

# Fluctuations and Correlations in Nuclear Collisions

-

## Results and Opportunities

Gunther Roland - MIT

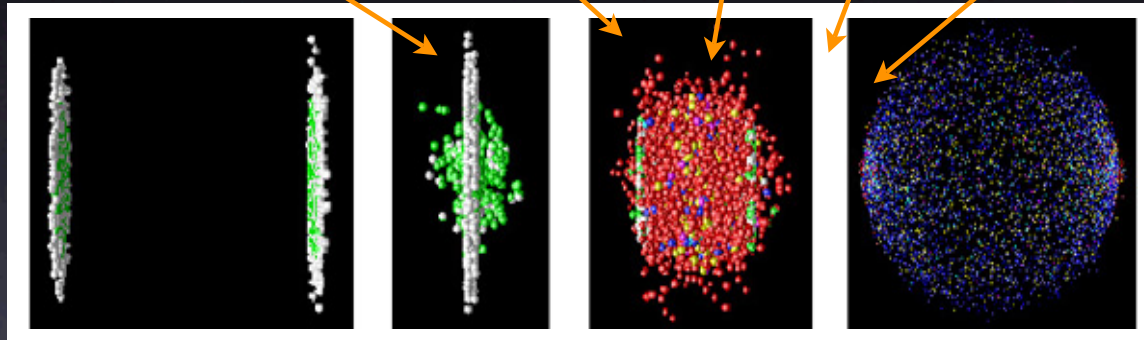
STAR Collaboration Meeting

BNL

March 3 2006

# What can we learn from fluctuations?

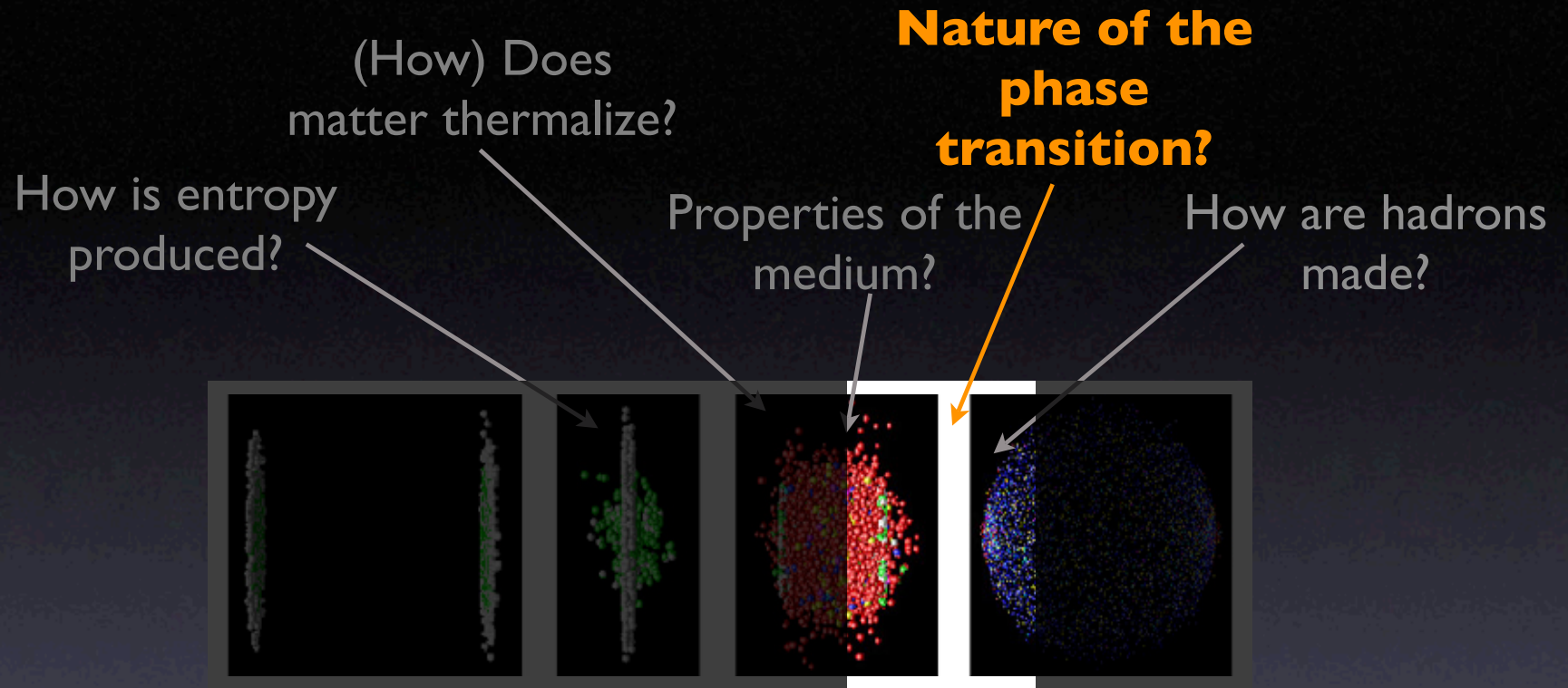
(How) Does matter thermalize?  
Nature of the phase transition?  
How is entropy produced?  
Properties of the medium?  
How are hadrons made?



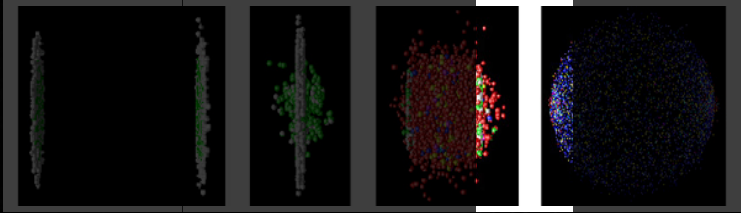
Unique answers to all of these questions from fluctuations/correlations

*How far have we come trying to realize this promise?*

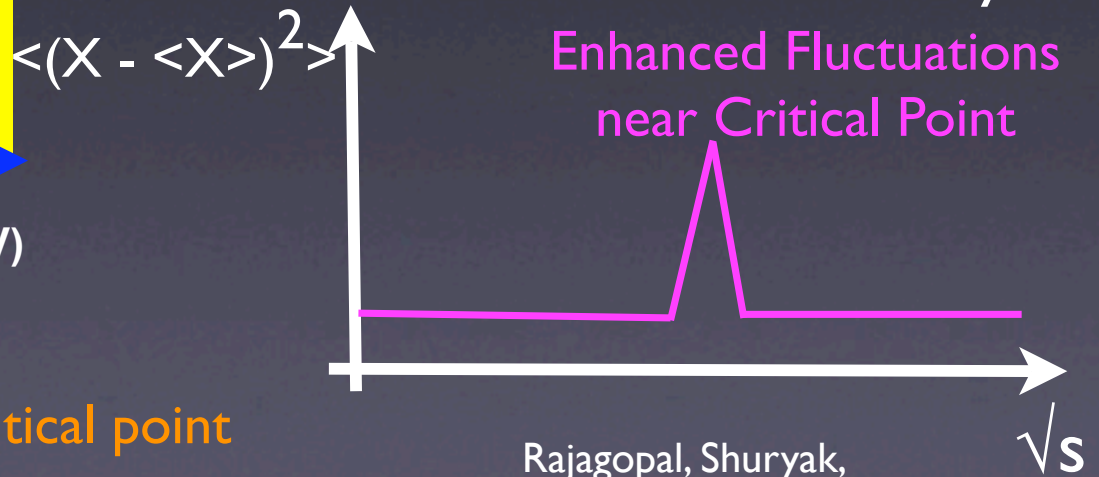
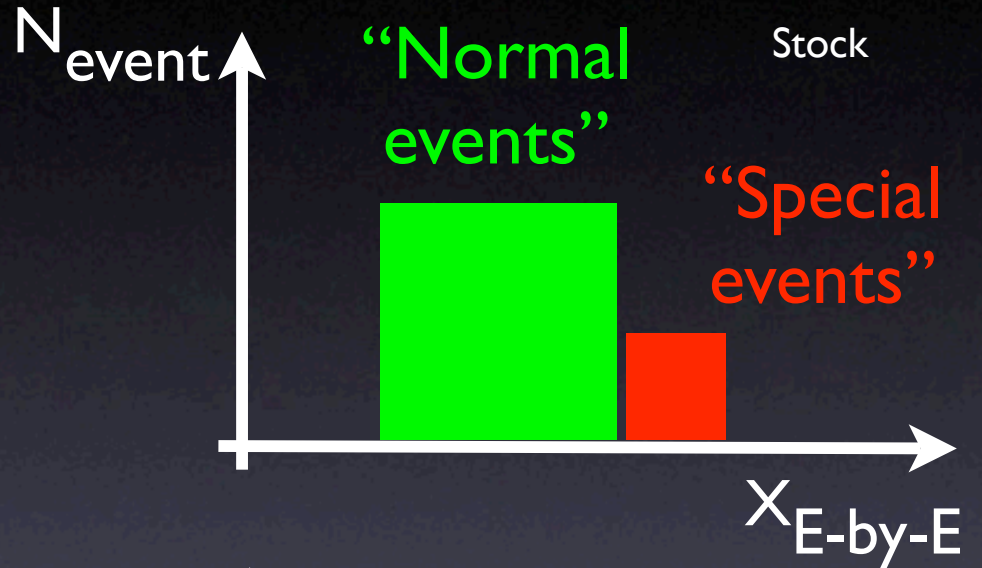
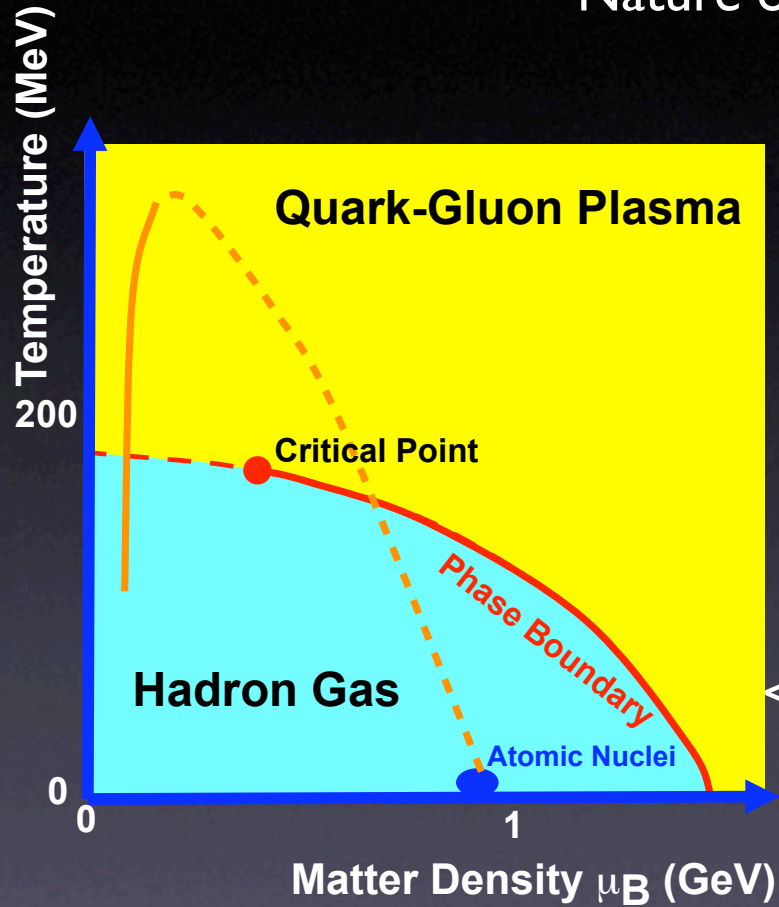
# What can we learn from fluctuations?



ca 1995

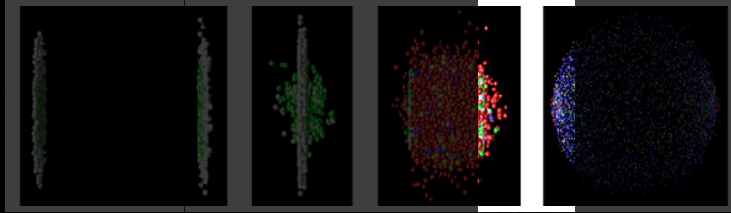


Nature of the Phase Transition

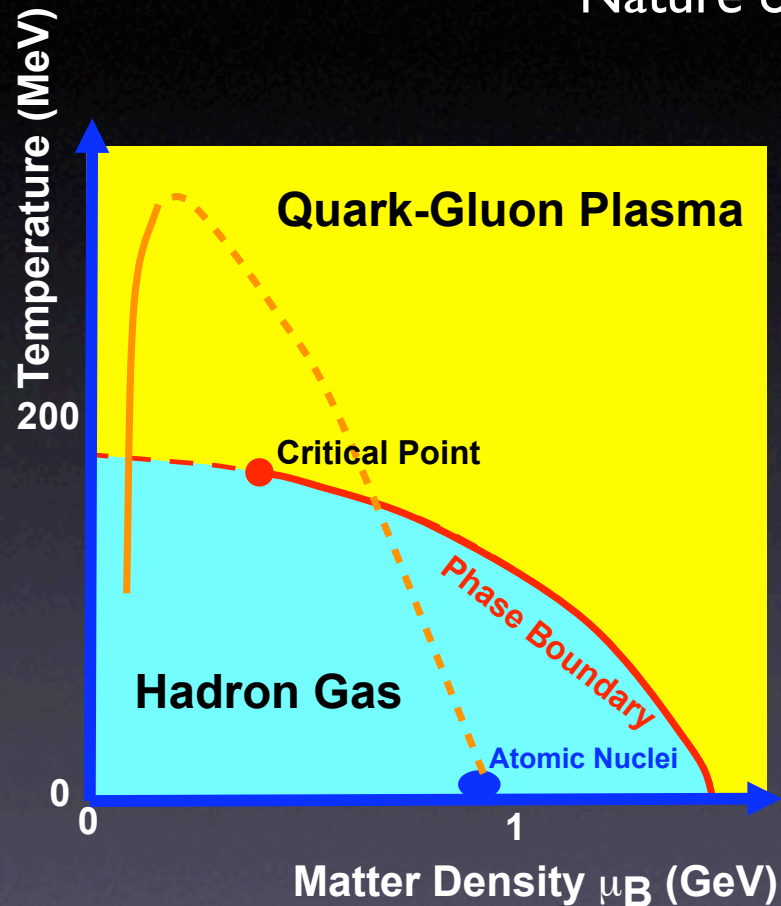


Search for critical phenomena induced near phase transition/critical point

Rajagopal, Shuryak, Stephanov, Wilczek



Nature of the Phase Transition



- Phase transition/Latent heat

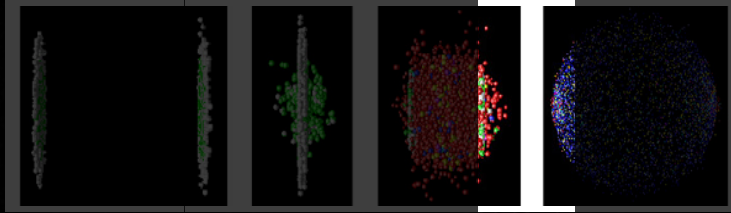
- Supercooling Mishustin
- Droplet Formation
- $\langle pT \rangle$ , Multiplicity Fluctuations

- Location of critical point

- $\langle pT \rangle$  Fluctuations Rajagopal, Shuryak,  
Stephanov, Wilczek

- Chiral Symmetry Restoration

- DCC formation Rajagopal, Wilczek  
Bjorken
- Charge/neutral fluctuations

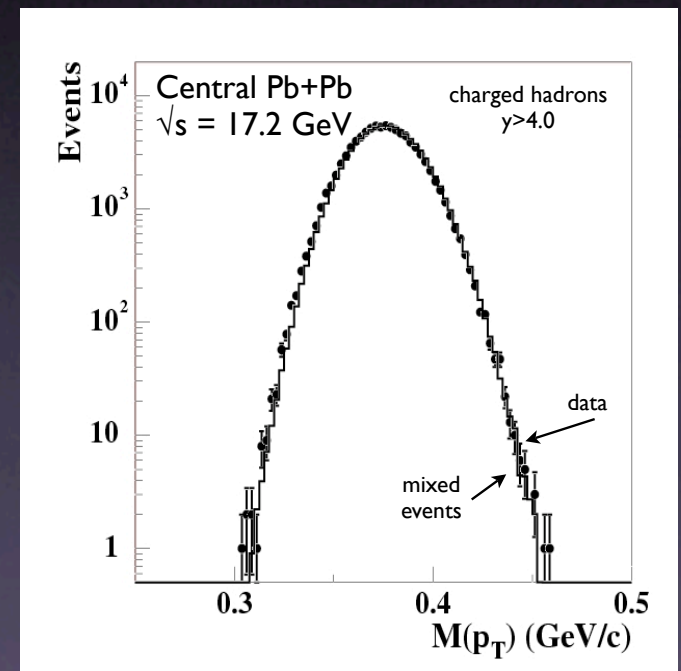


## Nature of the Phase Transition

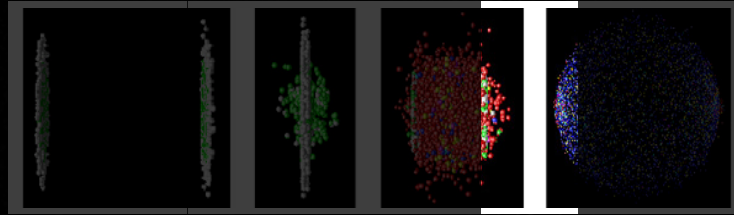
### $\langle p_T \rangle$ Fluctuations

- $p_T$  - simple observable (supposedly...)
- High statistical precision:
  - $\sigma_{p_T}/\langle p_T \rangle_{inc} < 0.1\%$
- Sensitive to many interesting scenarios
  - Critical Point
  - DCC production
  - Droplet formation
  - **Any non-statistical, momentum-localized process**

NA49, Phys Lett B459 (1999) 679

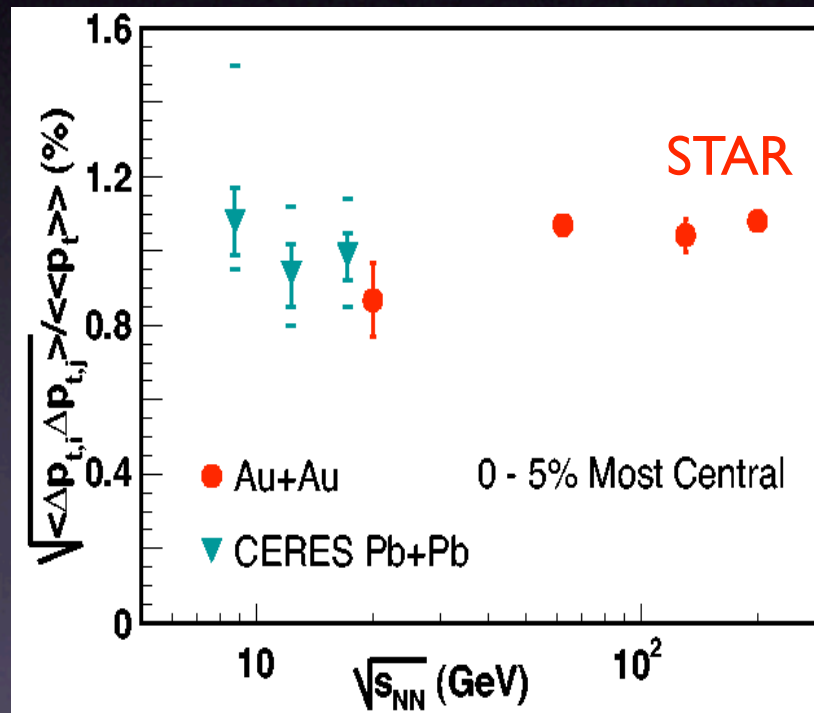


Event-by-event  $\langle p_T \rangle$  compared to stochastic reference (mixed events)

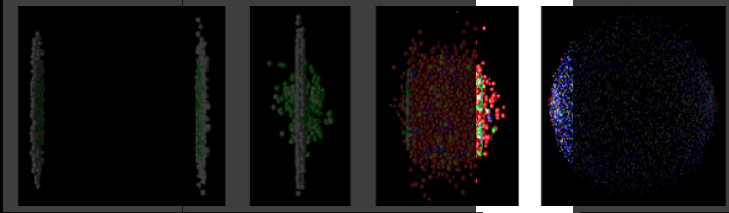


Nature of the Phase Transition

$\langle p_T \rangle$  Fluctuations



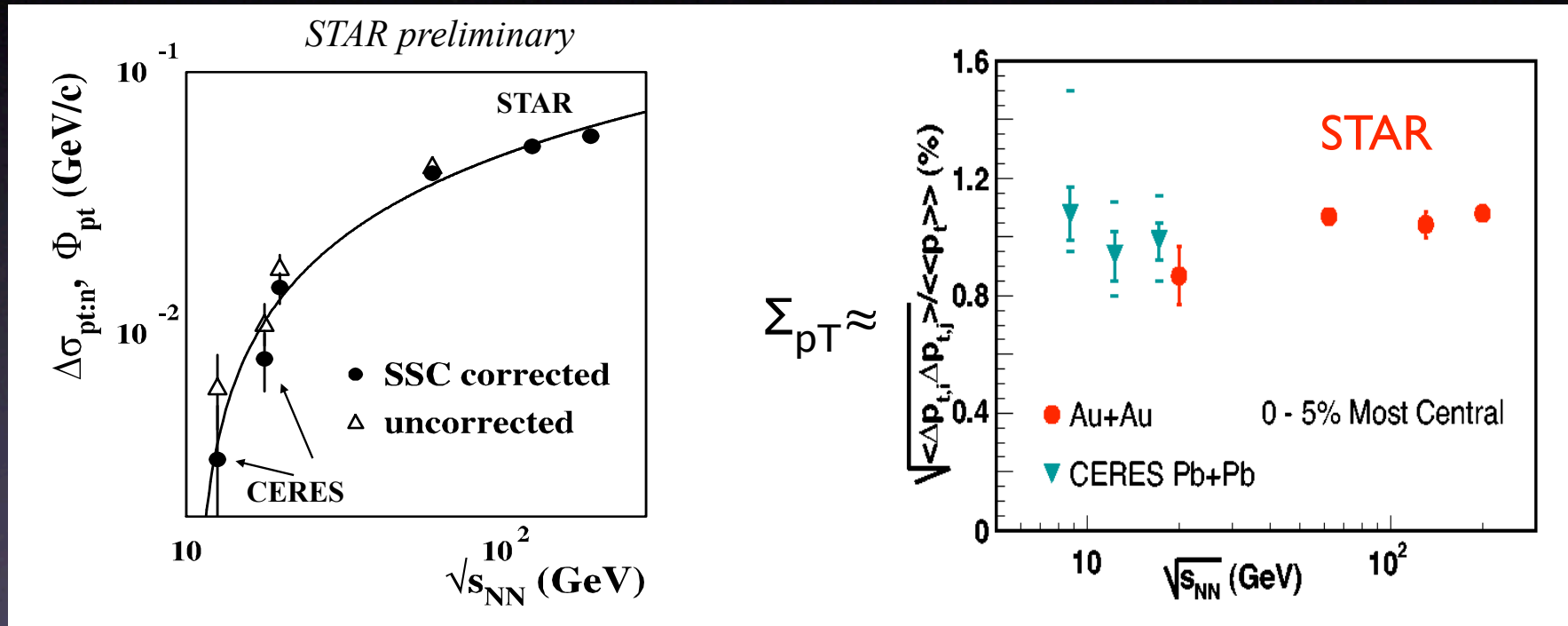
No evidence for non-monotonic energy dependence  
 But: Interpretation  $\Leftrightarrow$  choice of variables



Nature of the Phase Transition

## $\langle p_T \rangle$ Fluctuations

Scaling: Connection between  $\langle p_T \rangle$ ,  $N$ , fluctuations?

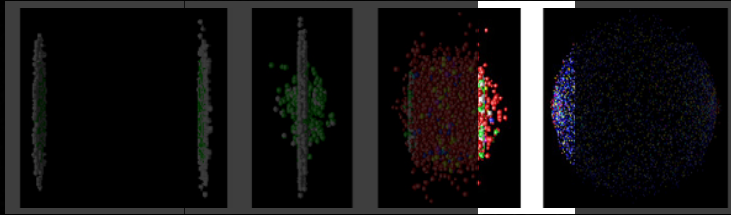


Connection to  
2-particle  
correlations

Normalization to  $\langle p_T \rangle$

Normalization per particle  
Linear or quadratic measures

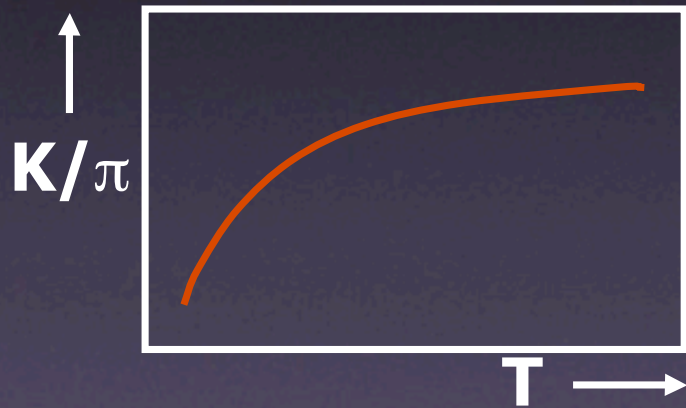
$$\Sigma_{p_T} \approx \sqrt{\frac{2\Phi_{p_T} \sqrt{\sigma_{\hat{p}_T}^2}}{N \bar{p}_T^2}}$$



Nature of the Phase Transition

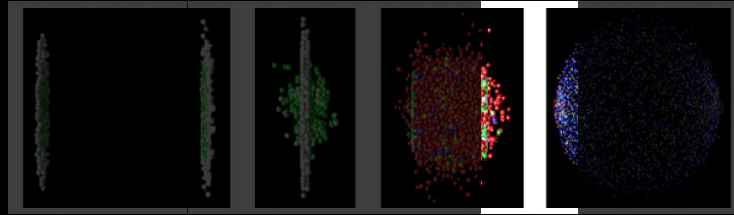
## $K/\pi$ Fluctuations

- Is strangeness enhanced in every event?
- Can we see signs of super-cooling below  $T_{\text{crit}}$ ?



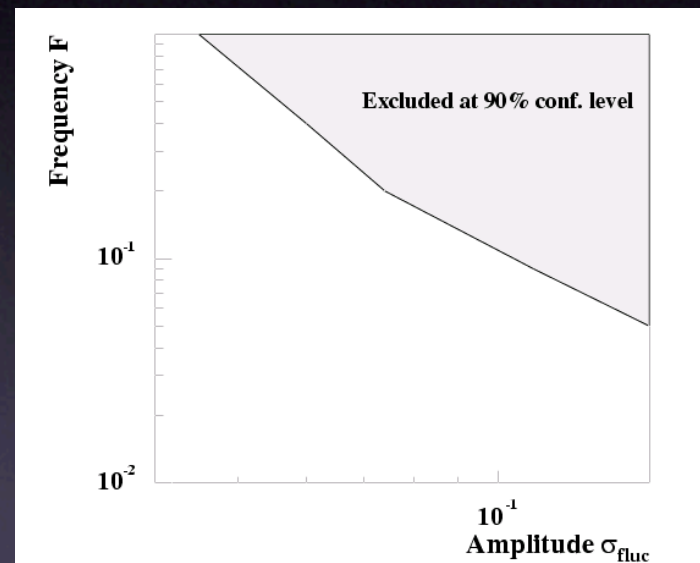
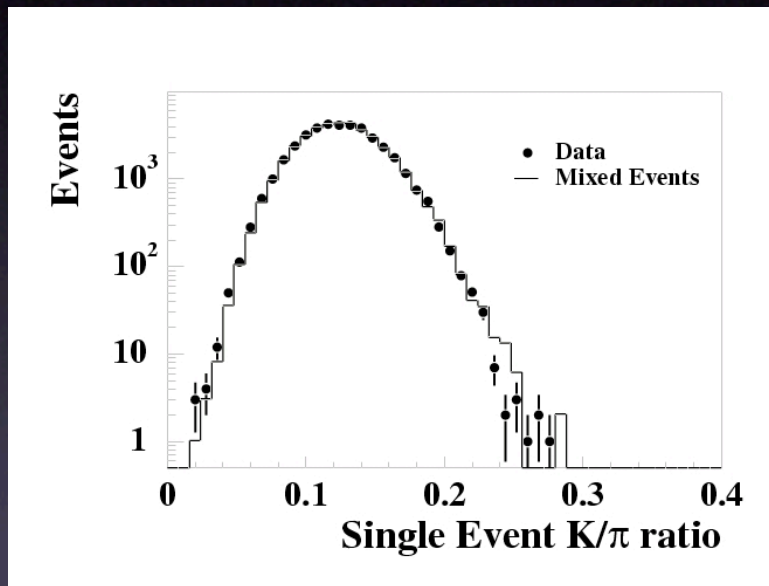
### NA49 Measurement

- Use  $dE/dx$  to identify  $\pi, K, p$  event-by-event
- Do Max Likelihood fit to extract  $K/\pi$  ratio event-by-event
- Required 2 years of detector calibration to eliminate  $dE/dx$  – multiplicity correlation



## Nature of the Phase Transition

## K/ $\pi$ Fluctuations Pb+Pb, 17.2 GeV NA49, PRL 86 (2001) 1965

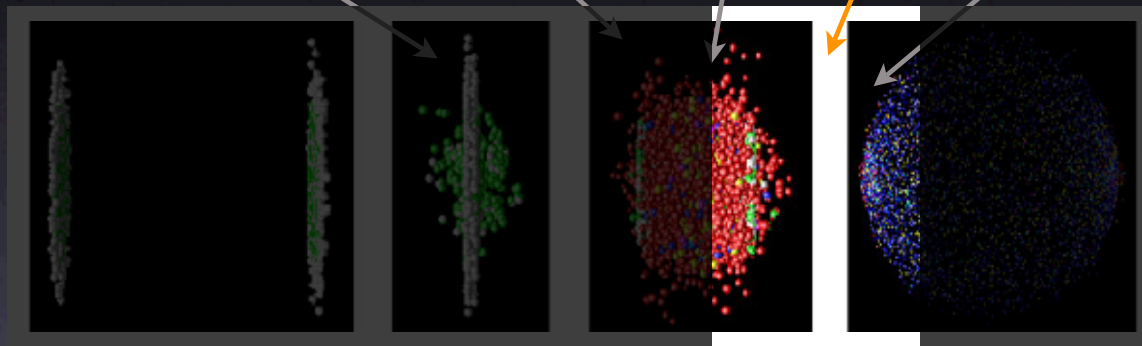


PhD thesis Christof Roland, 2000

- Dynamical fluctuations are small ( $< \sim 5\%$ )
- Compatible with resonance gas (Jeon, Koch; nucl-th/9906074)
- Strangeness enhancement in every event
- Chemical freeze-out at same  $T$  in every event

# What can we learn from fluctuations?

(How) Does matter thermalize?  
How is entropy produced?  
Properties of the medium?  
**Nature of the phase transition?**  
How are hadrons made?



Monotonic  $\sqrt{s}$  evolution  
of global fluctuations

Magnitude of fluctuations moderate

Scaling of relative fluctuations

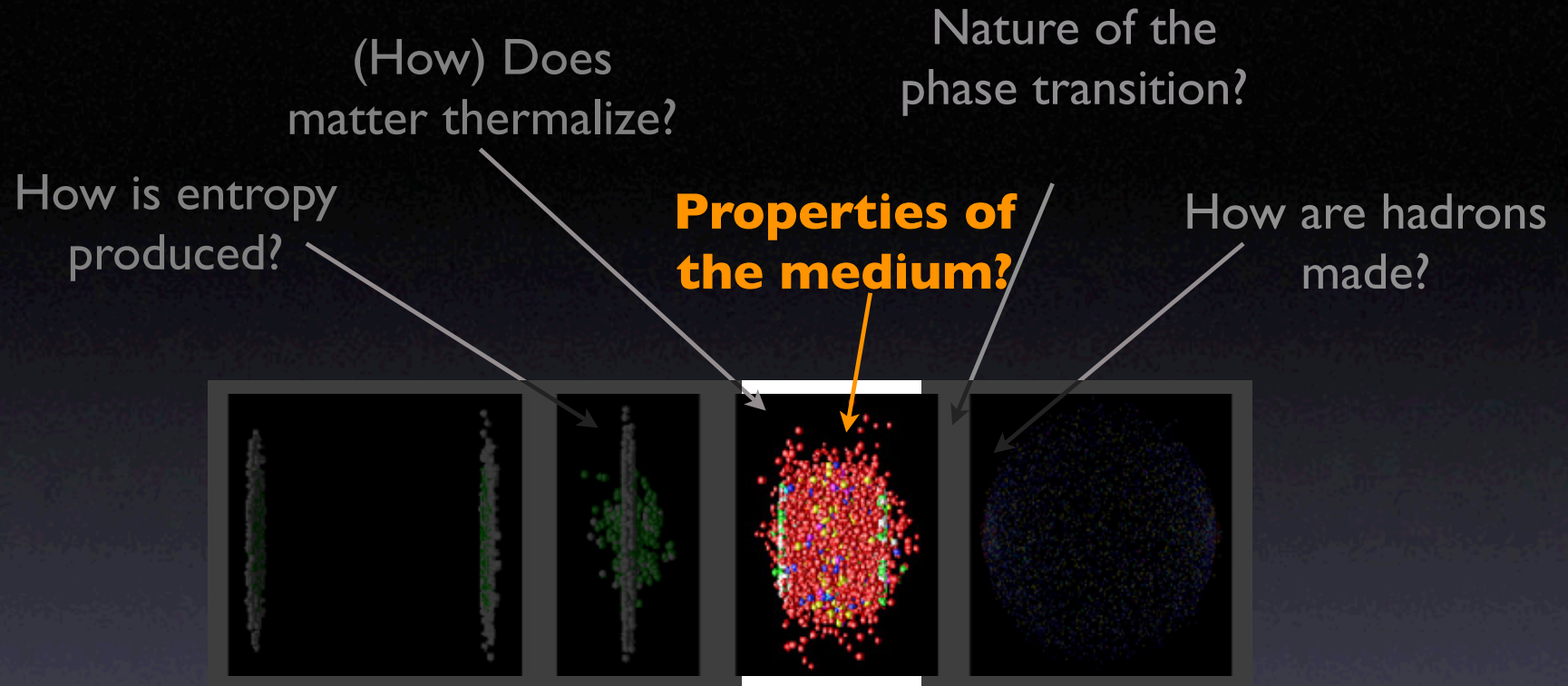


Small latent heat?

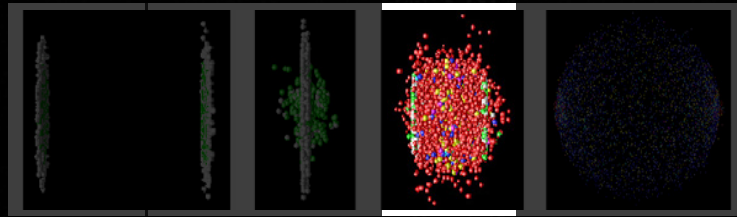
Equilibrium evolution?

Freeze-out far from  
critical point?

# What can we learn from fluctuations?

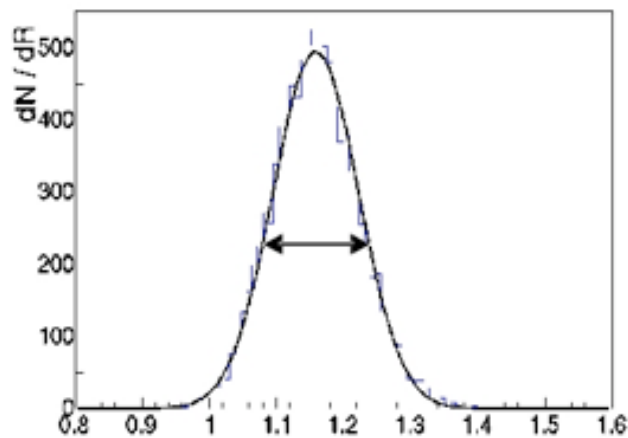
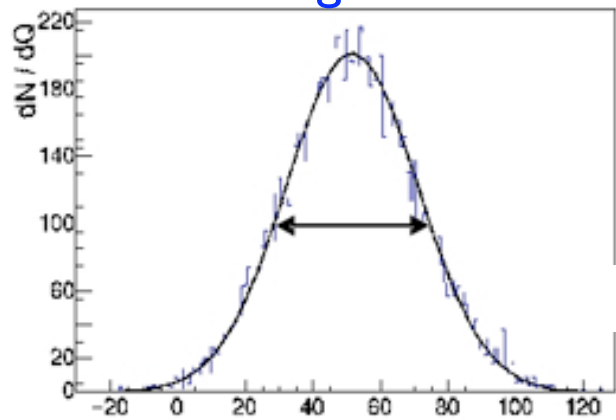


ca 2000



## Properties of the Medium

Net Charge  $N^+ - N^-$

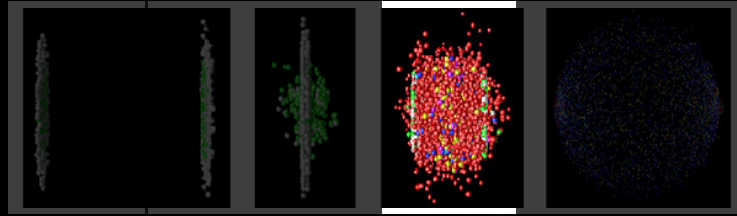


Ratio  $N^+/N^-$

- Net Charge/ $\Delta y$  Fluctuations  $\leftrightarrow$  Charge/DoF
  - Jeon, Koch hep-ph/0003168
  - Asakawa, Heinz, Mueller hep/ph/0003169
  - Change from 1-2 (QGP) to 4 (Pion Gas)

- Fluctuations frozen b/c charge conservation
  - Diffusion vs Expansion timescale

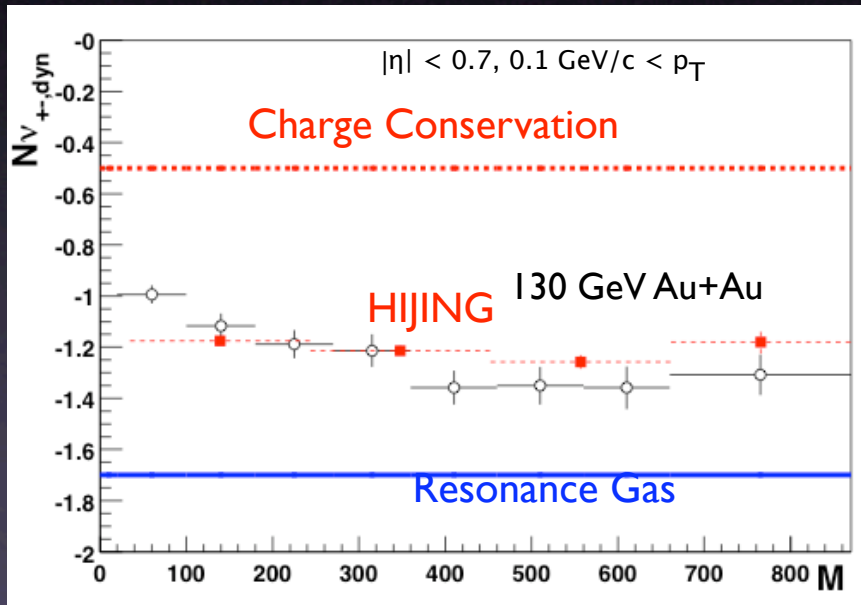
- Fluctuations of  $N^+ - N^-$  or  $N^+/N^-$  vs statistical reference



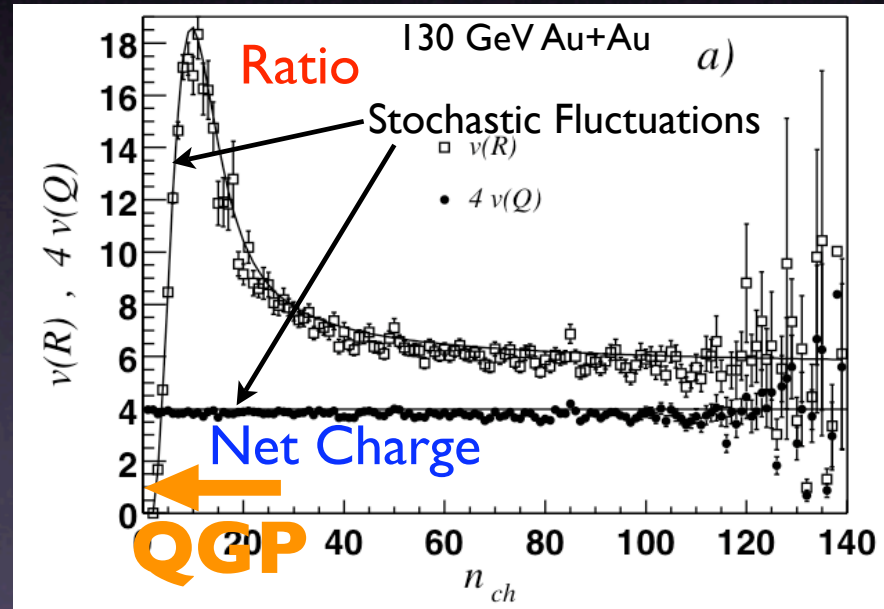
## Properties of the Medium

# Net Charge Fluctuations

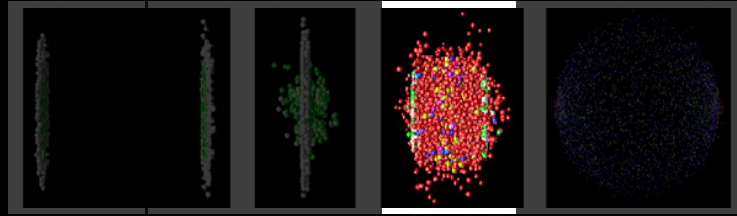
STAR PRC 68 (2003)



PHENIX PRL 89 (2002)

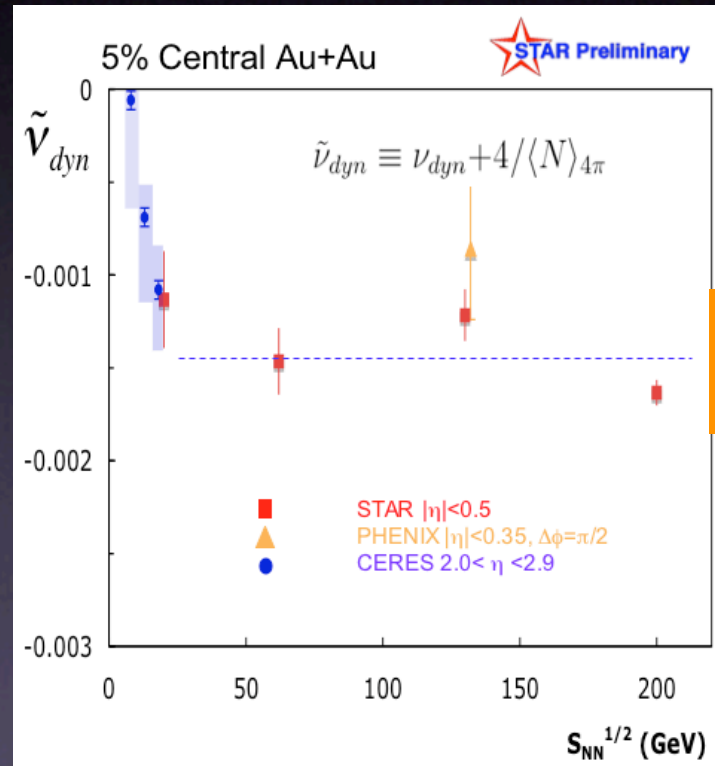
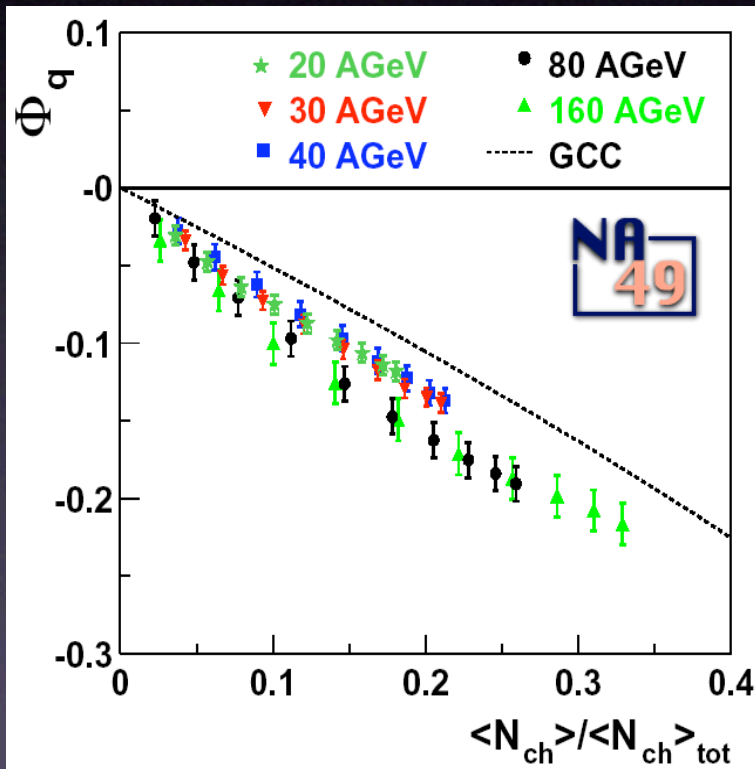


Fluctuations agree with stochastic distributions of Hadrons



## Properties of the Medium

# Net Charge Fluctuations



Quark-Coalescence  
Bialas, 2003

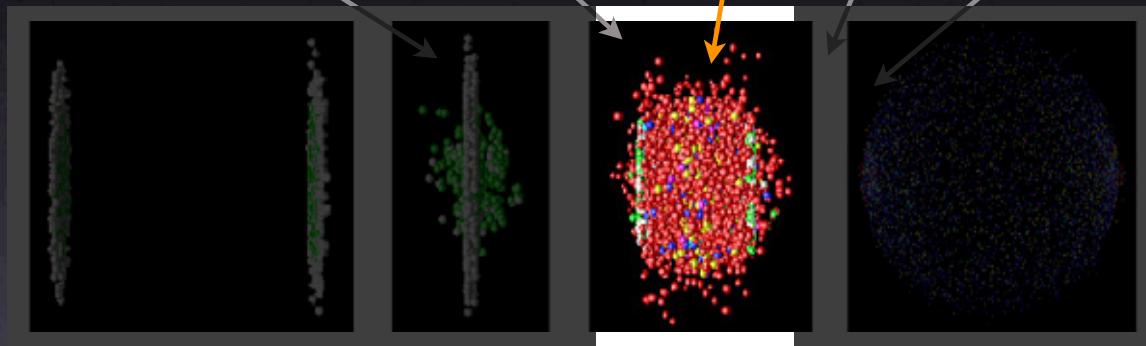
QGP



Little (no)  $\sqrt{s}$  dependence of charge fluctuations

# What can we learn from fluctuations?

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Nature of the phase transition?  
How is entropy produced?  
**Properties of the medium?**  
How are hadrons made?



Net charge fluctuations  
large ( $\sim$  hadron gas)

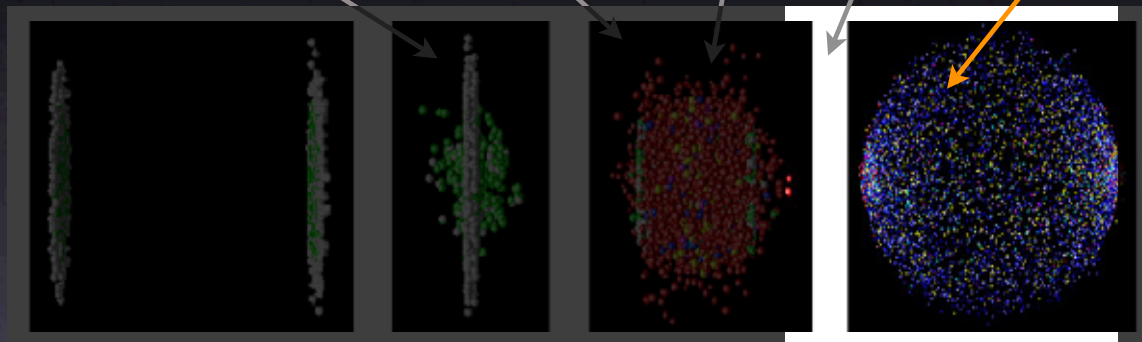
Small/no  $\sqrt{s}$  dependence



Quark coalescence?  
Property of Hadronization?  
Diffusion?  
Bound states?

# What can we learn from fluctuations?

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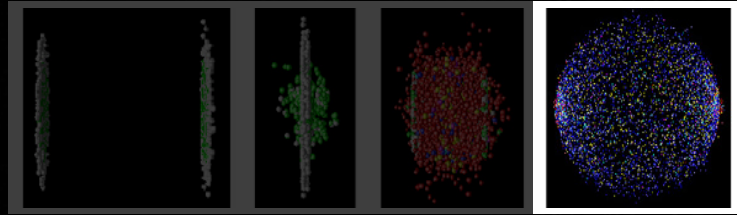


Quark coalescence?

**Property of Hadronization?**

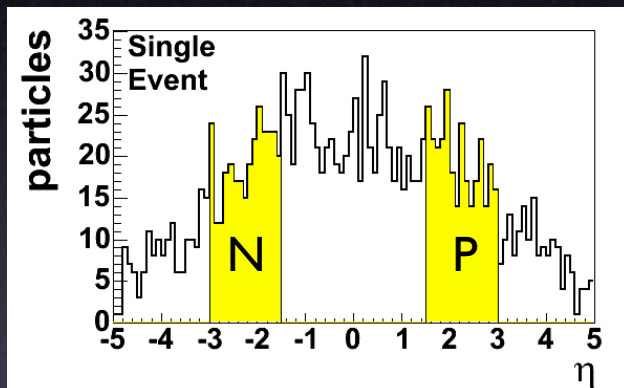
Diffusion?

Bound states?



Hadronization

## Forward/backward multiplicity correlations



$$C = \frac{P - N}{\sqrt{P + N}}$$

Use variance  $\sigma_C^2$

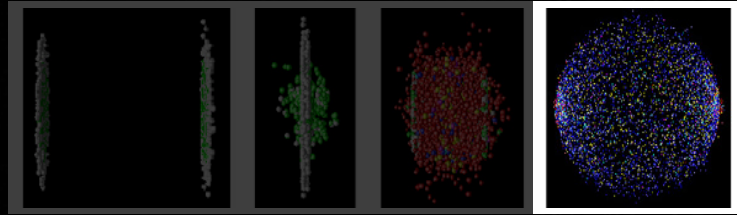
Particles produced independently:

$$\sigma_C^2 = 1$$

Particles produced in clusters of size  $K$ :

$$C \rightarrow \sqrt{K} C$$

$$\sigma_C^2 \rightarrow K \sigma_C^2$$



Hadronization

## Forward/backward multiplicity correlations

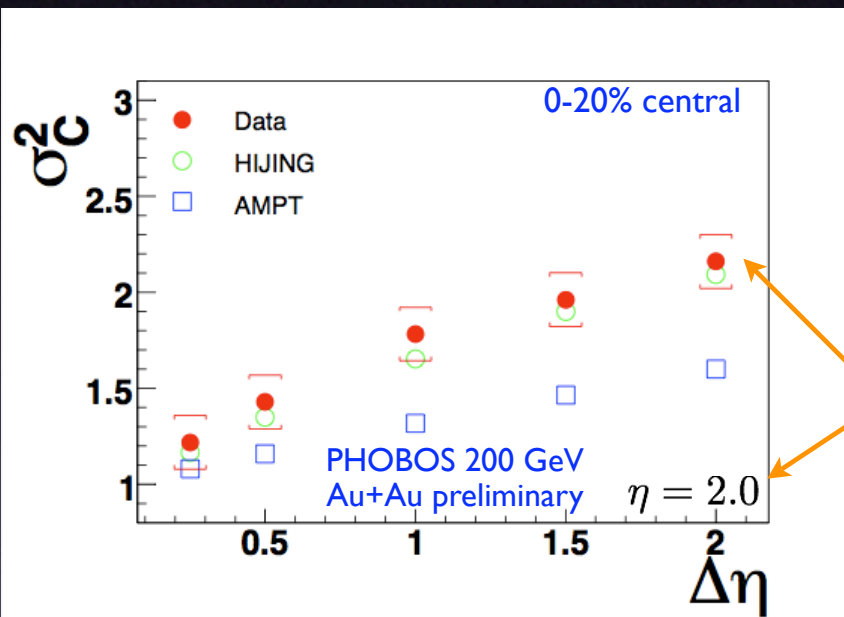
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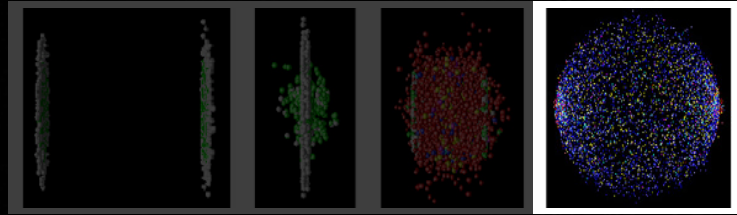
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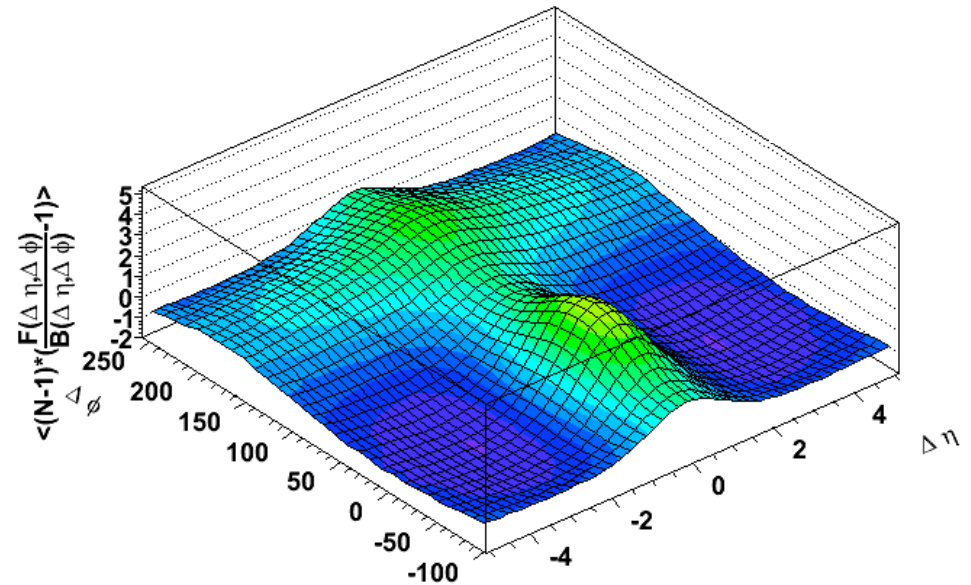
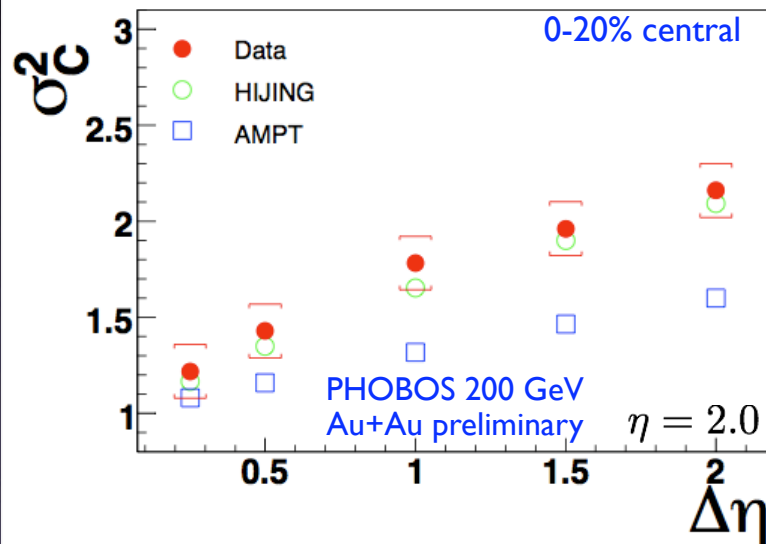


effective cluster size  $\approx 2-2.5$   
for 200 GeV Au+Au



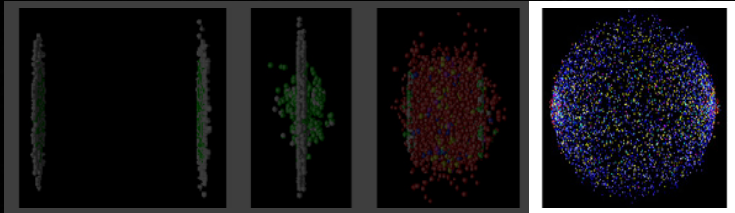
Hadronization

## Clusters in A+A (and p+p) collisions



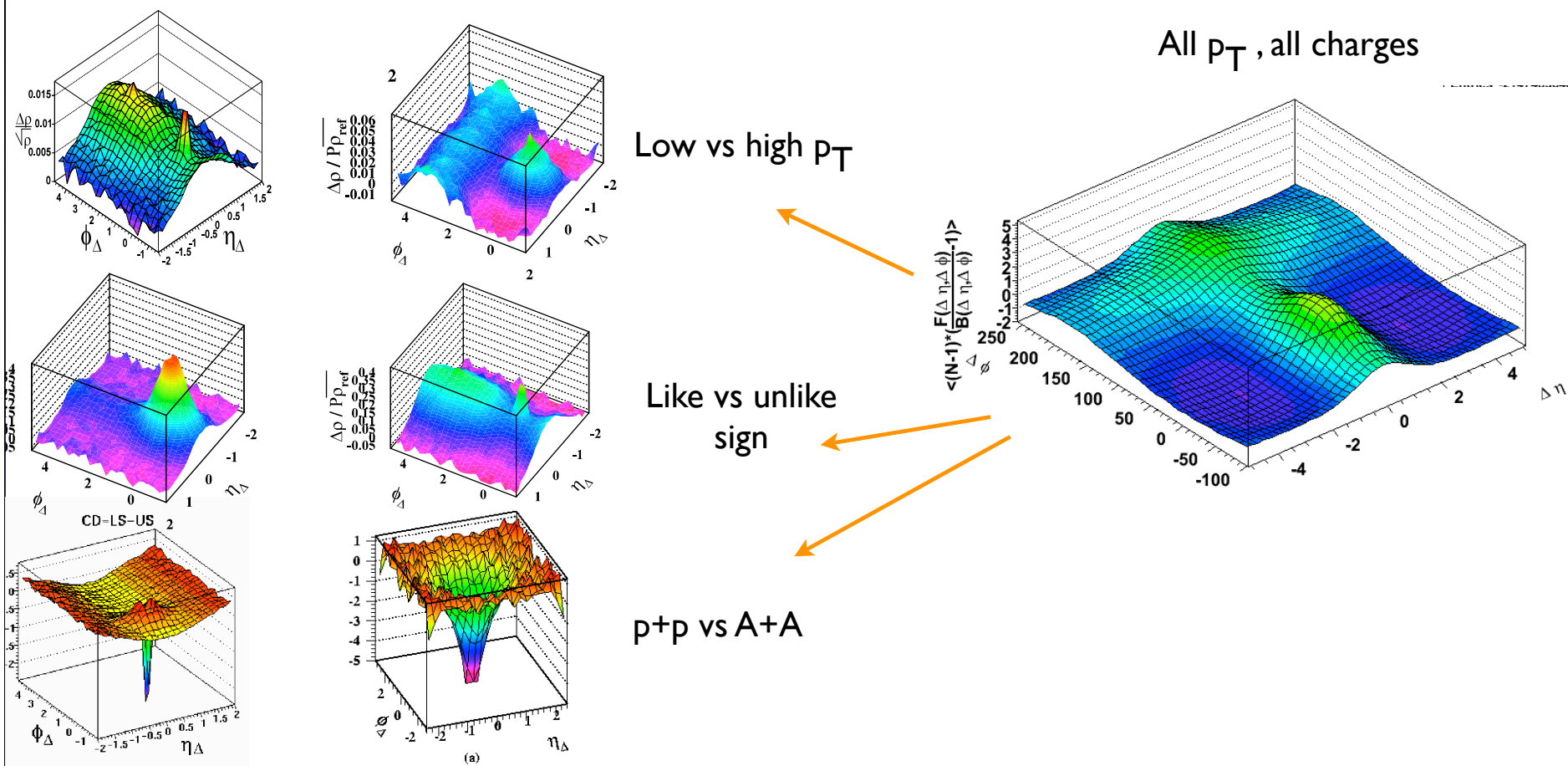
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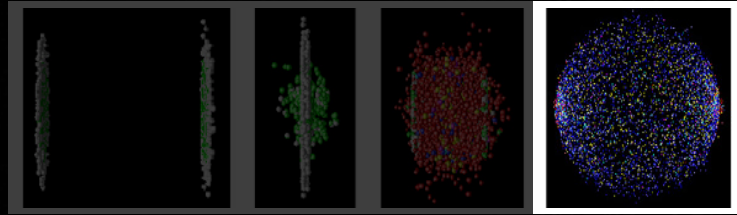
“Cluster” in  $\Delta\eta, \Delta\phi$  space via  
2-particle correlations  
(pythia p+p @200 GeV,  $\eta < 3$ )



Hadronization

# Landscape of correlation analyses

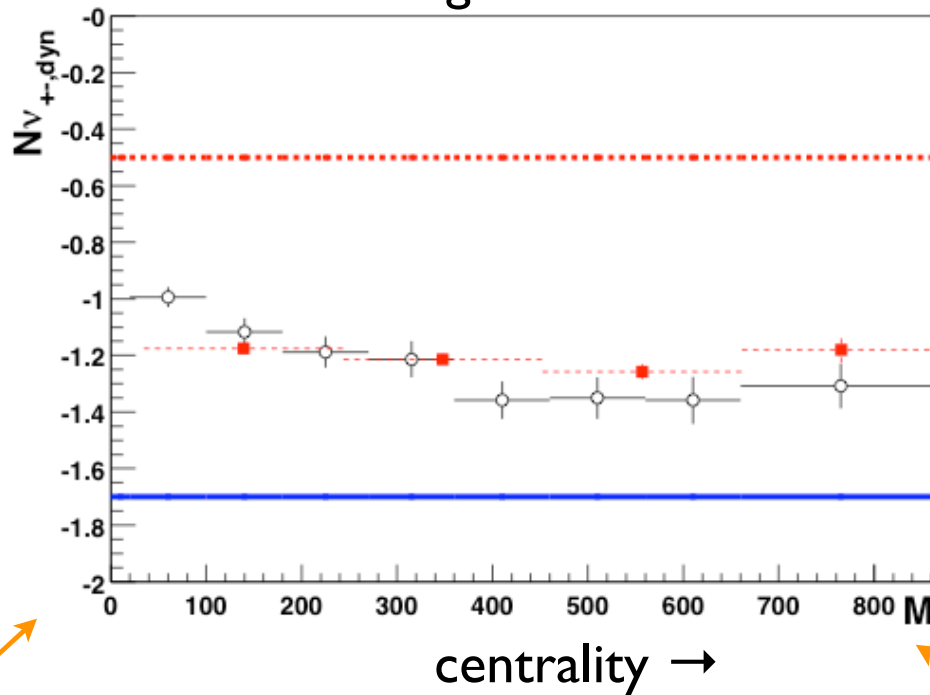




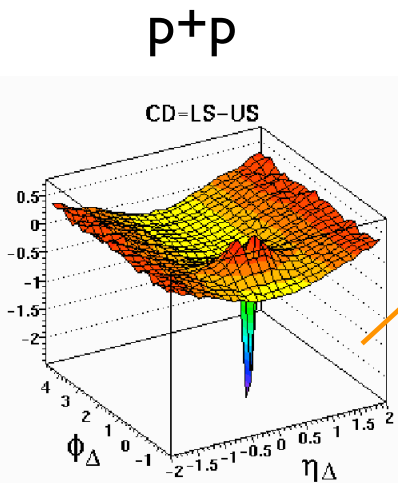
Hadronization

## Correlations and Fluctuations, revisited

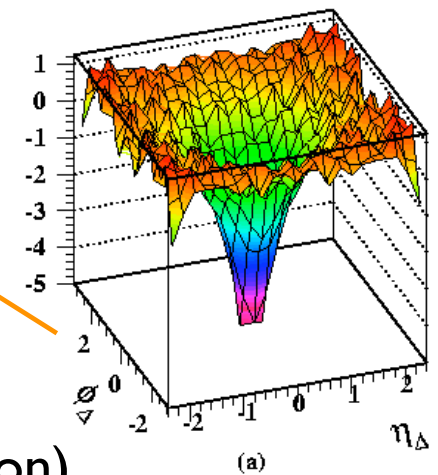
### Net-charge Fluctuations



Global scaling, even though underlying correlations change



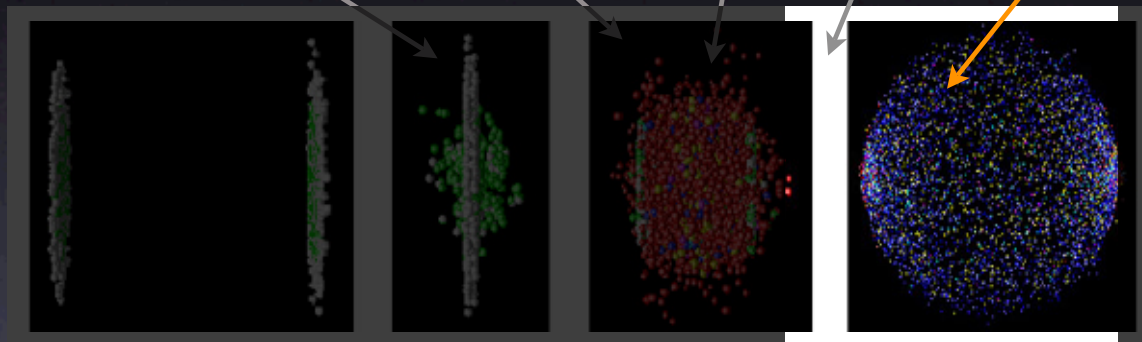
### Central A+A



Net-charge correlations (c.f. Balance Function)

# What can we learn from fluctuations?

(How) Does matter thermalize?  
Nature of the phase transition?  
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Properties of the medium?  
**How are hadrons made?**



Large multiplicity fluctuations

Strong change in underlying correlation structure

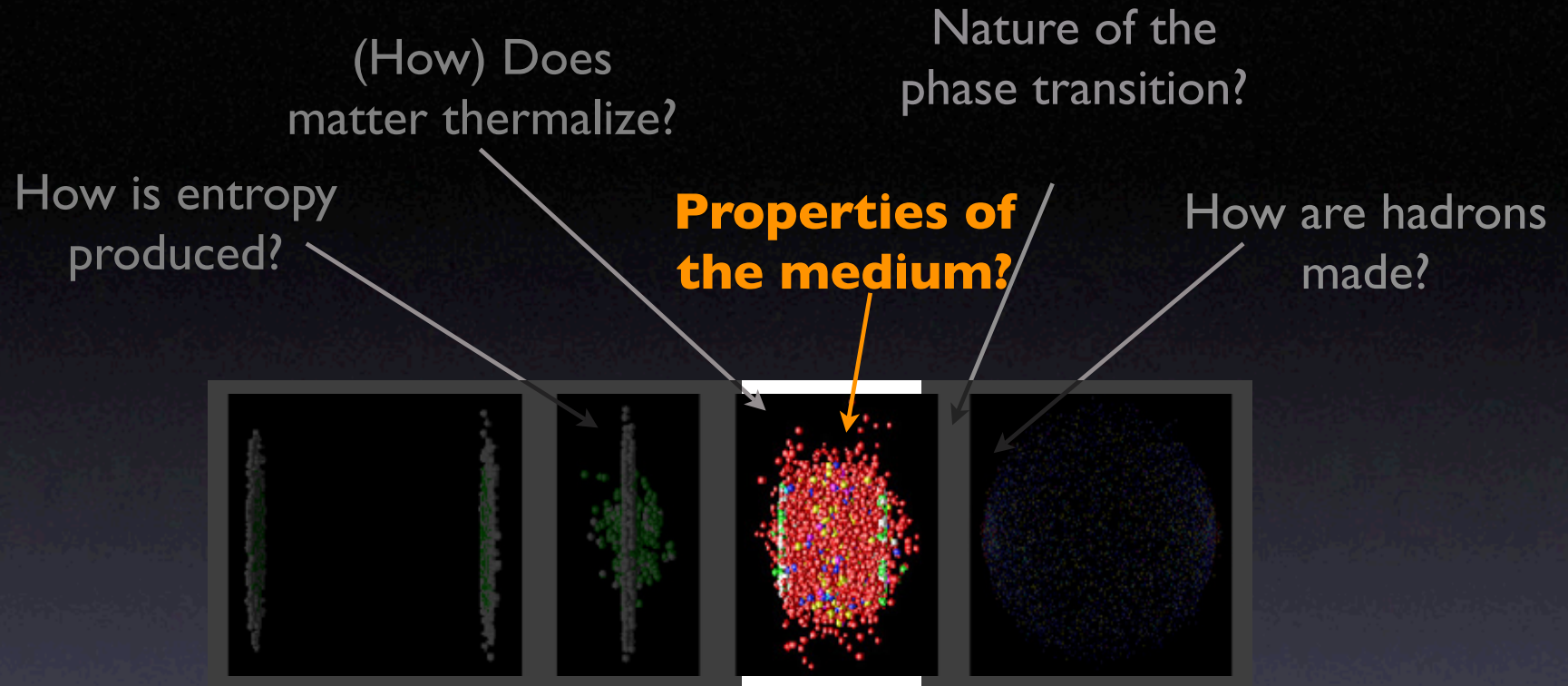


Particles produced in large 'clusters'

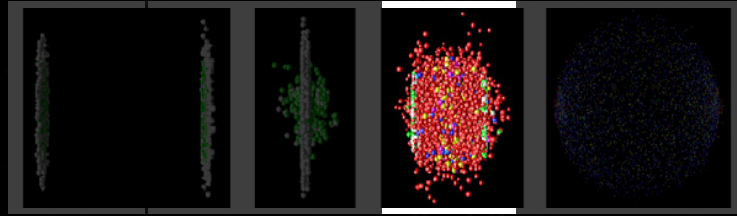
Understanding of hadronization essential

Collision dynamics reflected in correlation structure

# What can we learn from fluctuations?

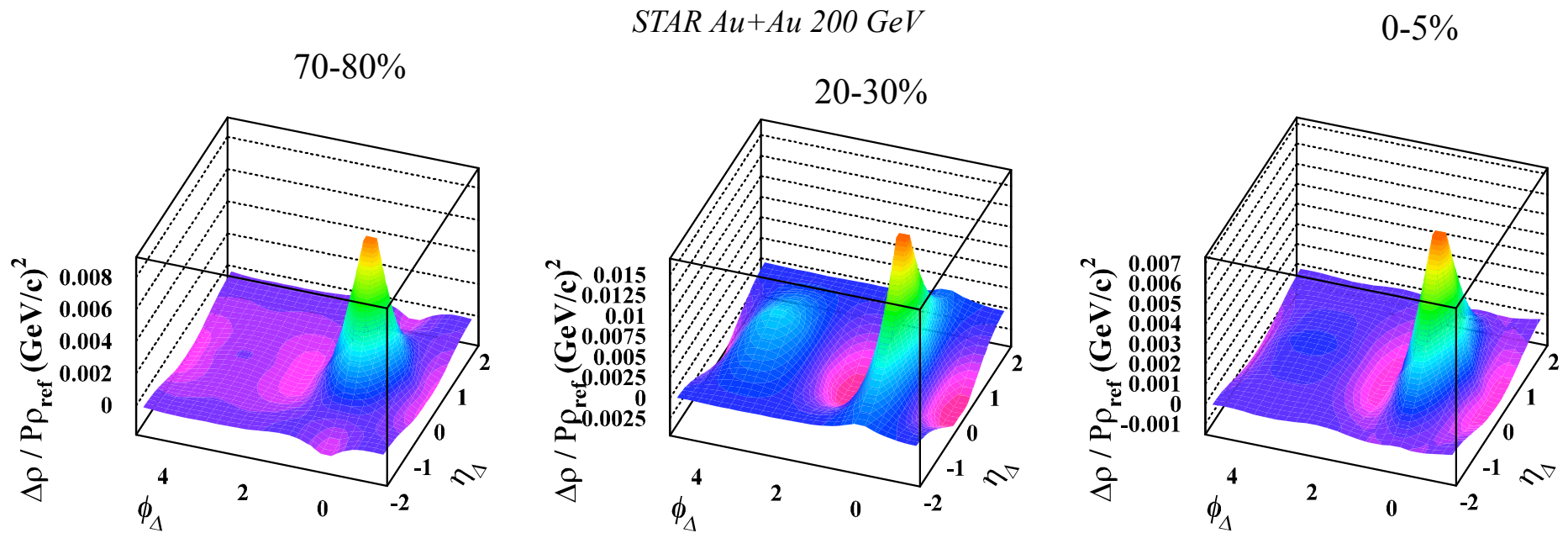


Look at the medium using 2-particle correlations  
(untriggered) at high(er)  $p_T$

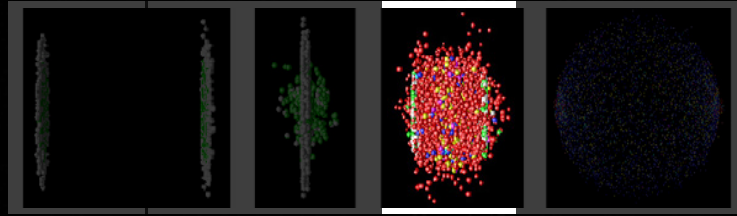


Properties of the Medium

## 2-particle momentum correlations

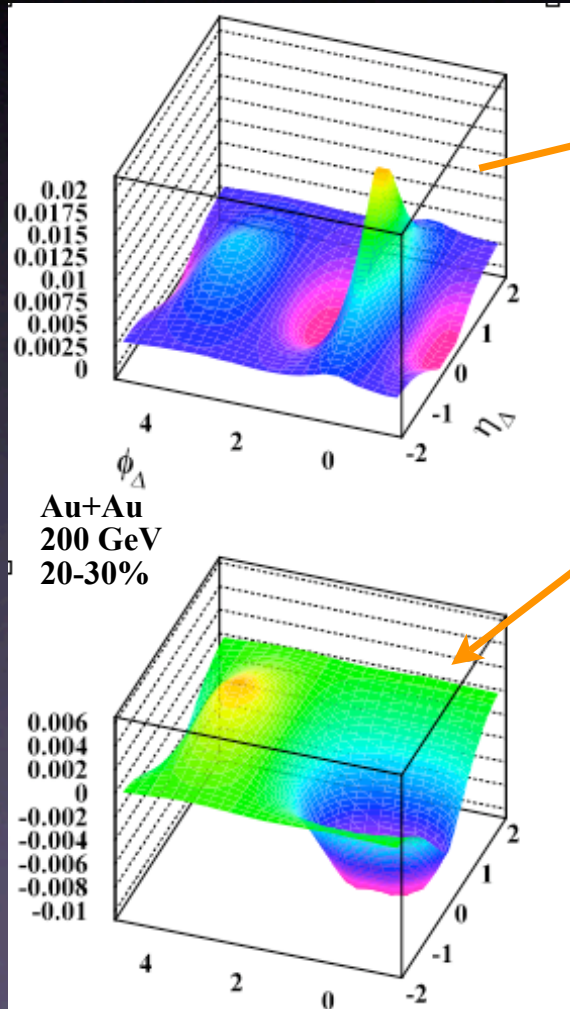


Shape of near-side “parton-fragmentation” peak evolves with centrality



Properties of the Medium

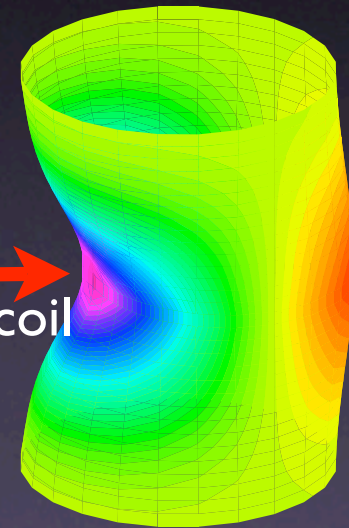
## 2-particle momentum correlations



Subtract fragmentation peak  
to look at medium

Jet

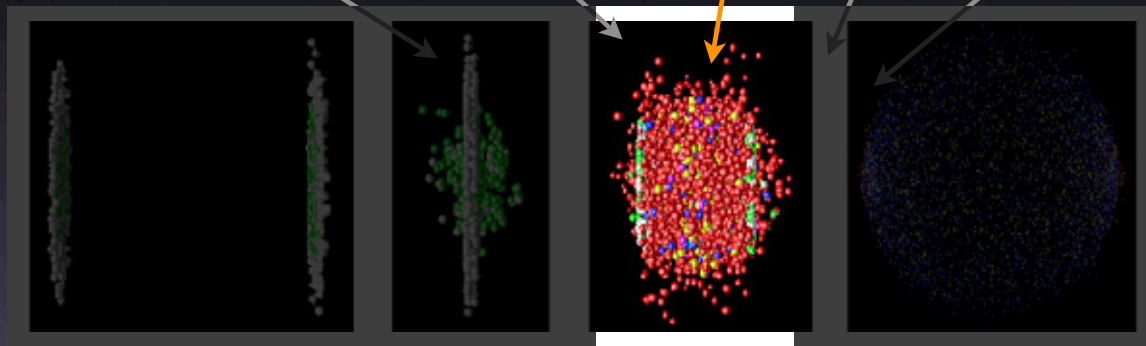
Recoil



*bulk medium*

# What can we learn from fluctuations?

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Medium modification of  $p_T$  correlation shape

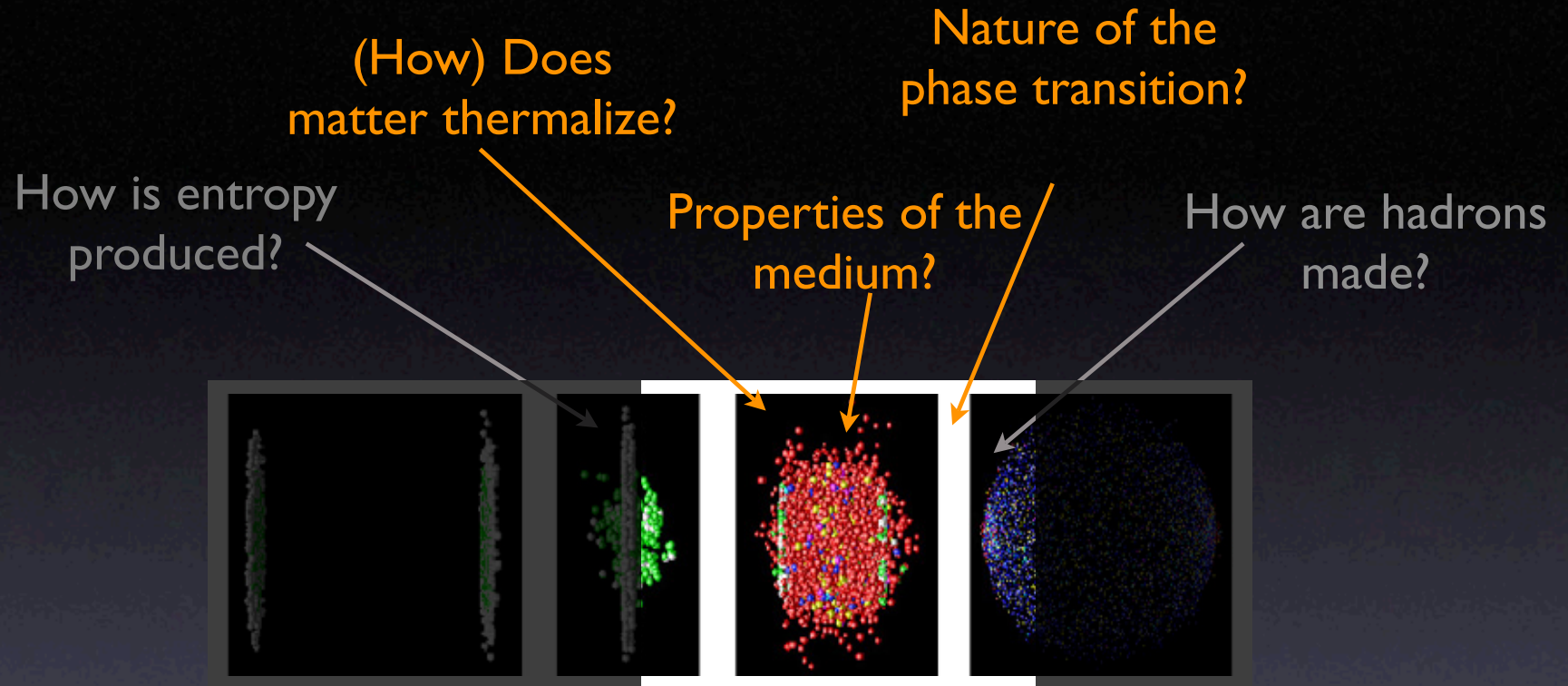
Interaction of partons with bulk medium (flow field)



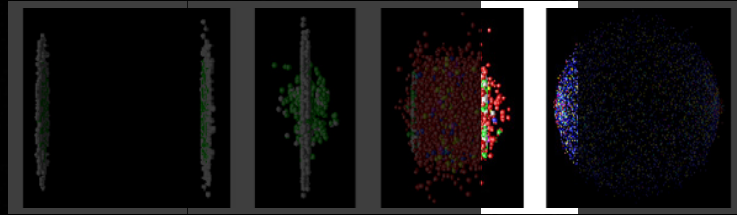
Possible medium modification due to partonic recoil

Extract bulk properties (e.g. viscosity)?

# What can we learn from fluctuations?

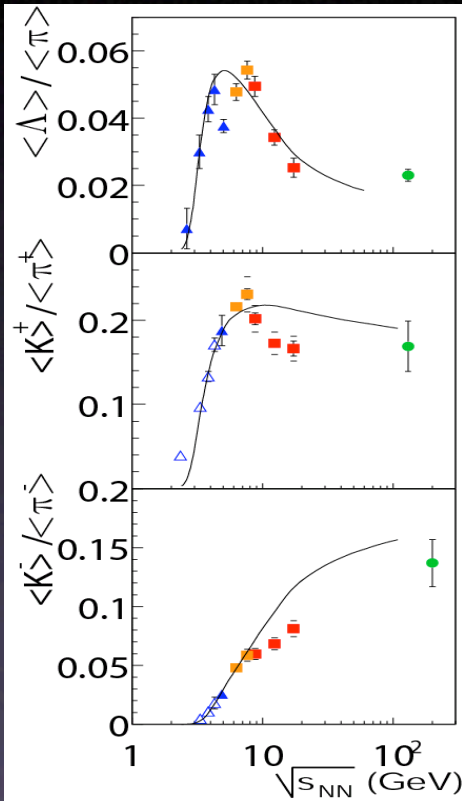


Some remarks on future measurements

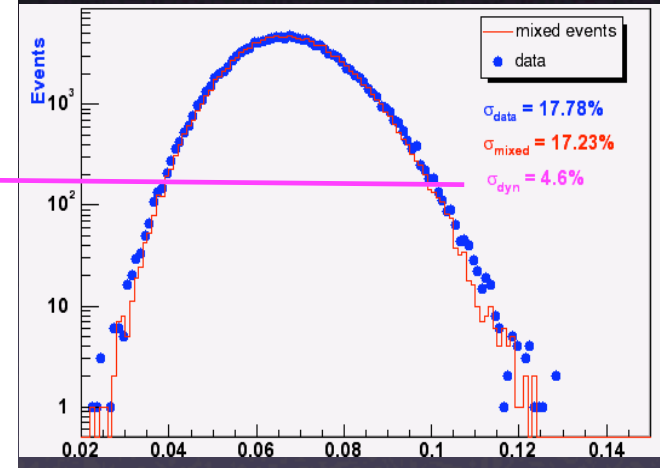
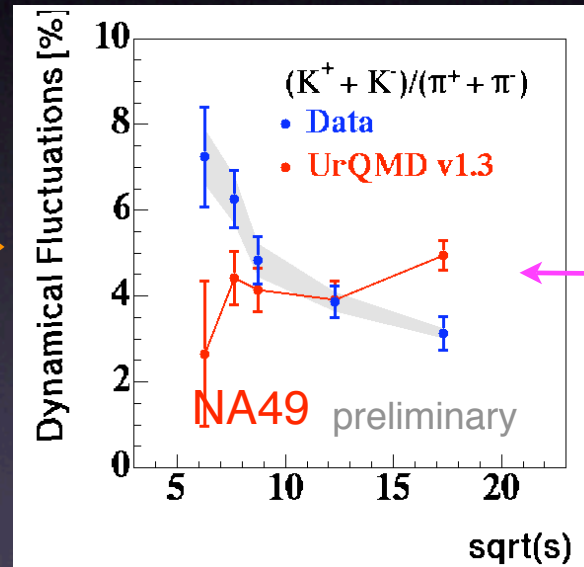


# NA49 'Horn'

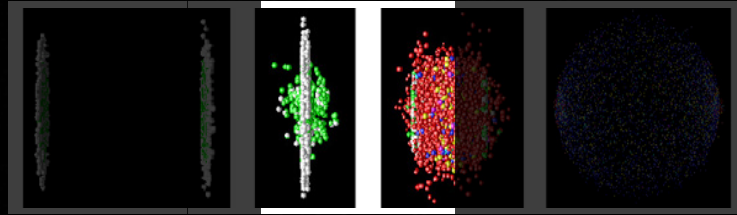
## Strangeness Fluctuations vs $\sqrt{s}$



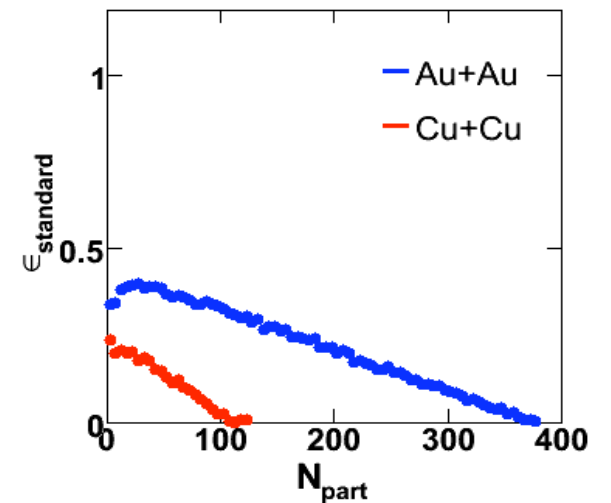
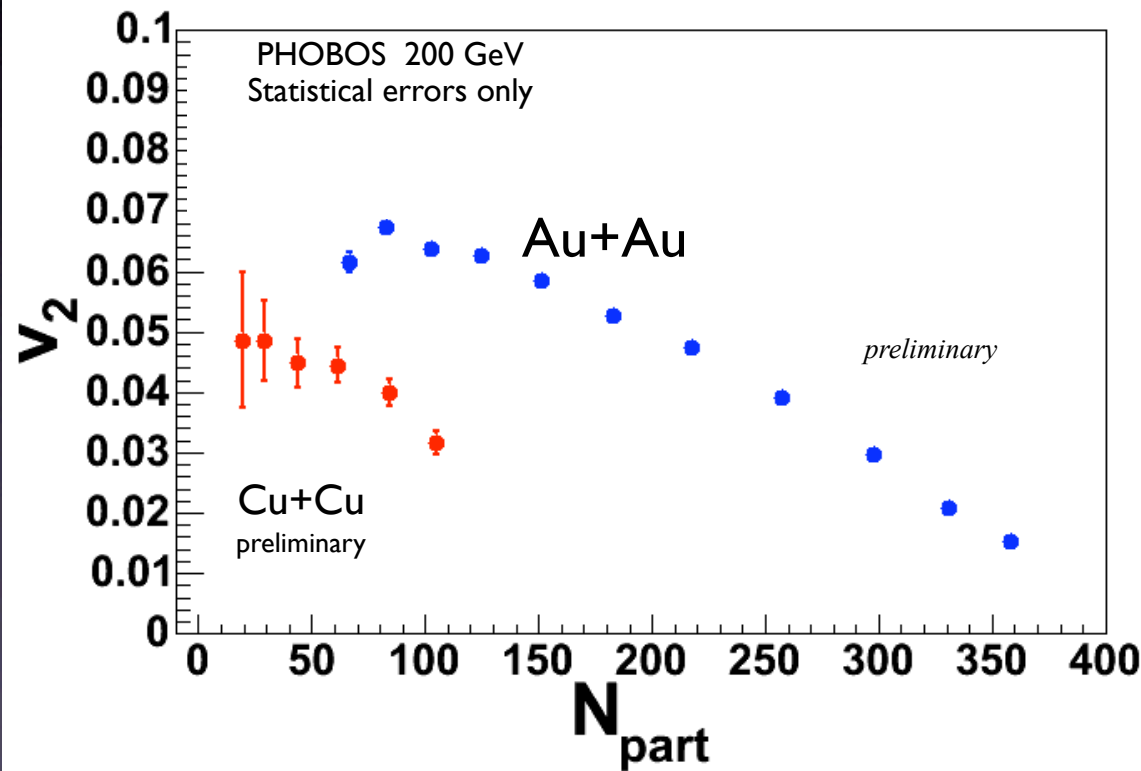
### NA49 (Christof Roland QM'04)



## Fluctuations in K/pi ratio

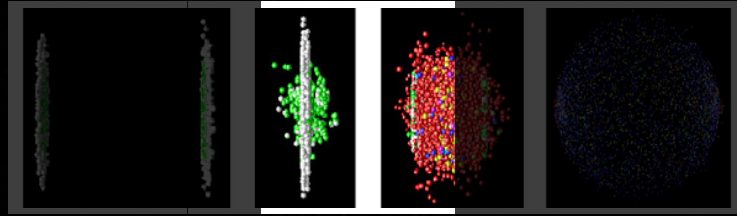


## Geometry and Thermalization



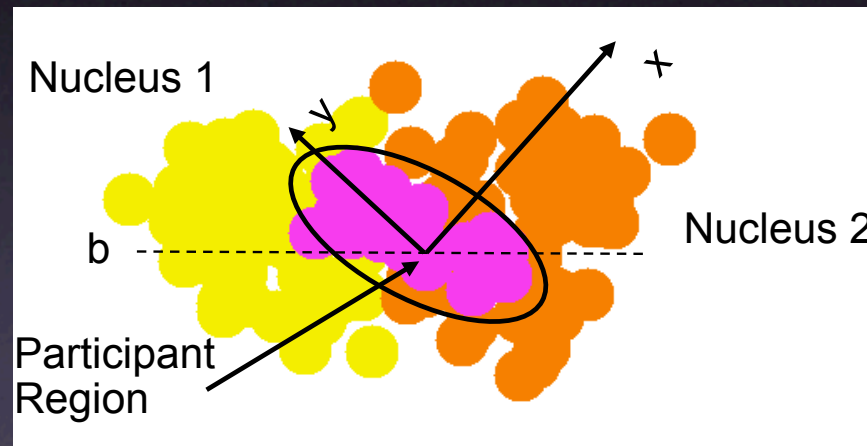
Geometrical initial state  
eccentricity from  
Glauber model

Surprisingly large flow signal  
in Cu+Cu!

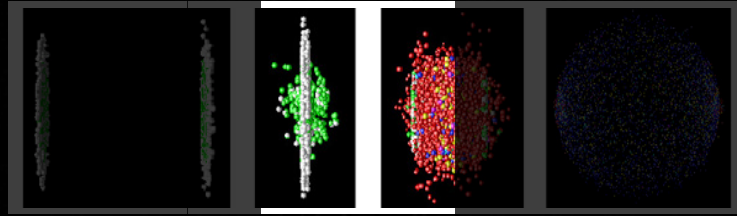


## Geometry and Thermalization

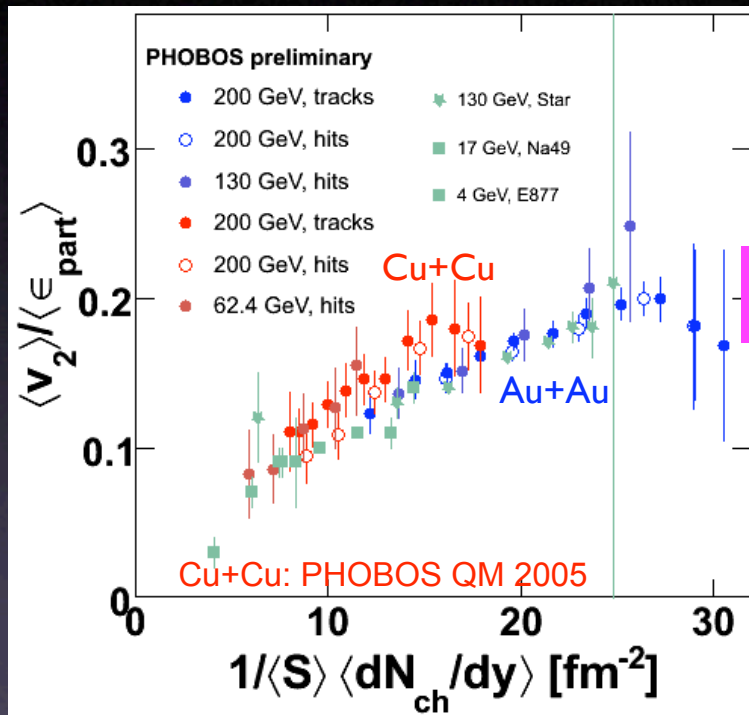
Realign the coordinate system to maximize ellipsoidal shape  
(a principal axis transformation)



“Participant” eccentricity  
(versus “standard” eccentricity)



## Geometry and Thermalization



“Hydro-Limit”

“Eccentricity Fluctuations” provide additional correlation strength

Nuclear Physics!?

➔ Measure  $v_2$  fluctuations

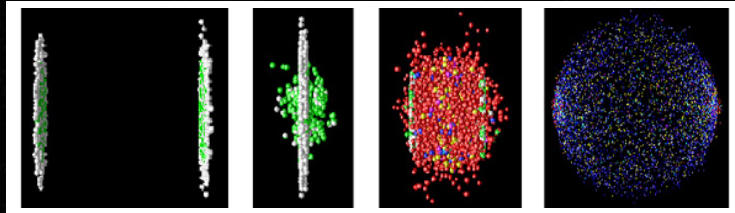
“Participant Eccentricity” provides universal scaling  
Approach to equilibrium?

Low Density Limit:

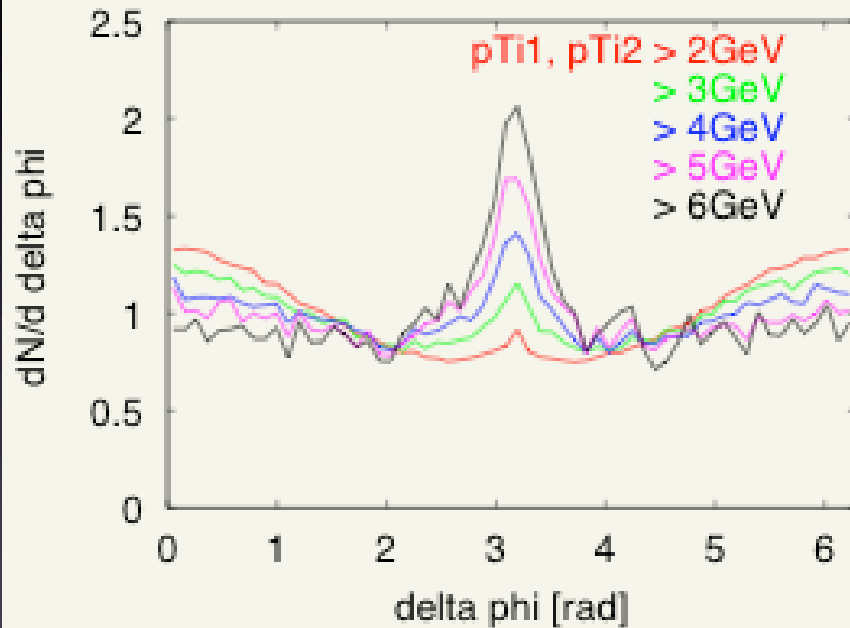
STAR, PRC 66 034904 (2002)

Voloshin, Poskanzer, PLB 474 27 (2000)

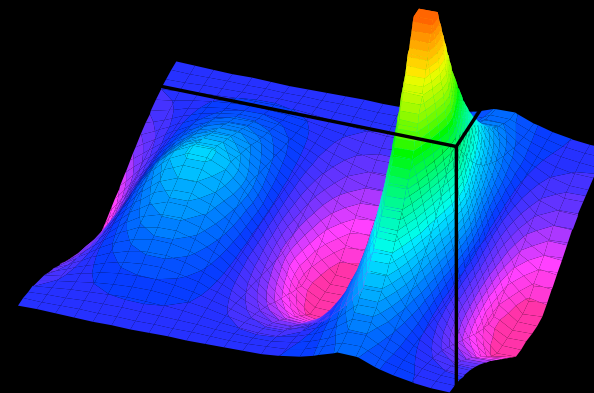
Heiselberg, Levy, PRC 59 2716, (1999)



cut on initial parton  $p_T$



STAR



Data

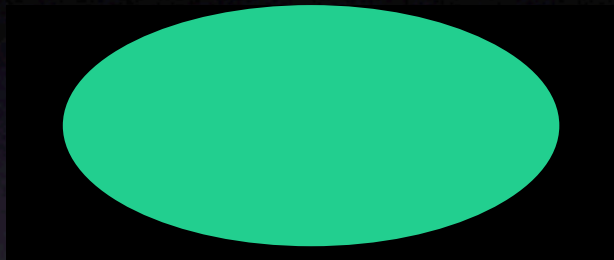
Denes Molnar,  
BNL workshop  
June '05

• This is the first study of jet correlations that treats the bulk sector and jets in the same framework. The results are encouraging but need several improvements:

- add soft partons ("push" effect will contribute)
- study centrality, particle type dependence (higher statistics)
- include hadronization (coalescence, fragmentation)
- extend to radiative processes, coherence
- could also study other correlations, e.g., Mach cone ...

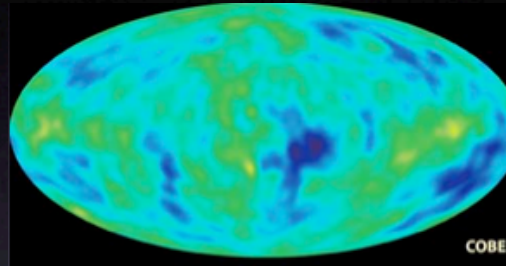
# Analogy: Cosmic Microwave Background

## Cosmic microwave background



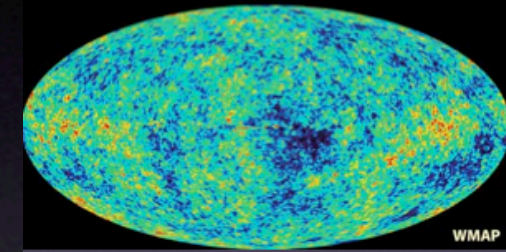
Penzias, Wilson  
1964

$$\langle T \rangle = 3\text{K}$$



COBE 1992

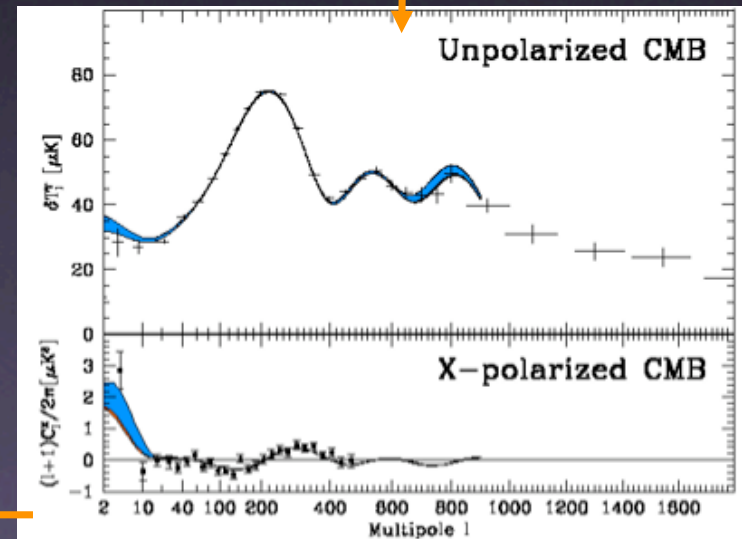
$$\Delta T/T \sim 10^{-5}$$



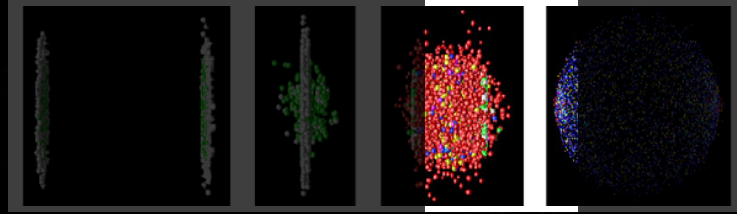
WMAP

"Best" Cosmological Parameters:  
Table 3 from Wilkinson Microwave Anisotropy Probe (WMAP) Observations:  
Preliminary Maps and Basic Results,  
C. L. Bennett et al. (2003), accepted by the *Astrophysical Journal*,  
available at <http://lambda.gsfc.nasa.gov/>

Description	Symbol	Value	+ uncertainty	- uncertainty
Total density	$\Omega_{tot}$	1.02	0.02	0.02
Equation of state of quintessence	$w$	$< -0.78$	95% CL	—
Dark energy density	$\Omega_{\Lambda}$	0.73	0.04	0.04
Baryon density	$\Omega_b h^2$	0.0224	0.0009	0.0009
Baryon density	$\Omega_b$	0.044	0.004	0.004
Baryon density ( $\text{cm}^{-3}$ )	$n_b$	$2.5 \times 10^{-7}$	$0.1 \times 10^{-7}$	$0.1 \times 10^{-7}$
Matter density	$\Omega_m h^2$	0.135	0.008	0.008
Matter density	$\Omega_m$	0.27	0.04	0.04
Light neutrino density	$\Omega_{\nu} h^2$	$< 0.0078$	95% CL	—
CMB temperature [K]	$T_{mb}$	2.725	0.002	0.002
CMB photon density ( $\text{cm}^{-3}$ )	$n_{\gamma}$	403.4	0.9	0.9
Baryon-to-photon ratio	$\eta$	$6.1 \times 10^{-10}$	$0.3 \times 10^{-10}$	$0.2 \times 10^{-10}$
Baryon-to-matter ratio	$\Omega_b \Omega_m^{-1}$	0.17	0.01	0.01
Fluctuation amplitude in $8h^{-1}$ Mpc spheres	$\sigma_8$	0.84	0.04	0.04
Lower cluster abundance scaling	$\sigma_8 \Omega_m^{-0.5}$	0.44	0.04	0.05
Power spectrum normalization (at $k_0 = 0.05 \text{ Mpc}^{-1}$ ) <sup>a</sup>	$A$	0.833	0.086	0.253
Scalar spectral index (at $k_0 = 0.05 \text{ Mpc}^{-1}$ ) <sup>a</sup>	$n_s$	0.96	0.03	0.03
Running index slope (at $k_0 = 0.05 \text{ Mpc}^{-1}$ ) <sup>a</sup>	$dn_s/d \ln k$	-0.021	0.016	0.018
Tensor-to-scalar ratio (at $k_0 = 0.002 \text{ Mpc}^{-1}$ ) <sup>a</sup>	$r$	$< 0.90$	95% CL	—
Redshift of decoupling	$z_{dec}$	1089	1	1
Thickness of decoupling (FWHM)	$\Delta z_{dec}$	196	2	2
Hubble constant	$h$	0.71	0.04	0.03
Age of universe (Gyr)	$t_0$	11.7	0.2	0.2
Age at decoupling (kyr)	$t_{dec}$	379	8	7
Age at reionization (Myr, 95% CL)	$t_{re}$	180	220	80
Decoupling time interval (kyr)	$\Delta t_{dec}$	118	9	9
Redshift of matter energy equality	$z_{eq}$	3231	194	210
Reionization optical depth	$\tau_{re}$	0.17	0.04	0.04
Redshift of reionization (95% CL)	$z_{re}$	20	10	9
Sound horizon at decoupling (")	$\theta_s$	0.598	0.002	0.002
Angular size distance to decoupling (Gpc)	$d_A$	14.0	0.2	0.3
Acoustic scale <sup>b</sup>	$\ell_A$	323	1	1
Sound horizon at decoupling (Mpc) <sup>d</sup>	$r_s$	347	2	2



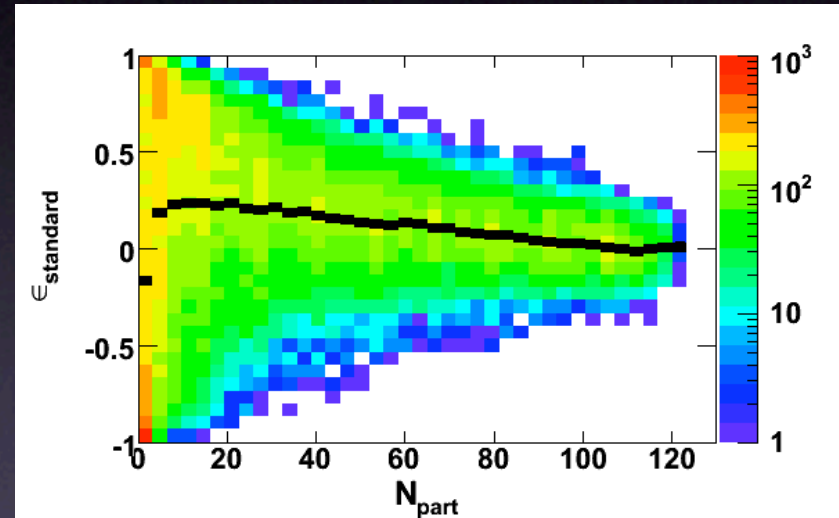
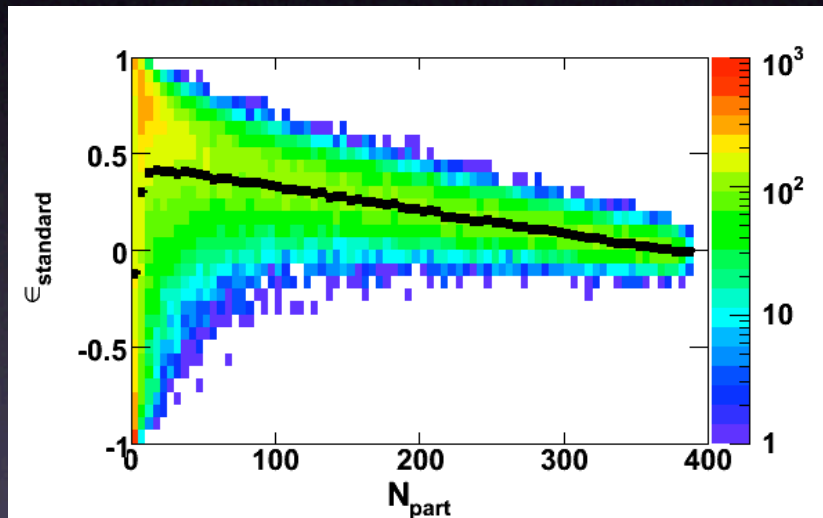




# Hydrodynamic Evolution

Au+Au

Cu+Cu

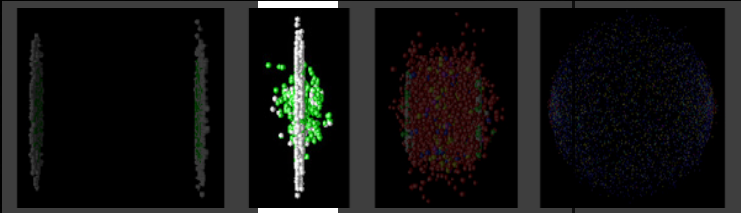


Large fluctuations in eccentricity

Even bigger fluctuations in Cu+Cu

Many peripheral events with negative eccentricity

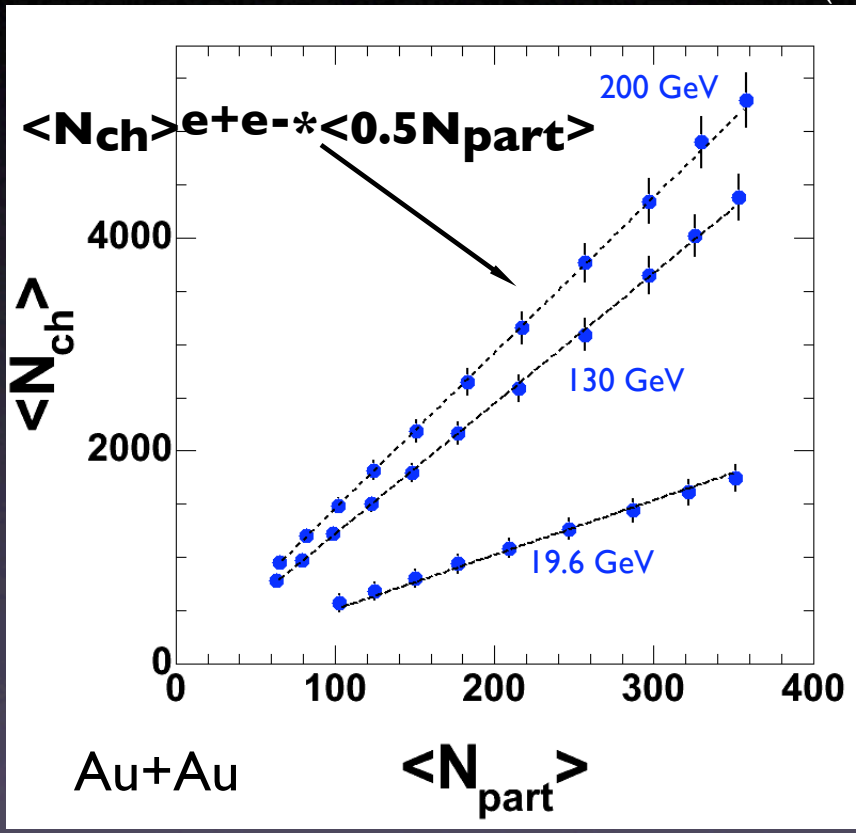
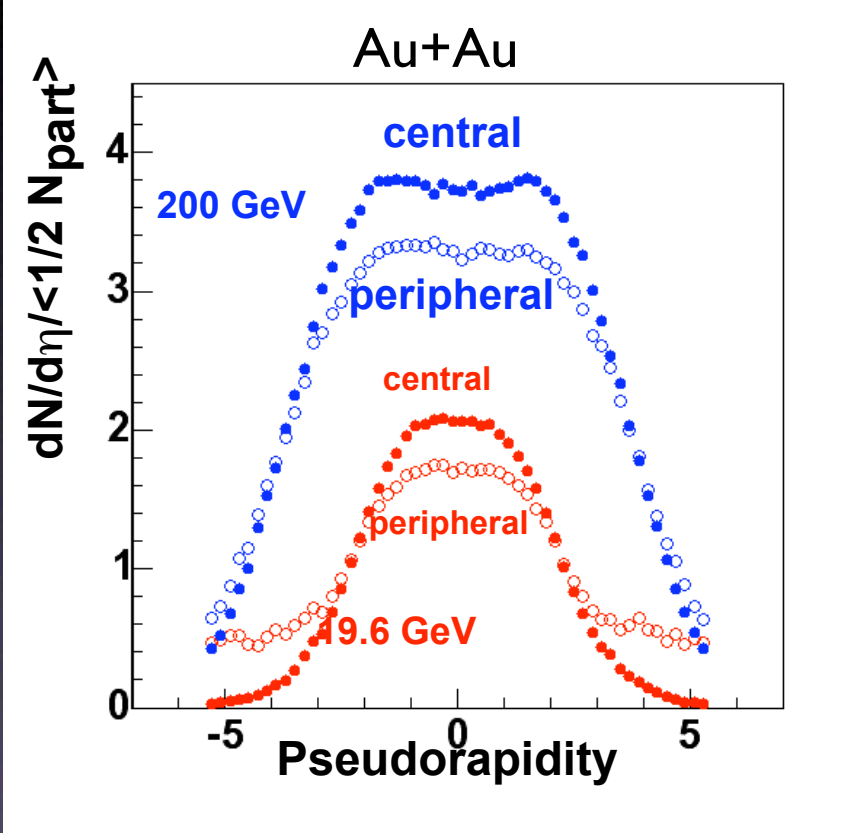
Glauber MC Calculations



# Hadron Multiplicities

PHOBOS PRL 91,052303 (2003)

PHOBOS PRL 91,052303 (2003)



Shape changes dramatically versus centrality

Multiplicity per participant is constant

$$\Phi_{p_T} = \sqrt{\frac{\frac{1}{\varepsilon} \sum_{j=1}^{\varepsilon} (N_j \langle p_T \rangle_j - N_j \hat{p}_T)^2}{\bar{N}}} - \sigma_{\hat{p}_T} \quad (1)$$

$$\simeq \sqrt{\frac{1}{\varepsilon} \sum_{j=1}^{\varepsilon} N_j (\langle p_T \rangle_j - \hat{p}_T)^2} - \sigma_{\hat{p}_T} \quad (2)$$

$$\Sigma_{p_T} = \frac{\sqrt{\sigma_{\langle p_T \rangle, dyn}^2}}{\bar{p}_T} \quad (3)$$

$$\sigma_{\langle p_T \rangle, dyn}^2 = \frac{1}{\varepsilon} \sum_{j=1}^{\varepsilon} \frac{N_j (\langle p_T \rangle_j - \hat{p}_T)^2}{\bar{N}} - \frac{\sigma_{\hat{p}_T}^2}{\bar{N}} \quad (4)$$

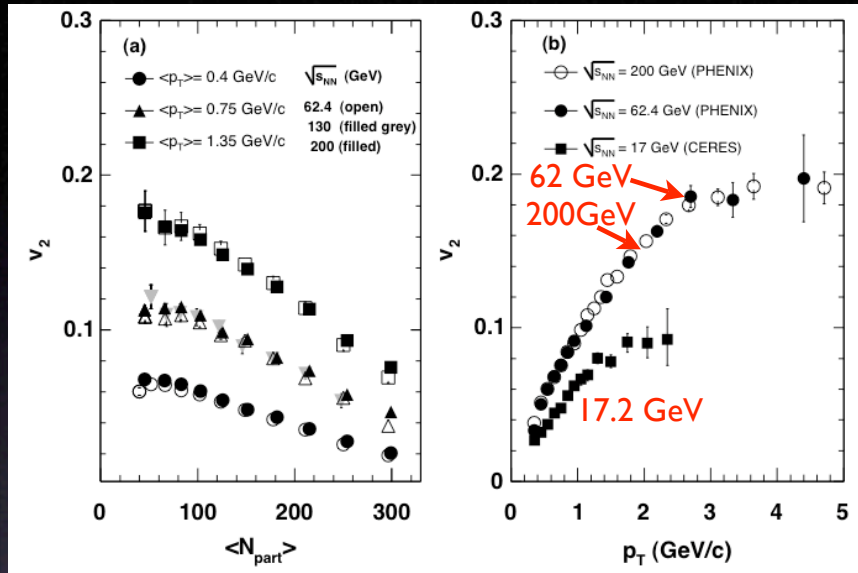
The relationship between  $\Phi_{p_T}$  and  $\Sigma_{p_T}$  when  $\Phi_{p_T}$  is small and  $\Phi_{p_T}^2$  term is neglected:

$$\Phi_{p_T} \simeq \frac{\sigma_{\langle p_T \rangle, dyn}^2 \bar{N}}{2\sqrt{\sigma_{\hat{p}_T}^2}} \quad (5)$$

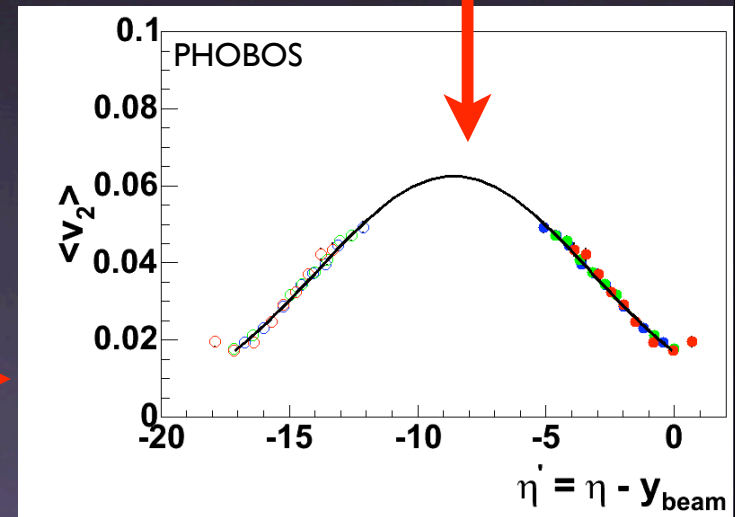
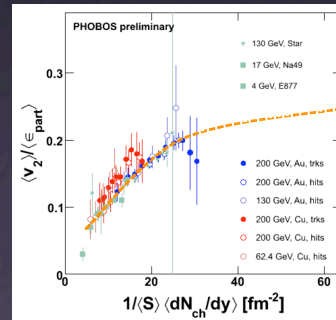
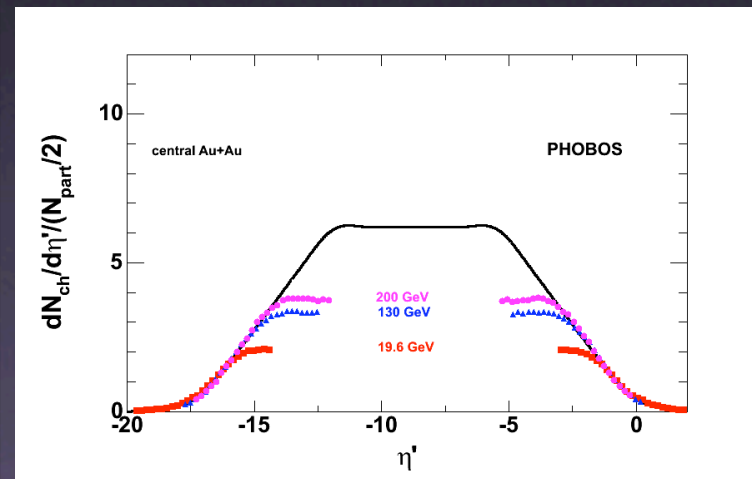
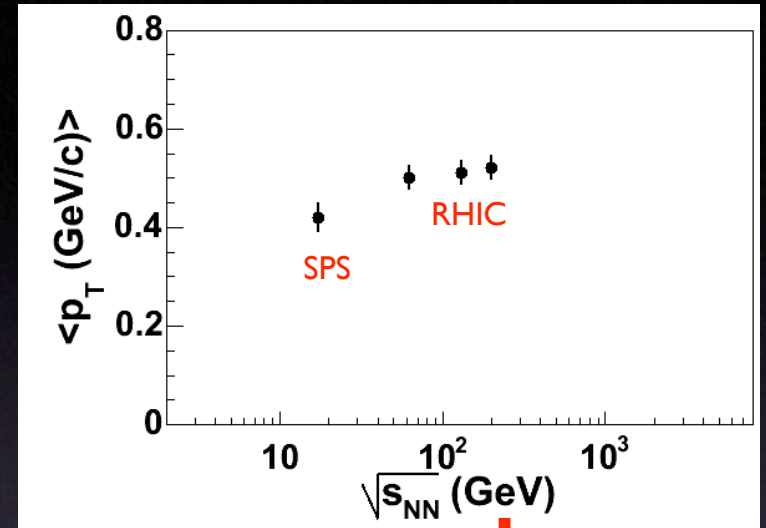
$$\Sigma_{p_T} \simeq \sqrt{\frac{2\Phi_{p_T} \sqrt{\sigma_{\hat{p}_T}^2}}{\bar{N} \bar{p}_T^2}} \quad (6)$$

# $v_2$ vs $p_T$

PHENIX nucl-ex/0411040



# $\langle p_T \rangle$ vs $\sqrt{s}$



# $dN/d\eta'$ vs $\sqrt{s}$

# $v_2(\eta')$ vs $\sqrt{s}$