-significant NPT due to wellbore instability in a thick shale formation
- No knowledge of the state of stress or rock mechanical properties



Nature of the problem



Serendipity Event#1



Found sample of the problem rock

Shale Sample of Opportunity

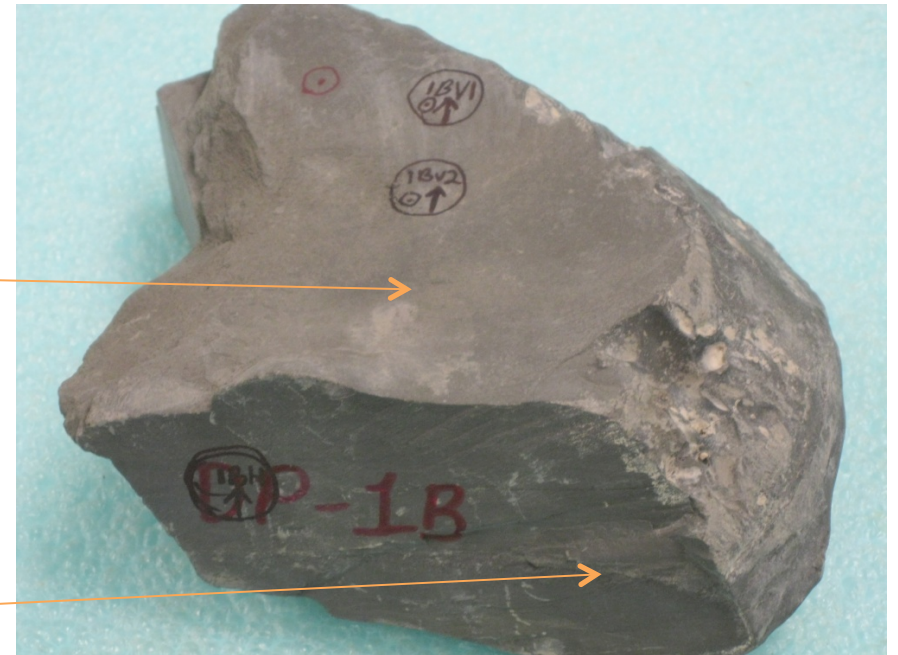


Bedding enhanced by erosion by water

Conchoidal-like fracture surface

1"
scale

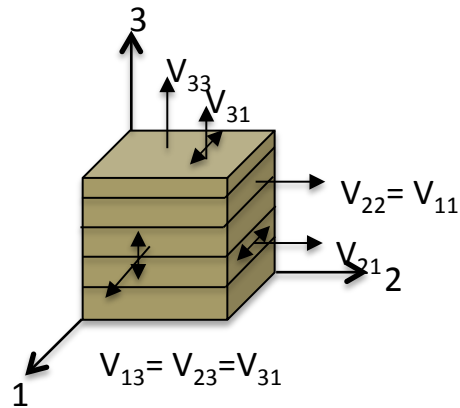
Weak compositional layering



Serendipity Event#2

I shared the experimental data with Doug Miller

TI parameters from ultrasonics

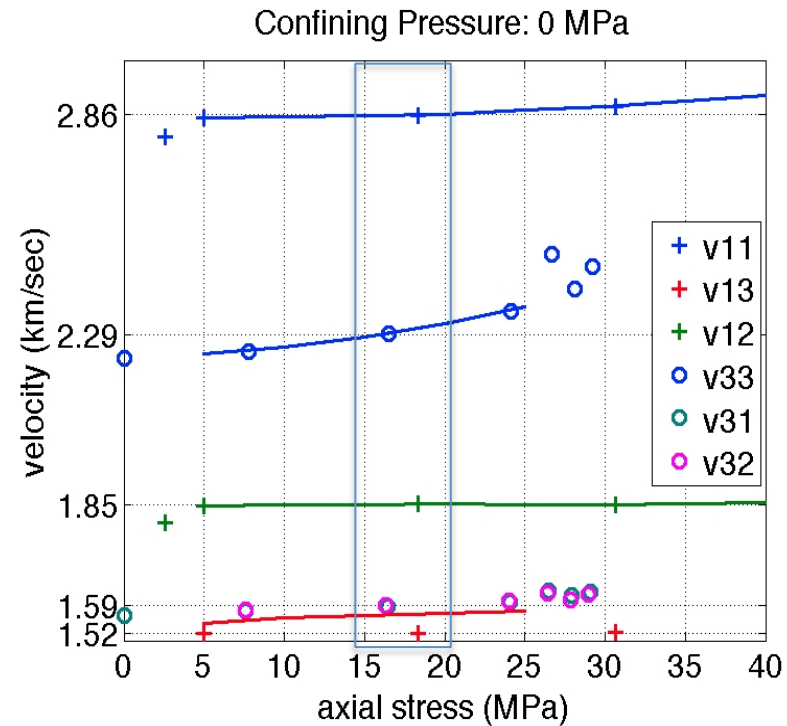


Theory and Measurement

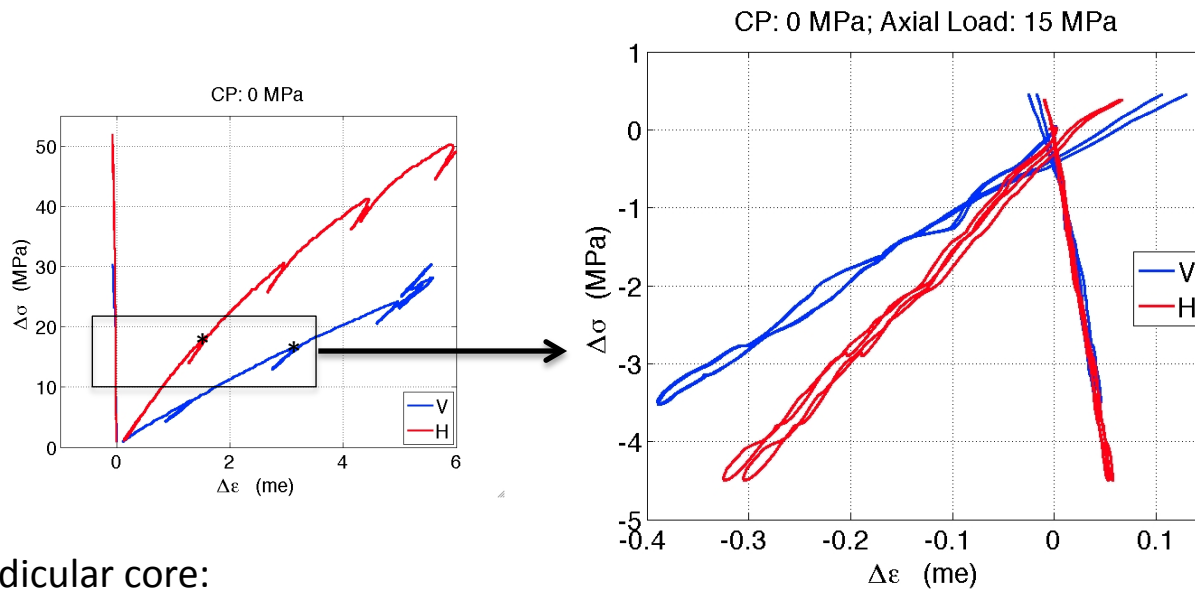
1. $V_{11}^2 = C_{11}/\rho$
2. $V_{33}^2 = C_{33}/\rho$
3. $V_{12}^2 = C_{66}/\rho$
4. $V_{13}^2 = V_{31}^2 = V_{32}^2 = C_{55}/\rho$

For TI symmetry: $C_{12} + 2 C_{66} = C_{11}$.

Thus, ultrasonics determine C_{33} , C_{55} , C_{11} , C_{12} , C_{66} (but not C_{13})



TI parameters from load-unload cycles



Theory:

Perpendicular core:

- axial stress/axial strain = $\sigma_{33}/\epsilon_{33} = 1/S_{33} = E_{33}$
- axial stress/radial strain = $\sigma_{33}/\epsilon_{11} = 1/S_{13} = E_{33}/\nu_{33}$

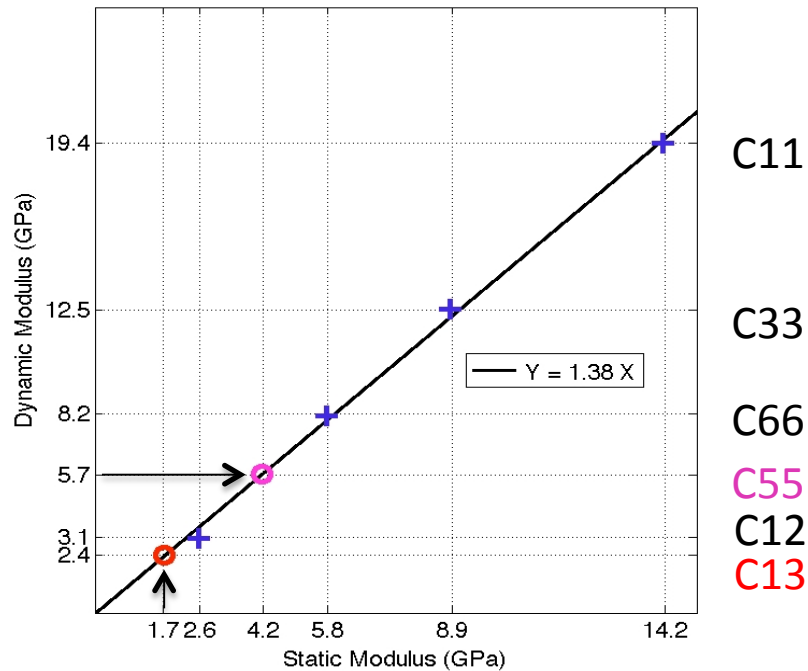
Parallel core

- axial stress/axial strain = $\sigma_{11}/\epsilon_{11} = 1/S_{11} = E_{11}$
- axial stress/radial strain@45° = $2 \sigma_{11}/(\epsilon_{33} + \epsilon_{11}) = 2/(S_{13} + S_{12})$

Observe in this case: $1/S_{12} = 2/(S_{13} + S_{12})$, hence $S_{12} = S_{13}$.

Statics determine S_{33} , S_{13} , S_{11} , S_{12} , & thence C_{33} , C_{13} , C_{11} , C_{12} , C_{66} (but not C_{55})

Combined Methods



- Elastostatics determine: C33, C13, C11, C12, C66 (but not C55)
- Ultrasonics determine: C33, C12, C55, C66 (but not C13)
- Doubly determined parameters are proportional:
Dynamic = 1.38 x Static
- *Singly determined moduli can be predicted by rescaling.*

Moduli	C11	C13	C33	C55	C66	C12
Ultrasonics	19.4	2.4	12.5	5.7	8.2	3.1
Elastostatics	14.2	1.7	8.9	4.2	5.8	2.4
Dynamic Stat x 1.38	19.5	2.4	12.2	5.7	8.0	3.3
Static	14.1	1.7	9.1	4.1	5.9	2.3

Conclusions

- The shale is anisotropic w.r.t. elastic moduli and compressive strength-consistent with TI symmetry
- Dynamic elastic moduli are systematically greater than the static moduli determined from small stress unloading cycles.
- There was a remarkably strong correlation between the static and dynamic moduli on this shale
- Consequently the two plug method enabled determination of *static* and *dynamic* values of all 5 TI parameters
- A fruitful research topic is understanding the physics governing the difference between the static/dynamic modulus of shale.

Acknowledgements

- Hunt Oil Dallas for permission to present this rock mechanics data
- New England research for conducting the laboratory measurements and preliminary rock characterization