



## Continuum modeling of a neuronal cell under blast loading

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### ABSTRACT

Traumatic brain injuries have recently been put under the spotlight as one of the most important causes of accidental brain dysfunctions. Significant experimental and modeling efforts are thus underway to study the associated biological, mechanical and physical mechanisms. In the field of cell mechanics, progress is also being made at the experimental and modeling levels to better characterize many of the cell functions, including differentiation, growth, migration and death. The work presented here aims to bridge both efforts by proposing a continuum model of a neuronal cell submitted to blast loading. In this approach, the cytoplasm, nucleus and membrane (plus cortex) are differentiated in a representative cell geometry, and different suitable material constitutive models are chosen for each one. The material parameters are calibrated against published experimental work on cell nanoindentation at multiple rates. The final cell model is ultimately subjected to blast loading within a complete computational framework of fluid–structure interaction. The results are compared to the nanoindentation simulation, and the specific effects of the blast wave on the pressure and shear levels at the interfaces are identified. As a conclusion, the presented model successfully captures some of the intrinsic intracellular phenomena occurring during the cellular deformation under blast loading that potentially lead to cell damage. It suggests, more particularly, that the localization of damage at the nucleus membrane is similar to what has already been observed at the overall cell membrane. This degree of damage is additionally predicted to be worsened by a longer blast positive phase duration. In conclusion, the proposed model ultimately provides a new three-dimensional computational tool to evaluate intracellular damage during blast loading.

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### 1. Introduction

The drastic increase in blast-induced traumatic brain injuries among both military (nearly 50% of the Iraq war injured returnees) and civilian casualties – mainly due to terrorists explosive devices – have generated important research efforts in the last few years [1,2]. Impact- and/or acceleration-induced brain traumatic injuries have already been the focus of many cellular and macroscopical studies through *in vivo* [3–10], *ex vivo* [11,12], *in vitro* [13–17], medical postanalysis [18–21] and modeling approaches [22–35]. However, the specific effects of a blast – a pressure wave of finite amplitude generated by a rapid release of energy [36] – on the brain is still widely unknown.

Blast overpressure, or “primary”, injuries have been known for close to 70 years, and have since been extensively observed in the lungs, eyes, ears, upper respiratory tract, heart, abdomen and more recently brain [37]. The recent wars in Iraq and Afghanistan have further exacerbated the awareness of the existence of

specific mechanisms of blast injuries in the brain [38,1,39]. Many neuropathological and neurological injuries have already been referenced for both animal models and humans [2]. At the cellular level, degradation of the cytoskeleton, changes in neurotransmitters, disruption of calcium homeostasis, mitochondrial disturbances, loss in membrane permeability and even altered gene expression have been observed [39,17]. More specifically, studies of cellular response after blast events provide evidence of degenerative processes in the neuron itself, not only through necrotic pathways but also through apoptotic pathways – or programmed cell death, at the origin of most brain dysfunctions [40,39,2].

Technical improvements now allow for the *in vivo* study of direct blast effects on animal brain without significantly invading the brain tissue [41,42], as well as *ex vivo* study to quantify the accompanying functional damage [12]. Additionally, a vast array of *in vitro* techniques, involving barotrauma chamber, rapid acceleration injury device or shock wave generator, allow for more flexibility, though at the cost of not taking into account the real environment provided under *in vivo* settings [43,44]. A wider set of experiments, ranging from simple stretch and isostatic pressurization to weight drop and stylus laceration, are also available to account for non-primary blast injuries, i.e. blast injuries arising

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from direct impact or penetration (secondary), collision arising from a fall of or onto the subject (tertiary), or exposure to gas, fire or similar (quaternary) [44]. Moreover, a recent study has directly compared *in vivo*, *in situ* and *in vitro* brain responses to different indentation rates [45], thus paving the way for more realistic constitutive models of brain tissue under high rate loadings. Coupled to these improvements in experimental testing, new imaging techniques can now achieve submicrometer resolution [46].

In parallel to these experimental efforts, recent complex large-scale parallel computational models accounting for fluid–solid interaction effects between the air blast and multiple organs in the cranium now allow for pressure extrema localization, and identification of more complex electromagnetic coupling effects with a very high precision [47–50].

At the cellular level, many groups have focused their efforts on the development of mechanical models of the deformation of individual cells or cell parts [34,51–81]. For instance, significant progress has been made on red blood cell (RBC) modeling, with full three-dimensional (3-D) models using finite-element-based continuum methods [55,66], coarse-grained molecular dynamics (MD) simulations [82,83], and dissipative particle dynamics (DPD) computations capable of describing detailed cell–fluid interactions [84]. These RBC models have been successfully applied to study diseases such as malaria [84,85]. Developing computational models for cells with a nucleus and a 3-D cytoskeleton network, however, has been much more challenging than for RBCs, which have a much simpler cytoskeletal structure and no nucleus.

Among the different techniques proposed in the literature to describe the mechanics of living cells with a nucleus and a 3-D cytoskeleton, the most notable involve: modeling the cytoskeleton as a simple mechanical elastic, viscoelastic or poroviscoelastic continuum [61,62], as a porous gel or soft glassy material [70], or as a “tensegrity” network incorporating discrete structural elements that bear compression [71]. At a smaller scale, cytoskeleton proteins and their interaction with the membrane have been more recently modeled using MD, coarse-grained MD and normal mode analysis [86–88]; however, the important length and time scale limitations of MD, coupled with the large number of unknowns either for the atomic interaction potentials or the protein interaction mechanisms, prevent its use at the cellular scale. Overall, it is observed that continuum models are flexible enough to allow for a relatively accurate representation of the geometry of cell parts (e.g. nucleus, cytoplasm and membrane/cortex), together with the individual macroscopic features of the deformation [51,52,54,57,63–65,67,68,70–74,35,80,76,81,77].

With a few notable exceptions, very little work has been dedicated to using such models under damaging – or, at least, high – rate loading conditions [34,77,78,80]. Such studies more often than not bring additional unknowns to the problem, but under loading rates fast enough to generally avoid the active deformation of the cell, i.e. the self-reorganization of its protein structures under external stimuli. As a consequence, continuum models *a priori* provide an adequate framework for neuron modeling under blast loading. Finally, to the best of our knowledge, direct simulations of the damaging effects of a blast on a cell with differentiated components has still not been achieved (note that Miller et al. presented a model of a cell subjected to stress waves but focused on cell–substrate decohesion [89,77]).

In this work, we thus propose a continuum model with differentiated nucleus, cytoplasm and membrane/cortex. Each one of these components is described by a visco-hyperelastic constitutive model. These models are purposefully chosen to be as simple as possible to adequately describe the different deformation mechanisms while reducing the size of the model parameters space. Each model is calibrated against published nanoindentation experimental results at multiple rates [78] and a fluid–structure interaction continuum

model of the calibrated cell is submitted to a blast wave. Section 2 introduces the constitutive framework and the finite element set-up for the simulations. The calibration of the model against experimental nanoindentation work is presented in Section 3 and the final blast simulation is shown in Section 4. Finally, the results are discussed and related to experimental studies in Section 5.

## 2. Numerical set-up

In this section, the visco-hyperelastic constitutive framework of all three modeled components is presented, followed by a description of the finite element model discretization and parametrization.

### 2.1. Constitutive framework

#### 2.1.1. General equations

The three main modeled cell components (membrane/cortex, cytoplasm and nucleus) are assumed to follow a visco-hyperelastic mechanical behavior.

For isotropic hyperelastic materials, it is generally assumed that a Helmholtz free energy function  $\Psi$  can be defined as a function of the Jacobian  $J$  and the modified strain invariants  $\bar{I}_1$  and  $\bar{I}_2$  [90].

The stress measure conjugated to the right Cauchy–Green tensor  $\mathbf{C}$ , the second Piola Kirchhoff stress  $\mathbf{S}$ , is then given by

$$\mathbf{S} = 2 \frac{\partial \Psi}{\partial \mathbf{C}} \tag{1}$$

#### 2.1.2. Generalized Maxwell model

The viscoelastic formulation used here is based on the work of Taylor et al. [91].

The generalized Maxwell model is a rheological model composed of a Hooke model (i.e. a spring) and a given number of Maxwell models – a Hooke model and a Newton model (i.e. a dashpot) in series – in parallel [92]. In order to minimize the number of model parameters, we couple the hyperelastic model defined earlier with a generalized Maxwell model composed of only one Maxwell component (see Fig. 1). It is the simplest model that allows consideration of both long-term and short-term elasticity with a viscous effect.

In Fig. 1,  $\mu_0$ ,  $\mu_1$  and  $\eta_1$  are respectively the long-term shear modulus, and the shear modulus and viscosity associated with the Maxwell component.  $\Gamma$  is the internal variable, a strain measure, associated with the dashpot, and  $\mathbf{S}_{iso} = \mathbf{S}_{vis} + \mathbf{S}_{iso}^\infty$  is the isochoric second Piola Kirchhoff stress defined as the sum of its viscous and long term components. This first tensor characterizes the viscous relaxation due to a viscous Newtonian fluid, and is representative here of all viscous effects arising in each one of the three components of the cell. It should be noted that these effects are restricted to the isochoric deformation mode. For more details on theory and implementation, see Ref. [90].

#### 2.1.3. Neo-Hookean model

As already stated, the work presented here is aimed at minimizing the number of parameters. As a consequence, the neo-Hookean

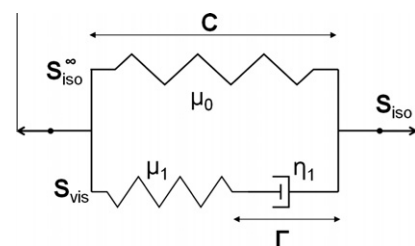


Fig. 1. First-order generalized Maxwell model.

model is chosen for all cell components. This model depends only on the Jacobian and the first strain invariant. The associated long-term volumetric and isochoric strain energy functions are given by [90]

$$\begin{cases} \Psi_{vol}^{\infty}(J) = \frac{1}{d_0}(J-1)^2 \\ \Psi_{iso}^{\infty}(\bar{I}_1) = c_0(\bar{I}_1-3) \end{cases} \quad (2)$$

where  $c_0 = \mu_0/2$  (see Section 2.1.2), and  $d_0$  is a material parameter related to the compressibility of the material.

#### 2.1.4. Hugoniot/Mie-Grüneisen equation of state

As long as relatively low strain rates and pressures are considered, the above description is reliable. However, when very fast material responses under high pressures are considered, such as the ones provoked by a shock wave, the volumetric part of the stress tensor, i.e. the pressure  $P$ , must be described by an equation of state. As a consequence, even though such an approach is not necessary for the indentation simulation, it is required for the blast simulation.

The shock response of many materials is described well by the Hugoniot relation between the shock velocity  $U_s$  and the material velocity  $U_p$  of the simple form [93]:

$$U_s = C_0 + sU_p \quad (3)$$

In this expression,  $C_0$  and  $s$  are material parameters which can be obtained from experiments.

By considering conservation of mass and momentum in a control volume at the shock front and Eq. (3), the final pressure<sup>1</sup> can be calculated explicitly as a function of the Jacobian behind the shock front  $J_H$  and the reference density ahead of the shock  $\rho_0$  [94]:

$$P_H = \frac{\rho_0 C_0^2 (1 - J_H)}{[1 - s(1 - J_H)]^2} \quad (4)$$

where  $J_H$  is related to the density  $\rho_H$ , the specific volume  $V_H$  or the deformation gradients tensor  $\mathbf{F}_H$ , defined behind the shock front, by:

$$J_H = \frac{\rho_0}{\rho_H} = \frac{V_H}{V_0} = \det(\mathbf{F}_H) \quad (5)$$

Alternatively, one can use the Mie-Grüneisen equation of state to relate the pressure  $P$  and the internal energy per unit mass  $E$  to their respective value on the Hugoniot curve  $P_H$  and  $E_H$  [93], which leads to

$$P = P_H \left( 1 - \frac{\Gamma_0}{2} \left( 1 - \frac{\rho_0}{\rho} \right) \right) + \Gamma_0 \rho_0 E \quad (6)$$

where  $\Gamma_0$  is the Grüneisen parameter in the initial state.

Finally, the internal energy rate per unit mass is given by the first law of thermodynamics as the sum of the volumetric and deviatoric work rates, and heat rate  $\dot{Q}$  [93]:

$$\dot{E} = -\frac{1}{\rho} \left( \frac{P\dot{\rho}}{\rho} + \dot{\Psi}_{iso} \right) + \dot{Q} \quad (7)$$

where use has been made of the deviatoric strain energy function, and where  $C_v$  is the specific heat capacity at constant volume and  $T$  is the temperature.

Additionally, the shock response can be considered as an adiabatic process:  $\dot{Q} = 0 \text{ J kg}^{-1} \text{ s}^{-1}$ . Note that the pressure release is actually isentropic, in general relatively close to the adiabatic process; as a consequence, the whole event can indeed be assumed as adiabatic [93].

The temperature can then be extracted easily from:

$$\dot{E} = C_v \dot{T} \quad (8)$$

An artificial viscosity scheme (necessary for shock wave propagation) is finally used (a complete description is provided in [Supplementary materials A-3](#)).

## 2.2. Finite element model

The main components that regulate the mechanical properties of the cell are the membrane, the cytoplasm (composed of the cytoskeleton and organelles bathed in a rheological fluid: the cytosol) and the nucleus [62]. The cytoskeleton is a dynamic structure that maintains the cell shape, protects it, enables cellular motion and plays an important role in all cellular processes. It contains three main mechanical structures with different functionalities: actin filaments, intermediate filaments and microtubules. The cell membrane is a semipermeable lipid bilayer that separates the interior of the cell from the outside. The cytoskeleton is found underlying the cell membrane in the cytoplasm and provides a scaffold for membrane proteins to anchor to, as well as enabling the formation of organelles that extend in and out of the cell. In fact, cytoskeletal elements interact extensively and intimately with the cell membrane, creating a region, just beneath the membrane, that is densely populated with proteins: the cortex [95]. Finally, the cell nucleus contains most of the cell's genetic material and is therefore the control center of the cell.

In the following, we detail the finite element discretization set-up for the calibration (nanoindentation) simulations and for the blast simulation. The commercial finite element software Abaqus was used for the simulations [96].

### 2.2.1. Nanoindentation finite element set-up

We propose here to follow the same overall geometry of a semi-spheroid as in Ref. [78], but focusing more on the intrinsic structures of the neuron, while simplifying the constitutive models for each modeled part, rather than adopting a more complex representative constitutive law for the whole neuron cell. The chosen modeled continua are the nucleus, the cytoplasm and the cortex plus membrane, see [Supplementary materials A](#).

The model size is based on the average height and diameter observed experimentally (from 79 observations) by Bernick et al. [78]: a height of 7.9  $\mu\text{m}$  for a diameter of 16.8  $\mu\text{m}$ . The nucleus is then considered as having a volume of one-third of the total cell volume [67]. Its dimensions are chosen such that the ratio of the diameters and heights of the full neuron cell and the nucleus are the same, i.e. the diameter and height are respectively 11.65 and 5.48  $\mu\text{m}$ . The nucleus is centered in the middle of the cell. The thickness of the “membrane plus cortex” region is estimated to be in the range of 100–400 nm [59,62]. For simplicity, a compromise value of 200 nm is chosen here. For the indentation simulation, the axisymmetry of the problem allows for the use of a 2-D axisymmetric mesh. The final mesh is shown in [Fig. 2](#). More details on the regions of interest, geometry and finite element mesh are given in [Supplementary materials A-1](#).

The boundary and loading conditions follow the set-up used in Ref. [78]. The bottom part is fixed in all directions, consistent with the experimental observation that the neuron is in slipless contact with its substrate [78]. The usual axisymmetric boundary conditions are specified along the axis of revolution. Finally, a 45  $\mu\text{m}$  diameter spherical bead is used for the nanoindentation and is modeled as an analytical rigid surface. The loading pattern is as follows: a first indentation at 0.3  $\mu\text{m s}^{-1}$  until a force of roughly 0.3 nN is measured; a plateau at the same position for 15 s; three load-unload cycles to 2  $\mu\text{m}$  additional depth at three increasing rates, 10, 1 and 0.1  $\mu\text{m s}^{-1}$ ; a final load at 10  $\mu\text{m s}^{-1}$  and a plateau

<sup>1</sup> In this section only, the pressure is by convention positive in compression.

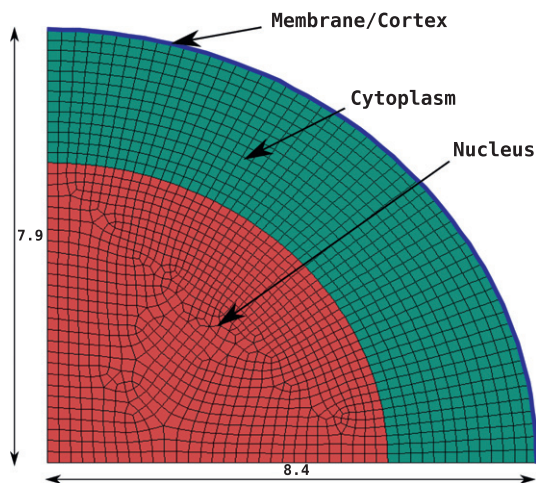


Fig. 2. 2-D axisymmetric mesh of the neuron used for nanoindentation (distances in  $\mu\text{m}$ ).

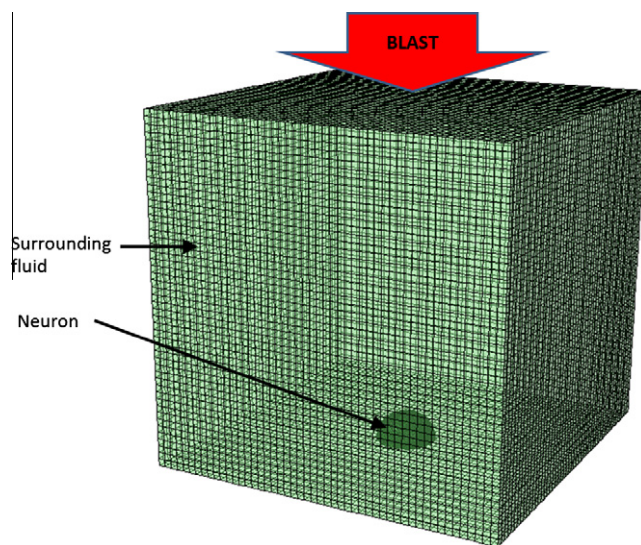


Fig. 3. Finite element set-up of the blast simulation.

at this depth for 120 s. See Ref. [78] for more details. Table 1 presents the different loading steps used in this reference.

A static implicit scheme is used for the nanoindentation simulation. Spatial convergence was verified. Note that the rates are small enough to ignore any inertial effect (the Reynolds numbers for the different model parts are in the range of  $2 \times 10^{-17}$ – $10^{-7}$ ), thus there is no need for dynamic simulations in this case.

2.2.2. Blast finite element model set-up

For the blast simulation, the previous cell model geometry is extended to three dimensions, with the same height and diameter and embedded at the bottom of a  $100 \mu\text{m} \times 100 \mu\text{m} \times 100 \mu\text{m}$  cubic fluid box. The final model is shown in Fig. 3. More details are given in Supplementary materials A-2.

The overpressure loading of a shock wave as emitted by a shock tube is typically of the order of hundreds of kPa (i.e. a few atm) with duration of the order of 1 ms [97]. However, recent in vitro studies have used laser-induced shock waves to study cell injury [98], as well as cell adhesion [89,77]. For such waves, the overpressure is of the order of 50 MPa [98] and the duration of the order of 5 ns for a Gaussian laser pulse [89].

Because the work proposed here is oriented towards the comparison of simulations with in vitro experiments, the pressure pulse used on the top face of the model follows the latter description: a constant applied pressure of 50 MPa for 5 ns.

3. Nanoindentation simulation

An extensive survey of the model parameter values that can be found in the literature is provided in Supplementary materials B.

The three cell components are considered to be incompressible, as is commonly assumed for biological cells [52,53,56,55,61,63,73,75–79]. Based on this incompressibility, the Poisson’s ratio is taken to be  $\nu = 0.5$  ( $d_o = 0$ ) for all regions. It should be emphasized, though, that other studies have suggested compressibility [99,74,81], in some cases with significant effects on the deforma-

tion mechanisms [74]. However, in view of the lack of consensus and the fact that, under shock loading (see Section 4), there is a priori not enough time for viscosity and/or volume change to occur, this value of 0.5 is chosen as a first approximation.

In view of the literature review, the value of 1000 Pa is chosen for the membrane/cortex Young’s modulus ( $c_0^{mem} = 166.67 \text{ Pa}$ ) and the relaxation time  $\tau_1^{mem}$  is taken as 3000 s (see Supplementary materials B-1). In the following, we determine the remaining parameters by calibrating them against the averaged experimental nanoindentation curve of Ref. [78], and validate them by comparing simulation and experiment for another cell-specific nanoindentation test [78].

It should finally be emphasized that in the proposed model the adhesion between cell and bead is not taking into account as a first approximation; for a modeling approach accounting for it, see Ref. [72].

3.1. Initial indentation depth and calibration of the Young’s moduli

As described in Section 2.2.1, the initial loading rate ( $0.3 \mu\text{m s}^{-1}$ ) is maintained until  $F_B = 0.3 \text{ nN}$  is reached (stages A and B in Table 1). Depending on the cell height, the indentation depth at which this load is reached consequently varies. Additionally, the final plateau of the loading at stage E yields an approximate force of  $F_E = 1.67 \text{ nN}$  in the average experimental curve [78].

Note that Hertz’s contact law does not apply here because of the multiple material stiffnesses of the cell regions. Both plateaux of stages B and E reach a steady-state value that is independent of viscosity by definition. As such, the only two remaining parameters of influence are the Young’s moduli of the cytoplasm and the nuclei,  $E_0^{cyto}$  and  $E_0^{nuc}$ . Assuming a factor of 4 difference between the two values (see Supplementary materials B-2), the set of unknown values defining both plateaux is narrowed down to two parameters only:  $\delta_0$  and  $E_0^{nuc}$  (or  $E_0^{cyto}$ ). Additionally, assuming that the contact

Table 1

Nanoindentation loading cycles followed by Bernick et al. [78] (rates are given in  $\mu\text{m s}^{-1}$ ; “0”, “+” and “–” refer to a plateau, loading and unloading, respectively, between the initial indentation depth  $\delta_0$  at Steps A and B to  $\delta_0 + 2 \mu\text{m}$ ).

Cycles	A	B	C <sub>1</sub>				C <sub>2</sub>				C <sub>3</sub>				D	E		
Load	+	0	+	–	+	–	+	–	+	–	+	–	+	–	+	–	+	0
Rate	0.3	0	10				1						0.1				10	0

is made in a similar way to Hertz's law but leaving the exponent  $n$  (fixed at 3/2 in Hertz's law) as a free parameter, one reaches:

$$\frac{\delta_0 + 2}{\delta_0} = \left(\frac{F_E}{F_B}\right)^n \quad (9)$$

This relation mathematically guarantees that the pair of unknowns  $(\delta_0, E_0^{nuc})$  is uniquely defined by the pair  $(F_B, F_E)$ . After calibration, we finally reach:

$$\begin{cases} \delta_0 = 1.41 \mu\text{m} \\ c_0^{nuc} = E_0^{nuc}/6 = 6.67 \text{ Pa} \\ c_0^{cyto} = E_0^{cyto}/6 = 1.66 \text{ Pa} \end{cases} \quad (10)$$

Note that the nucleus and cytoplasm values are in the lower range of the literature values (see Supplementary materials B-2).

### 3.2. Calibration of the viscosity parameters

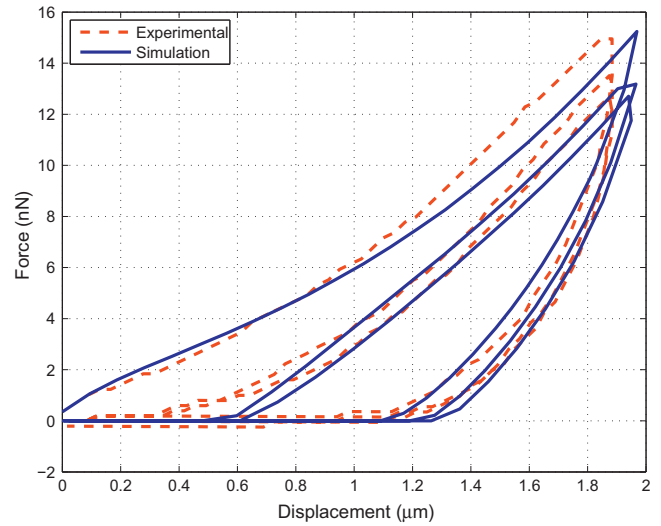
Because all the cell parts are taken as incompressible, the viscosity parameters are defined only for the shear component. The main difficulty of this calibration resides in the fact that five parameters need to be defined: the relaxation times  $\tau_1^{nuc}$  and  $\tau_1^{cyto}$ , the viscosities  $\eta_1^{nuc}$  and  $\eta_1^{cyto}$  for nucleus and cytoplasm, and also  $\eta_1^{mem}$  for the membrane/cortex. By considering that the factor of 4 between the long-term shear moduli of cytoplasm and nucleus is also valid for the shear moduli associated with the Maxwell components  $\mu_1$  (see Fig. 1), the space of the parameters is reduced to four unknowns:  $\tau_1^{nuc}$ ,  $\tau_1^{cyto}$ ,  $\eta_1^{nuc}$  (or  $\eta_1^{cyto}$ ) and  $\eta_1^{mem}$ . Note that picking a pair  $(\tau_1, \eta_1)$  is equivalent to picking  $(\tau_1, \mu_1)$ ; in the following we use the latter.

Despite the fact that simple viscous models have been chosen, the number of unknowns is relatively high. However, the advantage of having three cycles and two relaxation periods to fit the model is that each parameter is observed to influence the simulated curve in different ways. Without being able to fully guarantee the uniqueness of the parameters, we empirically observed that, around the final chosen values, changes in  $\tau_1^{nuc}$  and  $\tau_1^{cyto}$  affect the relaxation of the fast and slow cycles, respectively, while  $\mu_1^{nuc}$  (or  $\mu_1^{cyto}$ ) affects the peak values of the reaction forces at the maximum indentations, and  $\mu_1^{mem}$  affects most of the curve, albeit more lightly. As a consequence, most of the parameters have been calibrated by considering their action on the reaction-indentation curve patterns independently,  $\mu_1^{mem}$  being used to finalize the final fit. The final set of parameters is given in Table 2, and the set of curves for the three simulated cycles (done successively within the same simulation, as done experimentally) and the experimental curves taken from Ref. [78] are shown in Figs. 4–6. A good fit is obtained and the simulation results are well within the experimental error bars (not shown here; see Ref. [78]).

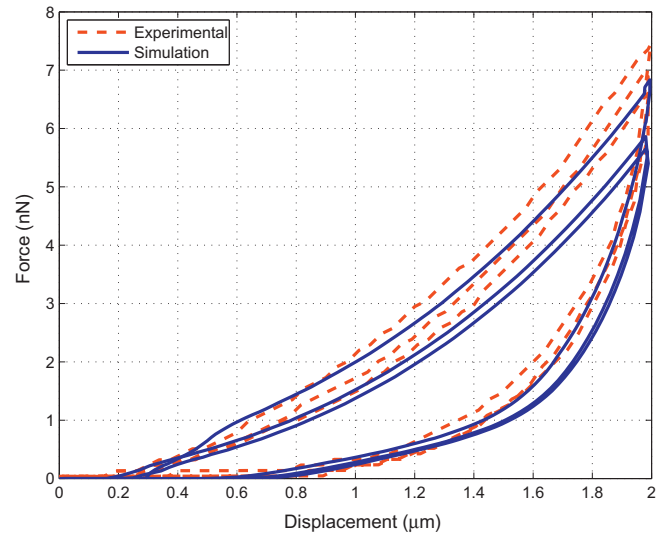
Note that the viscoelastic time constants for the nucleus and the cytoplasm  $\tau_1^{nuc/cyto}$  are in good agreement with the literature values (see Supplementary materials B-2). The membrane viscosity ( $\eta_1^{mem} = 41.67 \text{ kPa s}$ ) is slightly less than an order of magnitude smaller than the literature values (375 kPa s in Supplementary materials B-1), whereas the nuclear viscosity ( $\eta_1^{nuc} = 431.11 \text{ Pa s}$ ) lies within the literature range (52–1200 Pa s in Supplementary materials B-2).

**Table 2**  
Model parameters.

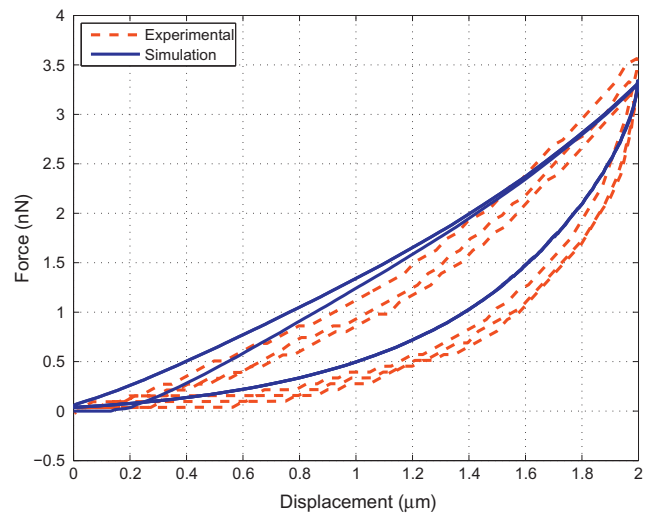
$\delta_0$	$c_0^{mem}$	$d_0^{mem}$	$\mu_1^{mem}$	$\tau_1^{mem}$	$c_0^{cyto}$
1.41 $\mu\text{m}$	166.67 Pa	0 Pa <sup>-1</sup>	13.89 Pa	3000 s	1.67 Pa
$d_0^{cyto}$	$\mu_1^{cyto}$	$\tau_1^{cyto}$	$c_0^{nuc}$	$d_0^{nuc}$	$\mu_1^{nuc}$
0 Pa <sup>-1</sup>	107.78 Pa	0.01 s	13.33 Pa	0 Pa <sup>-1</sup>	862.22 Pa
					$\tau_1^{nuc}$
					0.5 s



**Fig. 4.** Indentation force vs. displacement for the fast cycle ( $10 \mu\text{m s}^{-1}$ ).



**Fig. 5.** Indentation force vs. displacement for the medium cycle ( $1 \mu\text{m s}^{-1}$ ).



**Fig. 6.** Indentation force vs. displacement for the slow cycle ( $0.1 \mu\text{m s}^{-1}$ ).

However, the cytoplasmic viscosity ( $\eta_1^{cto} = 1.08 \text{ Pa s}$ ) is one to two orders of magnitude smaller than the full cytoplasm values (26–600 Pa s in [Supplementary materials B-2](#)), but just falls within the lower range of the crosslinked/bundled actin network ( $\sim 1\text{--}500 \text{ Pa s}$  in [Supplementary materials B-2](#)).

Finally, it should be emphasized that the literature values gathered here are from a wide range of cell types, and there is sometimes a wide range of values for the same type of cell. The observed discrepancy could be due to different experimental procedures, approximated modeling choices and/or differences in the culture of the cells. As a consequence, we complement this calibration with an additional validation step and compare simulation and experiment for an additional cell-specific nanoindentation test [78].

### 3.3. Validation

The validation is done by comparing the experimental results for another specific representative cell (as opposed to the average response in the previous section) with a diameter of 14.2  $\mu\text{m}$  and height of 7.6  $\mu\text{m}$ , similarly to what is done in Ref. [78], from which the experimental results are extracted.

The mesh presented in Section 2.2.1 was modified to account for the change in height and diameter, and all the parameters, except  $\delta_0$ , were taken from Table 2.  $\delta_0$  was then adjusted to reach the initial force of 0.3 nN, and the same loading pattern as before was used for the simulation. A value 0.84 nm for  $\delta_0$  was found. The final indentation force at each of the three maxima in each of the three cycles was extracted and compared to the experimental results (see Table 3).

Taking into account the large variability in the cell geometry (including experimental error, non-constant diameter and nucleus position within the cytoplasm), the model always captures the maximum forces within 17% of the experimental value, with an overall average error of 8.4%. These results confirm the ability of the model to capture the main rate-dependent deformation features operative here.

## 4. Blast simulation

In the following, we use the previously calibrated model and modify the volumetric contribution of the constitutive material model following Section 2.1.4. The new material parameters are then given and the simulation is analyzed. The corresponding stress patterns are finally compared with those for the indentation.

### 4.1. Modifications and new material parameters

#### 4.1.1. Surrounding fluid

As a constitutive description of the fluid deformation in the Eulerian mesh is beyond the scope of this work, we simply describe the parameters of the surrounding fluid. For more information on its implementation, see the documentation of Abaqus [96].

The Hugoniot/Mie-Grüneisen equation of state presented in Section 2.1.4 has been used successfully to describe shock wave

propagation in water below 1 GPa, which is the case here [100]. Because water is the main constituent of the surrounding fluid in *in vitro* laser-shock experiments [98], we chose water for the surrounding fluid in the cubic box [100].

$$\begin{cases} \rho_0 = 1000 \text{ kg m}^{-3} \\ C_0 = 1450 \text{ m s}^{-1} \\ s = 1.99 \end{cases} \quad (11)$$

Additionally, for water at ambient conditions, the Grüneisen parameter, the specific heat capacity at constant volume and the dynamic (Newtonian) viscosity  $\eta$  are taken as [101–103]:

$$\begin{cases} \Gamma_0 \approx 0.1 \\ C_v = 4184 \text{ J kg}^{-1} \text{ K}^{-1} \\ \eta \approx 0.001 \text{ Pa s} \end{cases} \quad (12)$$

#### 4.1.2. Neuron

As described previously, under shock loading conditions, the volumetric contribution of the stress needs to be described by an equation of state. The Hugoniot/Mie-Grüneisen has been shown to be a good candidate for the description of biomaterials submitted to shock loading [104]. Assuming the compressibility of the cell is similar to that of water (see Section 3), we use the water values for  $\rho_0$ ,  $C_0$ ,  $s$ ,  $\Gamma_0$  and  $C_v$  for the cytoplasm and nucleus. Note that, because of its shell formulation, the cortex/membrane volumetric constitutive model could not be easily replaced by an equation of state, and was kept as hyperelastic as a first approximation.

It must finally be emphasized that the deviatoric contribution of the stress is not assumed to follow the dynamic Newtonian viscosity of water, but remains the same as in the indentation model.

### 4.2. Simulation results

The blast simulation was run for 150 ns and the convergence was checked.

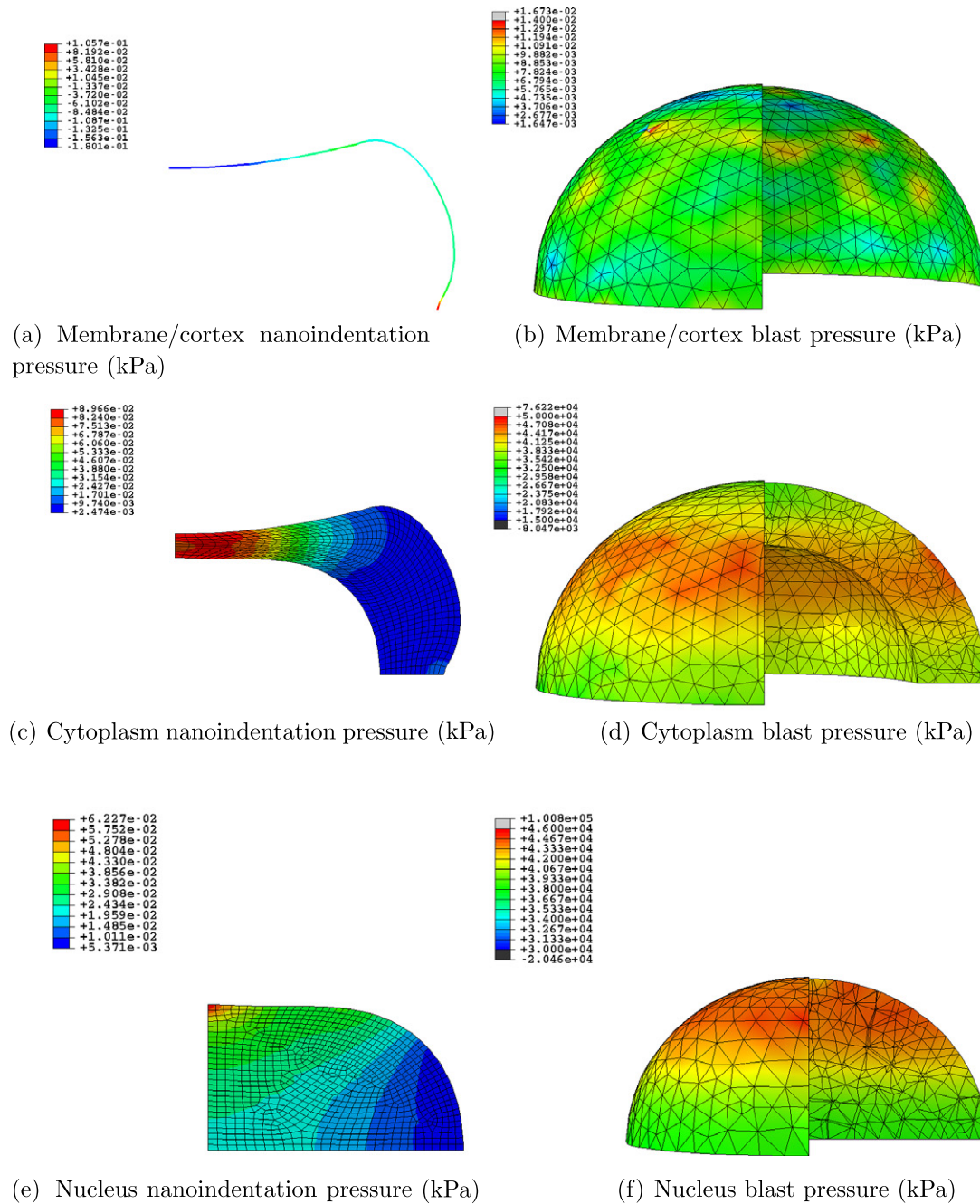
Figs. 7 and 8 show the pressure and von Mises stress fields for the different regions at 26.88 s for the nanoindentation simulation (which corresponds to the first indentation peak, with maximum pressure and von Mises stress) and 65.5 ns for the blast simulation (which corresponds to the time at which the wave has crossed half the cell, as a good compromise between the moment the wave hits the membrane and the moment it bounces back from the substrate, thus roughly doubling the pressure level). Note that maximum compression is reached at 70 ns in the blast simulation, i.e. the results shown are at almost maximum deformation. Fig. 9 shows the temperature increase for the whole cell during the blast event. Videos of the pressure field evolution during the blast for the whole mesh, as well as for the individual cell parts, are available as [Supplementary materials](#).

Fig. 7 shows that, whereas the pressure is mainly concentrated in the cytoplasm and the top of nucleus directly underneath the indenter in the nanoindentation case, it follows the wave along the horizontal propagating plane in the blast case. Furthermore, the pressure is discontinuous in the former case at the cortex–cytoplasm (with a jump of  $\sim 300 \text{ Pa}$ ) and cytoplasm–nucleus (with a jump of  $\sim 30 \text{ Pa}$ ) interfaces, and continuous in the latter. It can thus be concluded that the blast event propagates hydrostatic stress in a less material-specific way than is done at lower rate deformations.

Interestingly, the von Mises stress levels are of the same orders of magnitude for both simulations (see Fig. 8), with maxima of  $\sim 10\text{--}100 \text{ Pa}$ . Note that this result is even more surprising, considering that the typical cell viscosity characteristic time is of the same order of magnitude as our nanoindentation duration (seconds) [68], but much larger than that of the blast event

**Table 3**  
Comparison between the maximum forces of an indentation experiment [78] (Exp) and simulation (Sim) for a specific representative cell;  $C_{\alpha,\beta}$  refers to cycle  $\alpha$ , maximum loading  $\beta$  (see Table 2).

Cycle	$C_{1,i}$	$C_{1,ii}$	$C_{1,iii}$	$C_{2,i}$	$C_{2,ii}$	$C_{2,iii}$	$C_{3,i}$	$C_{3,ii}$	$C_{3,iii}$
Exp (nN)	11.5	10.8	10.3	5	4.9	4.8	3	3	3
Sim (nN)	11.5	11	10.2	5.3	4.6	4.3	2.5	2.5	2.5
Error (%)	0	2	1	6	6	10	17	17	17



**Fig. 7.** Pressure field (kPa) for the nanoindentation and blast simulations at 26.88 s and 65.5 ns, respectively, for the three regions; a quarter of the mesh for the blast simulation has been removed for visualization purposes.

(nanoseconds). However, whereas the shearing forces are concentrated mainly within the nucleus in the nanoindentation case, the maxima can be identified at the interfaces in the blast case.

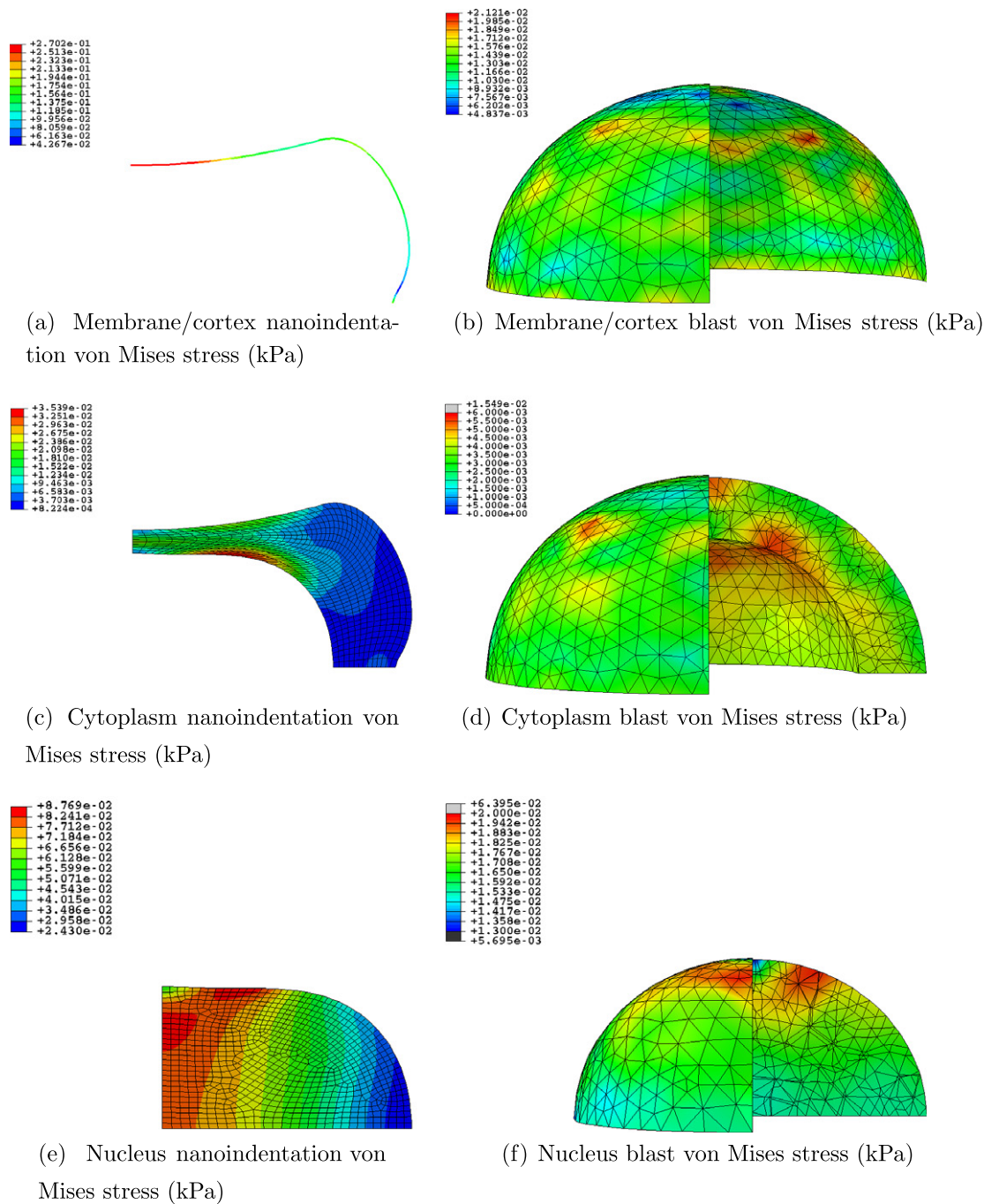
Finally, it can be seen from Fig. 9 that the temperature is rising by  $\sim 0.1$  °C.

## 5. Discussion

The high pressure ( $\sim 50$  MPa) is propagated directly from the water into the cell, and in between the cell parts, mainly because of the lack of a volumetric impedance mismatch (the equation of state parameters are the same). It could thus be relevant to have accurately calibrated parameters for each part of the cell in order to observe the effect of such possible mismatches. However, the

volumetric material parameters would still remain relatively similar, and a drastic change in pressure should not be expected. Based on brain tissue studies [48], such high pressure should a priori be sufficient to cause a high degree of brain damage. This conclusion is confirmed by the fact that the rates used here are much higher than those used as tissue damage criteria in other works on impact [26,27] or blast [48,97].

Other works have focused directly on the cell by increasing the pressure up to  $\sim 2$  MPa (20 atm) over a period of 6 s and sustaining it for 1–10 min [43]. If such work leaves aside the rate effects, it has the benefit of independently identifying the effect of sustained pressure on cell components. Specifically, membrane damage was observed above 10 atm, eventually leading to irreversible damage under sufficient pressure and duration [43]. Additional



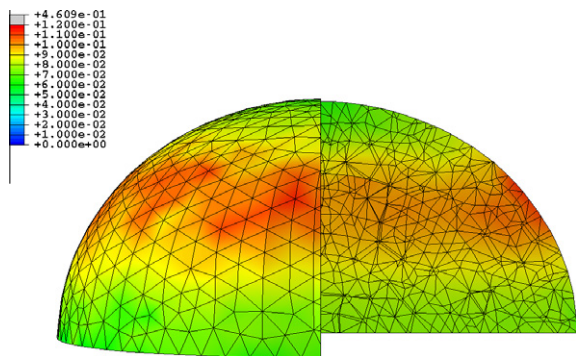
**Fig. 8.** Von Mises stress field (kPa) for the nanoindentation and blast simulations at 26.88 s and 65.5 ns, respectively, for the three regions; a quarter of the mesh for the blast simulation has been removed for visualization purposes.

works have similarly focused on the effect of such high hydrostatic pressure on cell functions such as migration [105]. By studying the release of fatty acids and lactate dehydrogenase into the extracellular medium under different pressure levels/durations, Murphy and Horrocks [43] identified damage thresholds for different types of cells. They proposed that, under high pressure, the motion of the membrane’s acyl chains is reduced as they condense to accommodate their volume decrease. By so doing, the viscosity is reduced and the “fluid behavior” of the membrane is modified to a stiffer configuration, eventually leading to receptor damage [43]. Along the same lines, recent work by Alford et al. suggests that, under rapid blast-driven stretching, the stimulation of cellular membrane

integrins is altered, thus potentially modifying the calcium dynamics and phenotypic behavior in the affected cells [17].

Such experimental findings are corroborated by the von Mises stress fields in Fig. 8. These results show that one of the main features of a blast event is the localized concentration of the von Mises stress at the interfaces within the blast wave plane. The resulting interface shearing effect could have drastic implications on the organization of receptors, transmembranes organelles and associated cytoskeletal components (e.g. in the cortex). The coupling effect of the mechanical loading of the membrane receptors due to pressure and shearing at the interface could thus lead to their alteration. More specifically, the loss of membrane integrity,



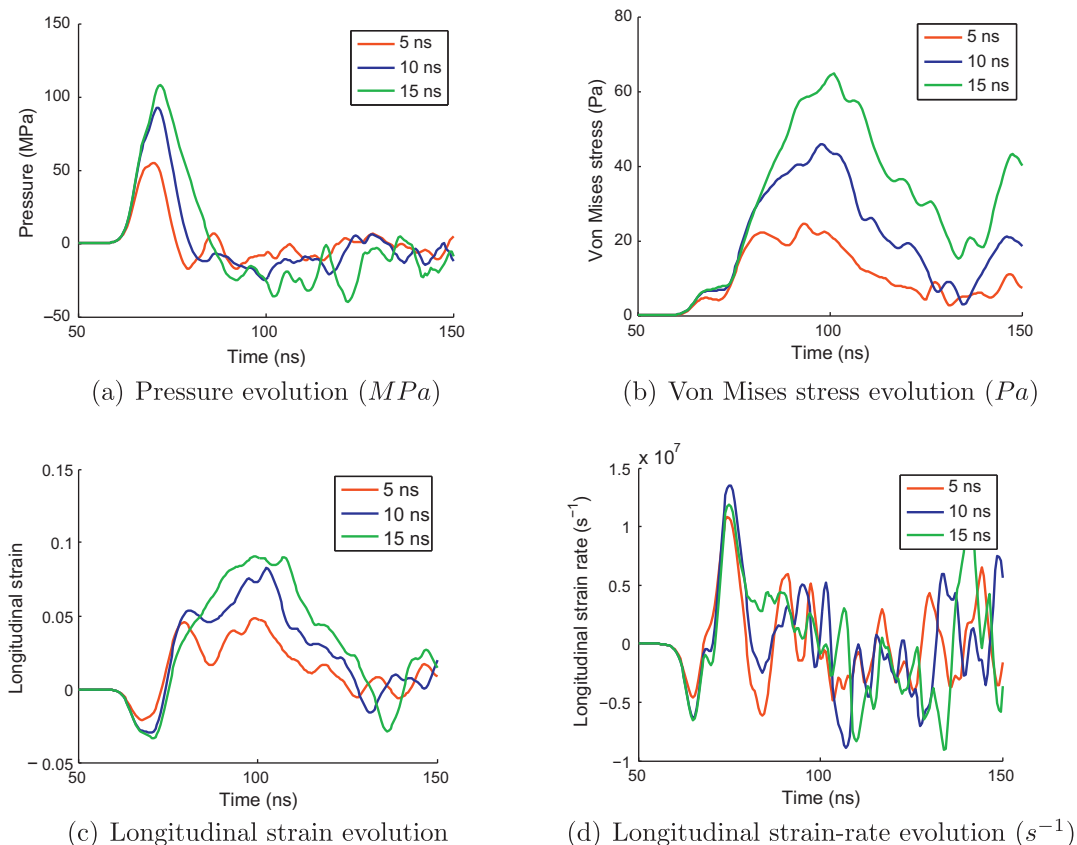


**Fig. 9.** Temperature increase field (K) for the blast simulation at 65.5 ns for the whole cell; a quarter of the mesh has been removed for visualization purposes.

despite the presence of reversible repair mechanisms below some pressure/duration limits, is a common type of damage in all catastrophic types of cell death. For instance, apoptosis and the detachment of the F-actin cortex from the membrane have been directly related [106], and a direct relation between cell death and loss of membrane integrity has also been observed in necrosis and necroptosis [107–109]. The recent work of Alford et al. on the role of integrin alteration in phenotypic switching confirms that point [17]. Note finally that, to the best of our knowledge, no experimental findings of loss of integrity of the nucleus membrane have been reported. However, the model predicts similar shear stress levels at both the nucleus membrane and the overall cell membrane, and thus potentially similar damage patterns for both the nucleus and cell membranes.

Using shock tube experimental set-ups with different configurations, Reneer et al. have recently highlighted a direct correlation between a longer positive phase duration and a higher level of damage at the same peak pressure [42]. In order to compare this experimentally observed trend to our numerical predictions, the initial shock positive phase duration was extended from 5 ns to 10 and 15 ns. The pressure, von Mises stress, longitudinal (in the shock direction) strain and longitudinal strain rate evolutions for a material point situated along the interface between the cytoplasm and the nucleus at roughly 75% of the total height of the nucleus were measured (see Fig. 10). The results confirm the experimental findings by predicting higher pressure, von Mises stress, strain and strain rate with increasing durations. The von Mises stress level, in particular, has been found to increase proportionally with the duration (doubling and tripling for doubled and tripled durations), thus potentially aggravating the effect of shearing at the interface. The strain rate, however, was found to increase only moderately.

As a consequence, our simulations confirm that laser-induced shock wave experiments on cells lead to interface damage within the cell. The fact that a blast wave seems to concentrate shear forces at these particular regions while potentially debilitating some of its functions through pressure-dependent structural reorganization of the membrane is even more relevant for neurons. Indeed, whereas large strains seem to be sustained by the axon membrane at low rates, high rates of deformation are known to drastically affect the conduction and thus functional properties of axons [110]. This confirms that the model prediction of shear localization at the cortex, potentially exacerbated by a longer positive phase duration, has direct implications on the functional properties of the neuron, and consequently the brain.



**Fig. 10.** Pressure, von Mises stress, longitudinal strain and strain rate evolution at the nucleus–cytoplasm interface, at ~75% of the nucleus height, for three initial positive phase durations: 5, 10 and 15 ns.

Finally, the temperature rise (see Fig. 9) can a priori be judged as too small to damage the cell and/or affect the cell's health. Accordingly, although thermal shock has been shown to have a significant impact on cytoskeletal organization, potentially leading to microtubule malfunctions [111], the experimental temperature change used in that reference is two orders of magnitude higher than here. However, it must be emphasized that the increase of 0.1 °C observable in the cell is achieved in roughly 5 ns, which corresponds to a rate of 20 million °C s<sup>-1</sup>. It is thus not clear if the temperature rate itself, and not just the level reached, is relevant to the cell's health. Molecular dynamics studies could potentially allow for further investigations in this direction.

## 6. Conclusion

In this work, a comprehensive continuum model of a neuron was presented. This model involves the consideration of three independent regions: the nucleus, the cytoplasm and the cortex plus membrane. Each region is described by a constitutive model based on visco-hyperelasticity and an equation of state for high rate/pressure loadings. The parameters that were not taken from the literature were calibrated against published experimental multi-rate indentation results. Finally, a blast event within typical in vitro conditions was simulated.

The results show that, whereas the pressure level affects the cell homogeneously, shearing effects are observed mainly at the interfaces. This phenomenon has been shown to be critically important for the integrity and health of cell membranes, confirming what was observed experimentally at the cell function level. Finally, both the pressure and the von Mises stress, and thus the potential damage, have been observed to increase significantly with increased positive phase duration of the shock wave.

In conclusion, the presented model successfully captures some of the intrinsic intracellular phenomena that occur during the rate-dependent neuron deformation and potentially lead to damage. It also predicts that the nucleus membrane is likely to suffer from the same type of damage as has been observed for the cell membrane. Ultimately, the proposed model constitutes a novel numerical tool that is able to predict some of the most complex cell deformation mechanisms occurring during traumatic brain injury.

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## Appendix A. Figures with essential colour discrimination

Certain figures in this article, particularly Figs. 2–10, are difficult to interpret in black and white. The full colour images can be found in the on-line version, at <http://dx.doi.org/10.1016/j.actbio.2012.04.039>.

## Appendix B. Supplementary data

Supplementary data associated with this article can be found, in the online version, at <http://dx.doi.org/10.1016/j.actbio.2012.04.039>.

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